



# The CaFe Experiment:

## Isospin Dependence of Short-Range Correlations in Nuclei

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H. Szumila-Vance, L.B.Weinstein

Hall C Experiment-Theory Working Group Meeting

April 15, 2024

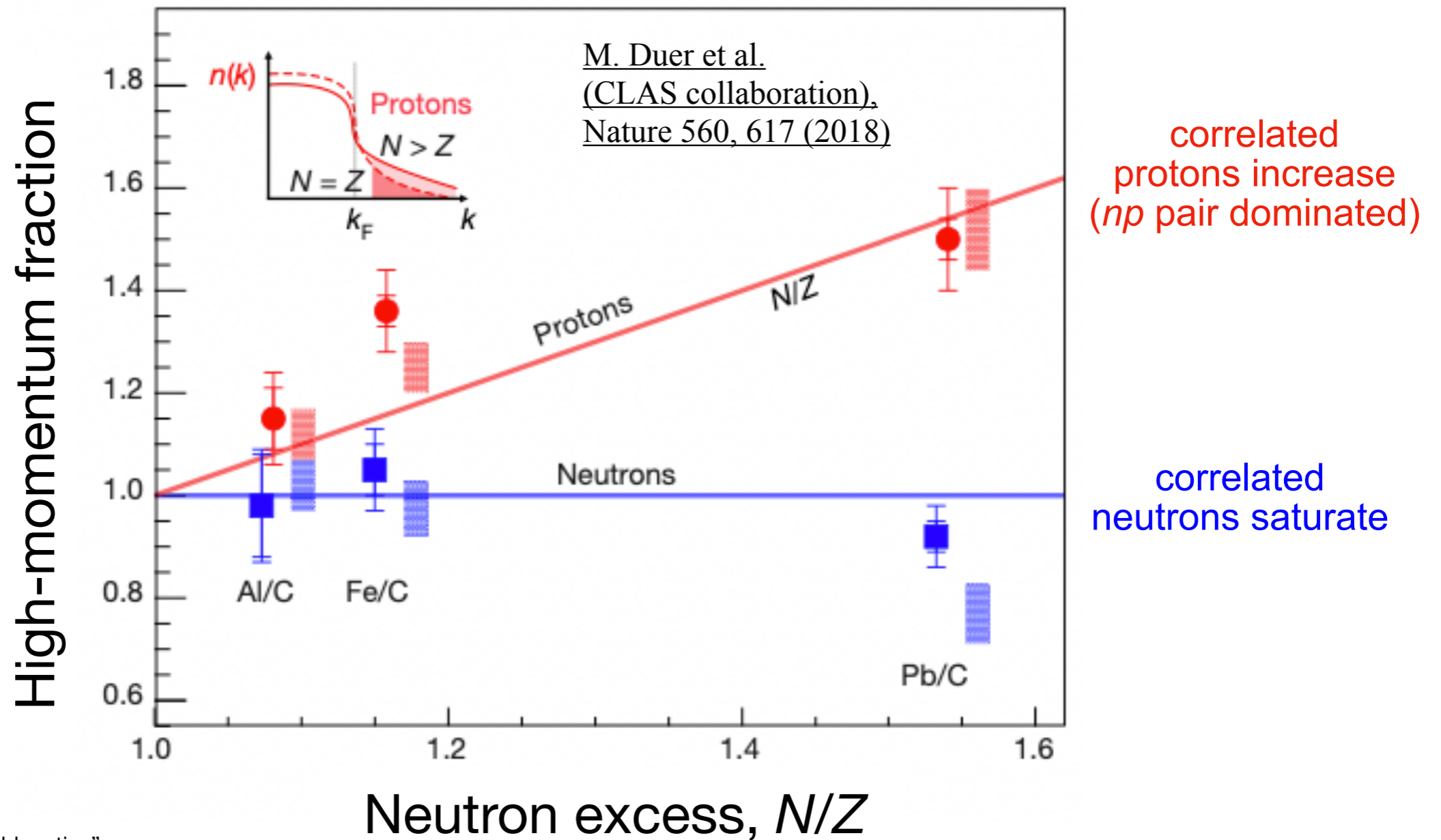


**Proposal: PR12-16-004**

**Spokespeople:** D. Higinbotham (JLab), F. Hauenstein (JLab), O. Hen (MIT), L. Weinstein (ODU)



# which nucleons form SRC pairs ?

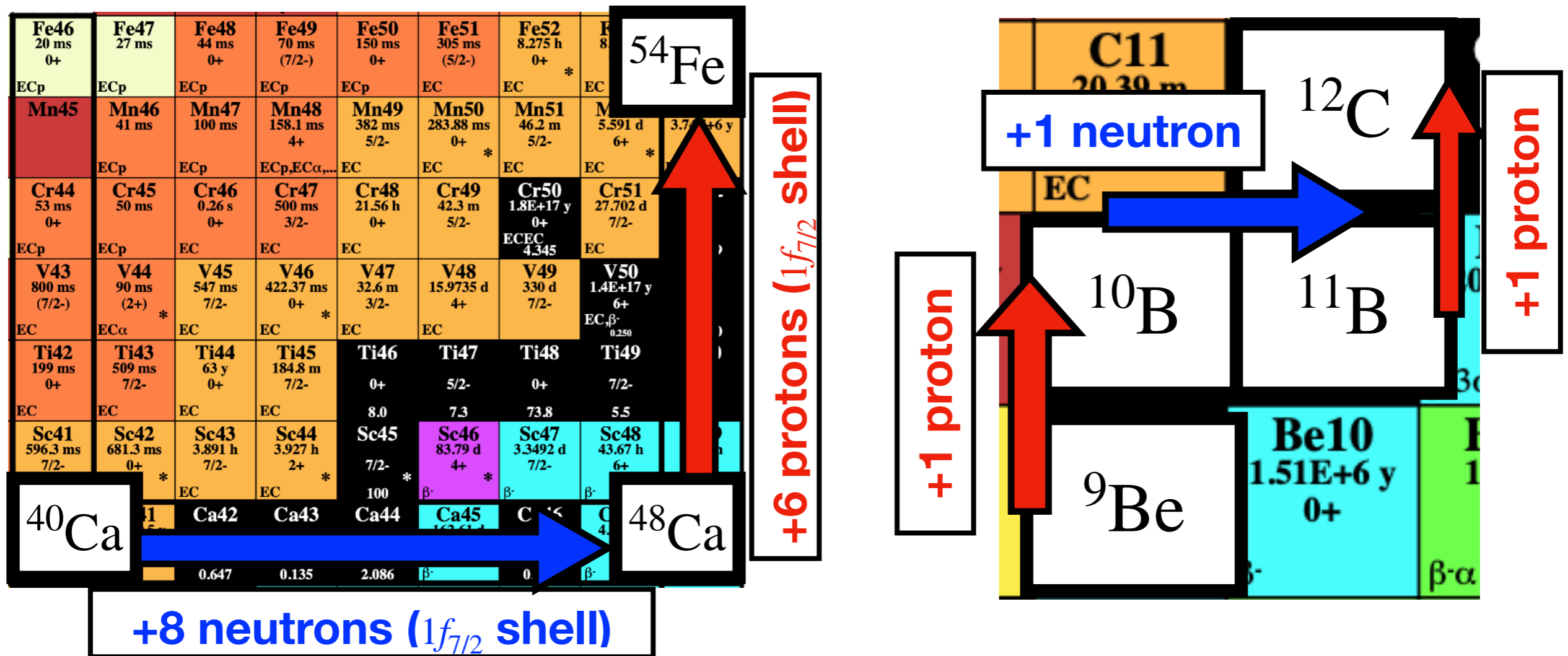


High-momentum fraction a.k.a. “double ratios”

$$\frac{A(e, e'p)^{SRC} / A(e, e'p)^{MF}}{^{12}\text{C}(e, e'p)^{SRC} / ^{12}\text{C}(e, e'p)^{MF}}$$

How does NN-SRC pairing change with mass ( $A$ ) and asymmetry ( $N/Z$ ) ?

# which nuclei to investigate ?



Which nucleons form pairs?

- ▶ How does adding +8 1f<sub>7/2</sub> neutrons to a 2s1d closed shell <sup>40</sup>Ca change the proton pairing?
- ▶ How does adding +6 1f<sub>7/2</sub> protons to <sup>48</sup>Ca change the proton pairing?
- ▶ What about adding +1p, +1n in light nuclei? <sup>9</sup>Be → <sup>10</sup>B → <sup>11</sup>B → <sup>12</sup>C

\* we also took data on Au197

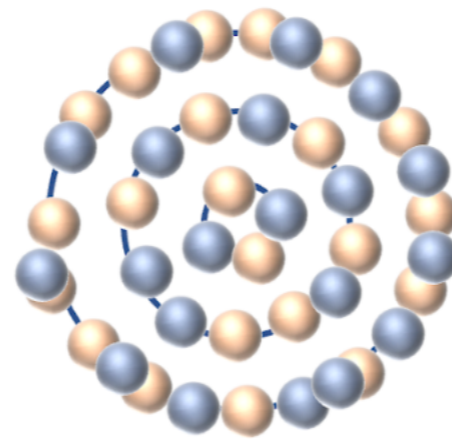
# CaFe Triplet Shell Diagram

Diagram/Picture by: Larry Weinstein / Or Hen

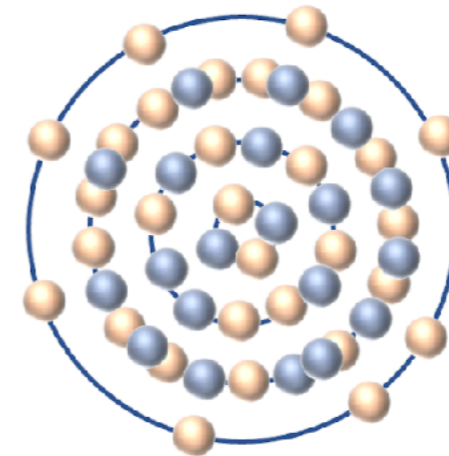
CaFe @ Hall C will answer:

- Which bound nucleons form pairs?
- How does adding ( $n$  or  $p$ ) independently change  $NN$  pairing?

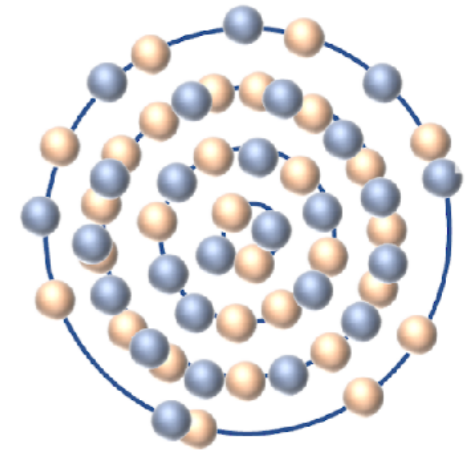
Ca-40



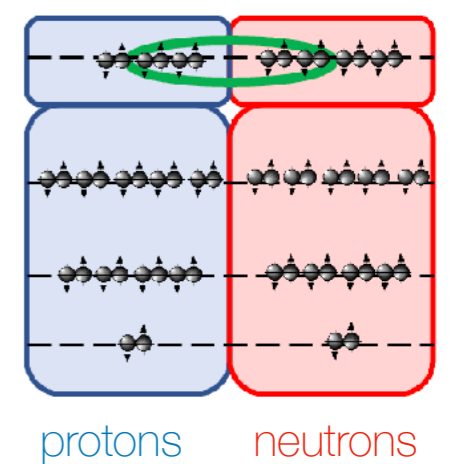
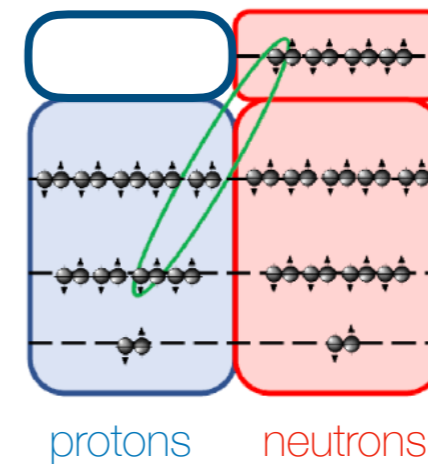
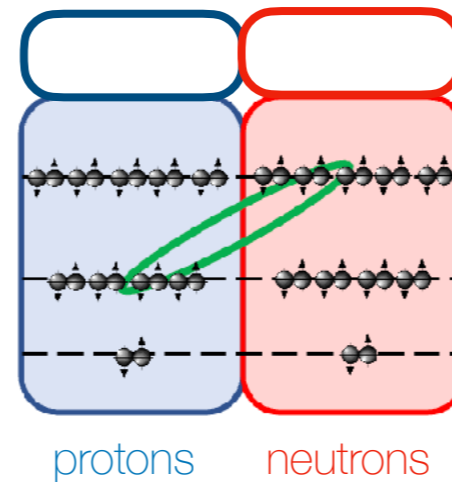
Ca-48  
+8 neutrons



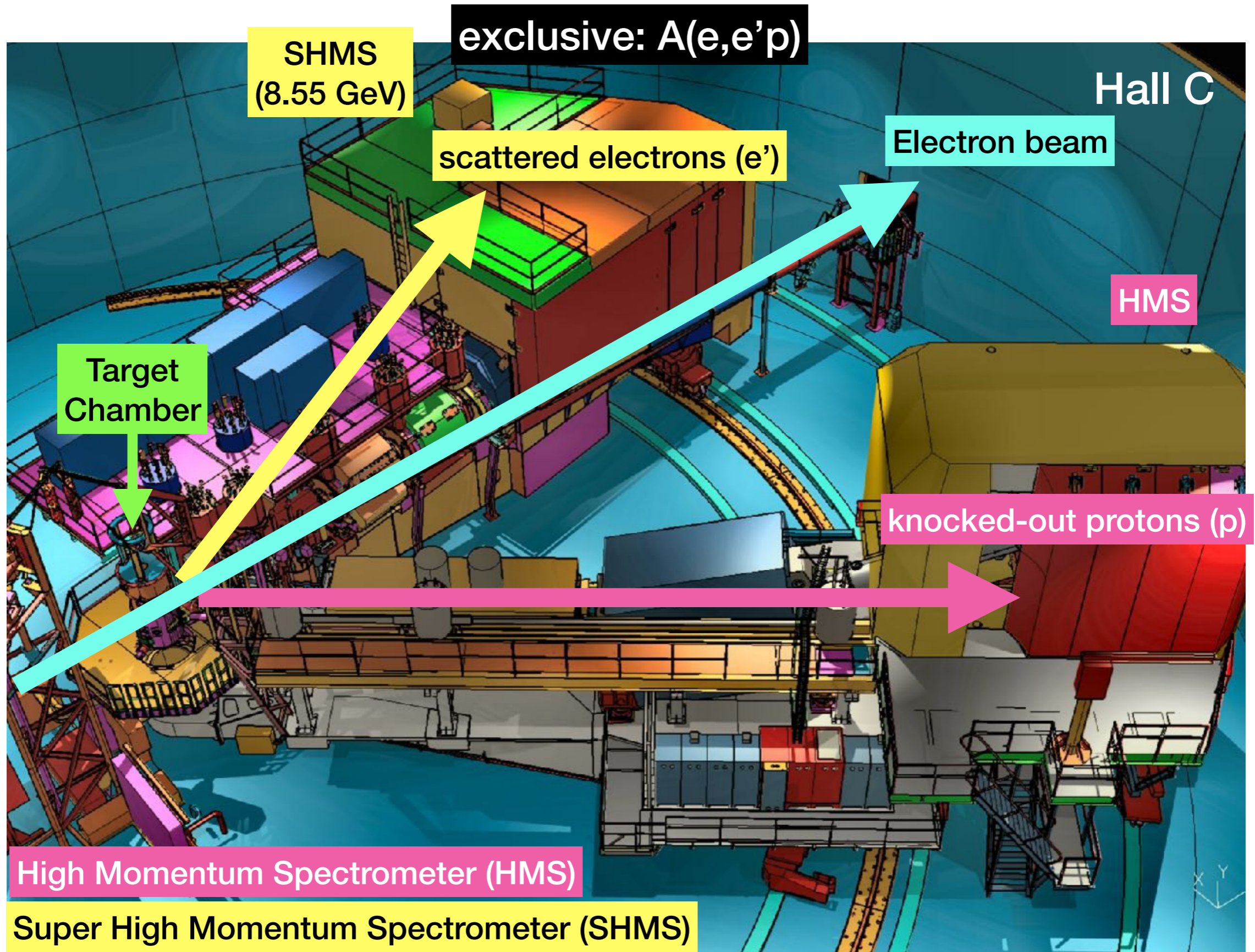
Fe-54  
+6 protons



1f7/2  
Shells  
1s,1p,2s1d

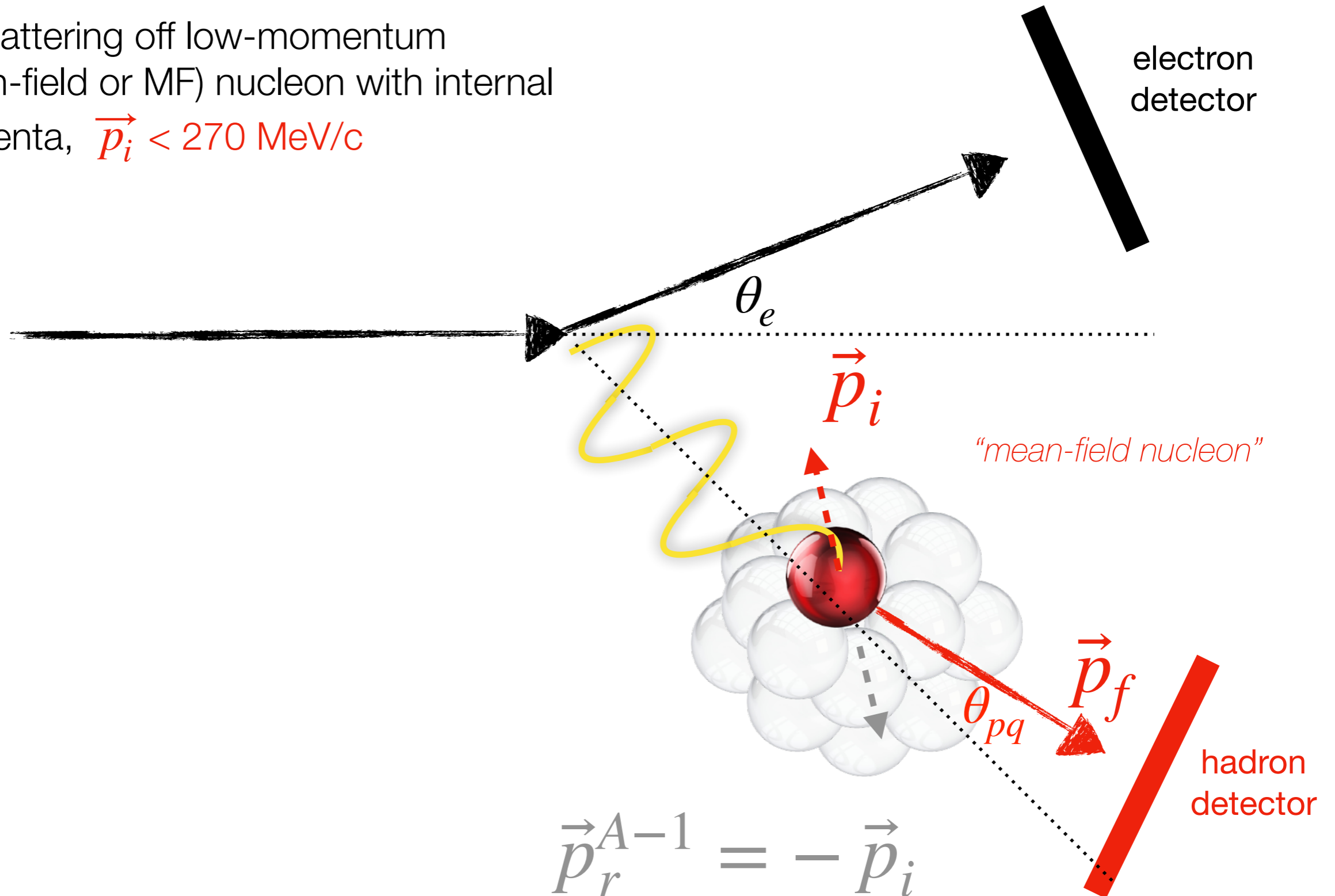


# CaFe Experiment Setup @ Hall C



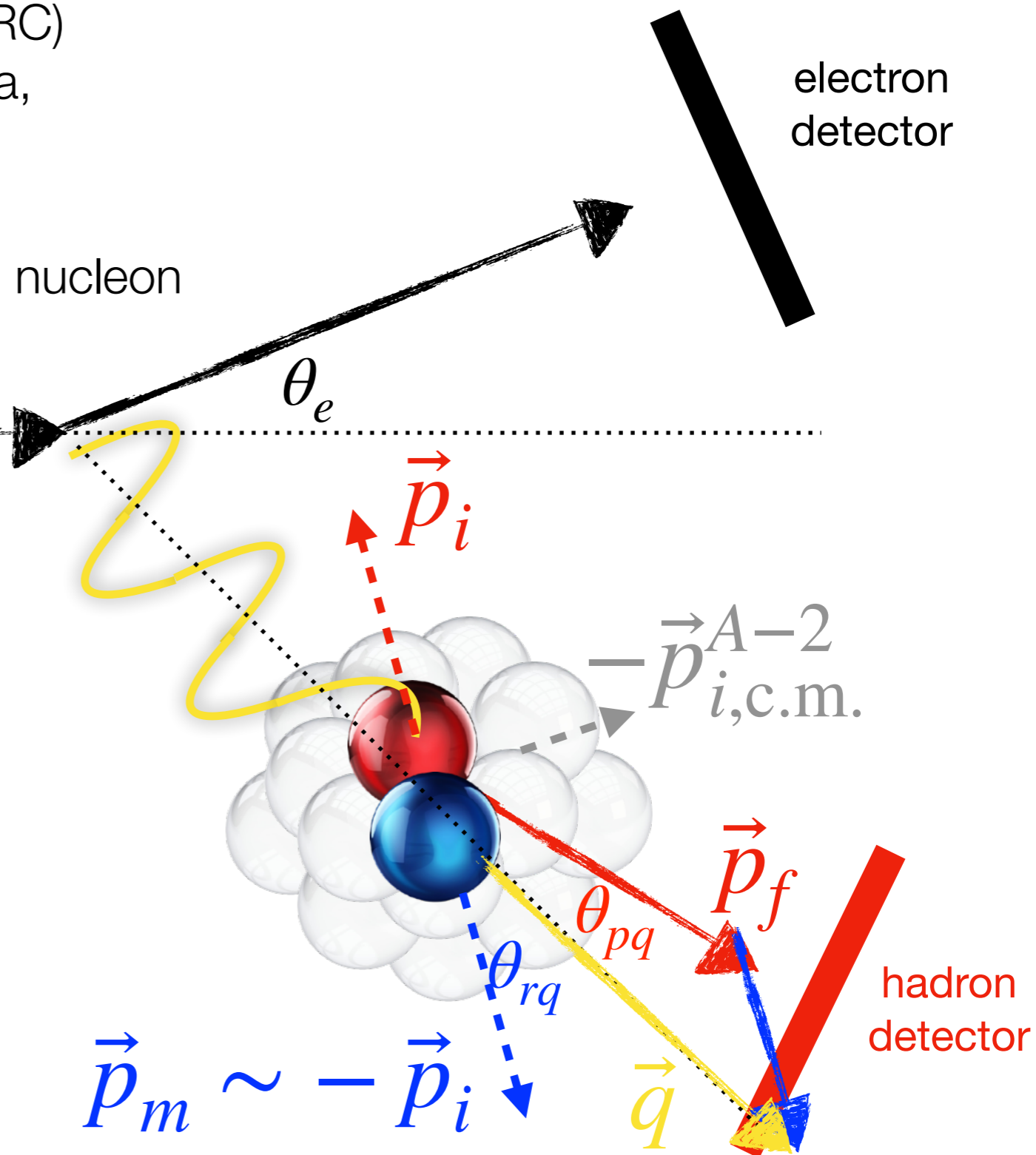
# exclusive: $A(e, e'p)$ @ MF

- e- scattering off low-momentum (mean-field or MF) nucleon with internal momenta,  $\vec{p}_i < 270 \text{ MeV}/c$



# exclusive: $A(e, e'p)$ @ SRC

- e- scattering off high-momentum (SRC) bound nucleon with internal momenta,  $\vec{p}_i > 375 \text{ MeV}/c \sim 700 \text{ MeV}/c$
- reconstructed (undetected) “missing” nucleon momenta,  $\vec{p}_m = \vec{q} - \vec{p}_f$



- plane-wave impulse approximation (PWIA)
  - ▶ no further re-interaction between **knocked-out** and **missing** nucleon
  - ▶ recoil momentum unchanged,  $\vec{p}_r \sim -\vec{p}_i$
  - ▶ FSI significantly reduced at neutron recoil angles  $\theta_{rq} \lesssim 40^\circ$   
(Sargsian and Boeglin, Int.J.Mod.Phys.E 24 (2015) Modern Studies of the Deuteron: From the Lab Frame to the Light Front)

# Kinematics

NOTE: put the actual central momentum used (based on histos)

Beam Energy:  $E_b = 10.6 \text{ GeV}$

Targets: 9Be, 10B, 11B, 12C, 40Ca, 48Ca, 54Fe, 197Au

KIN	$k_e$ (GeV/c)	$\theta_e$ (deg)	$p_f$ (GeV/c)	$\theta_p$ (deg)	$Q^2$ (GeV <sup>2</sup> )	$P_{\text{miss}}$ (GeV/c)
<b>MF</b>	9.4	8.3	1.820	48.3	>1.8	<b>0.150</b>
<b>SRC</b>	9.4	8.3	1.325	66.4	>1.8	<b>0.400</b>

## Mean Field (MF) Kinematics

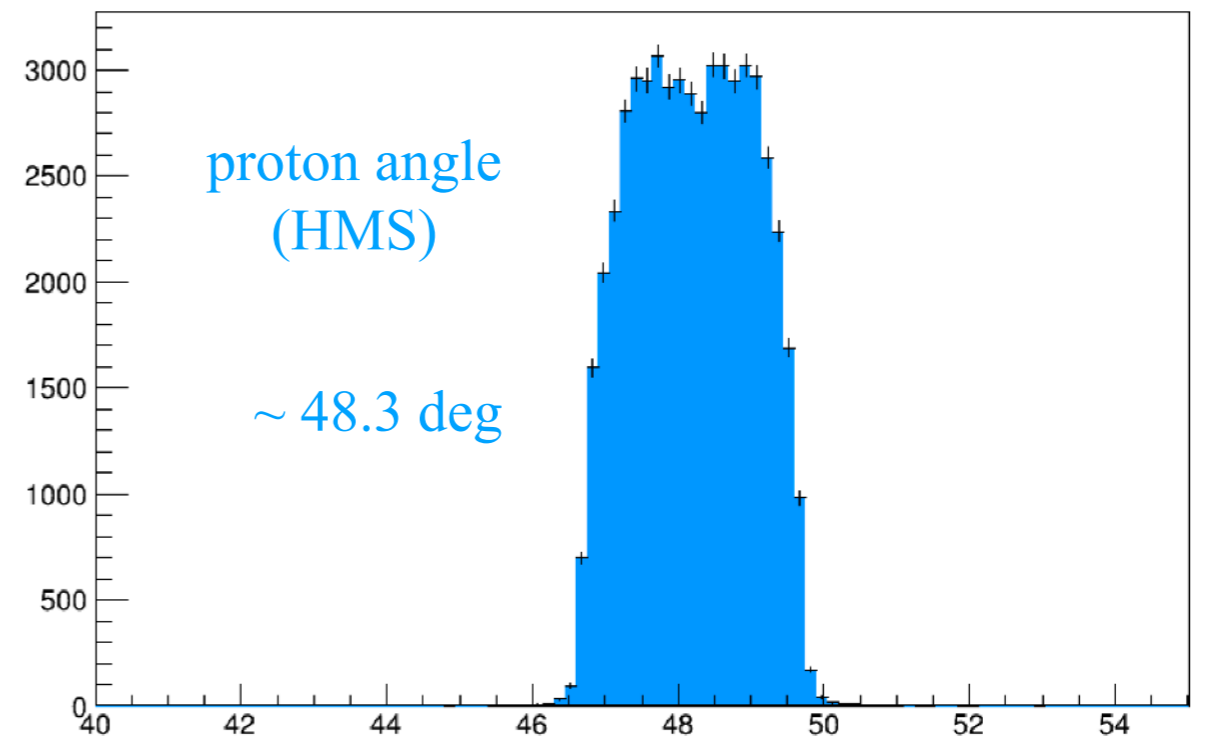
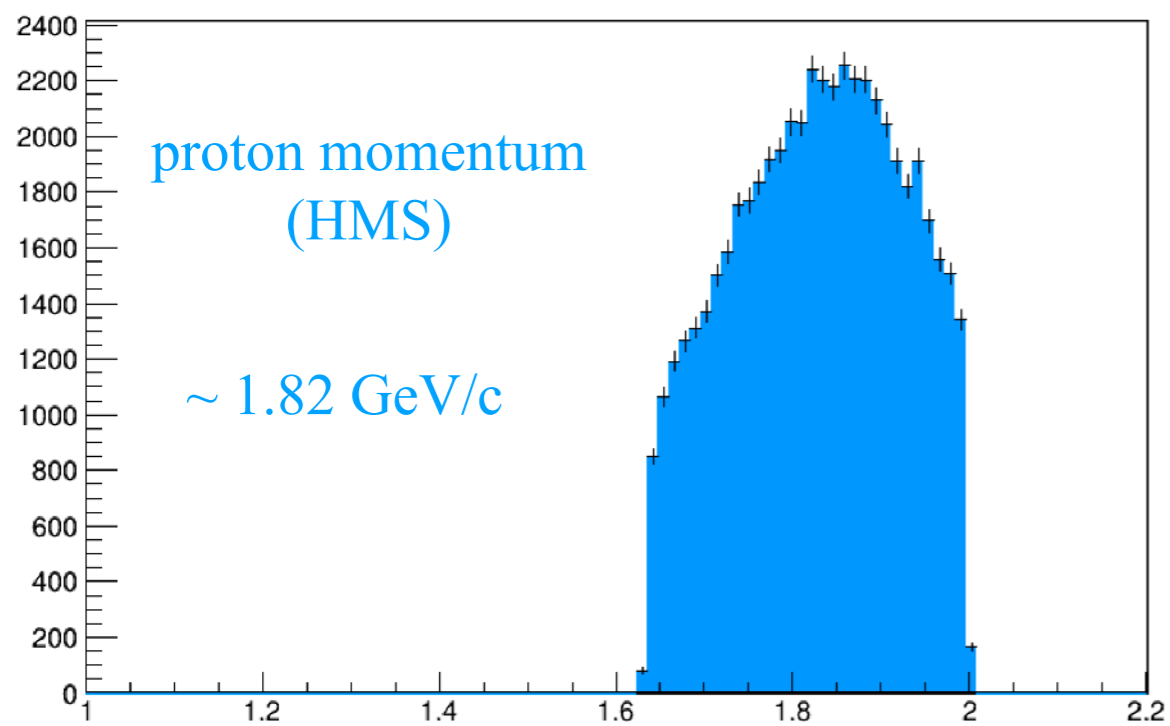
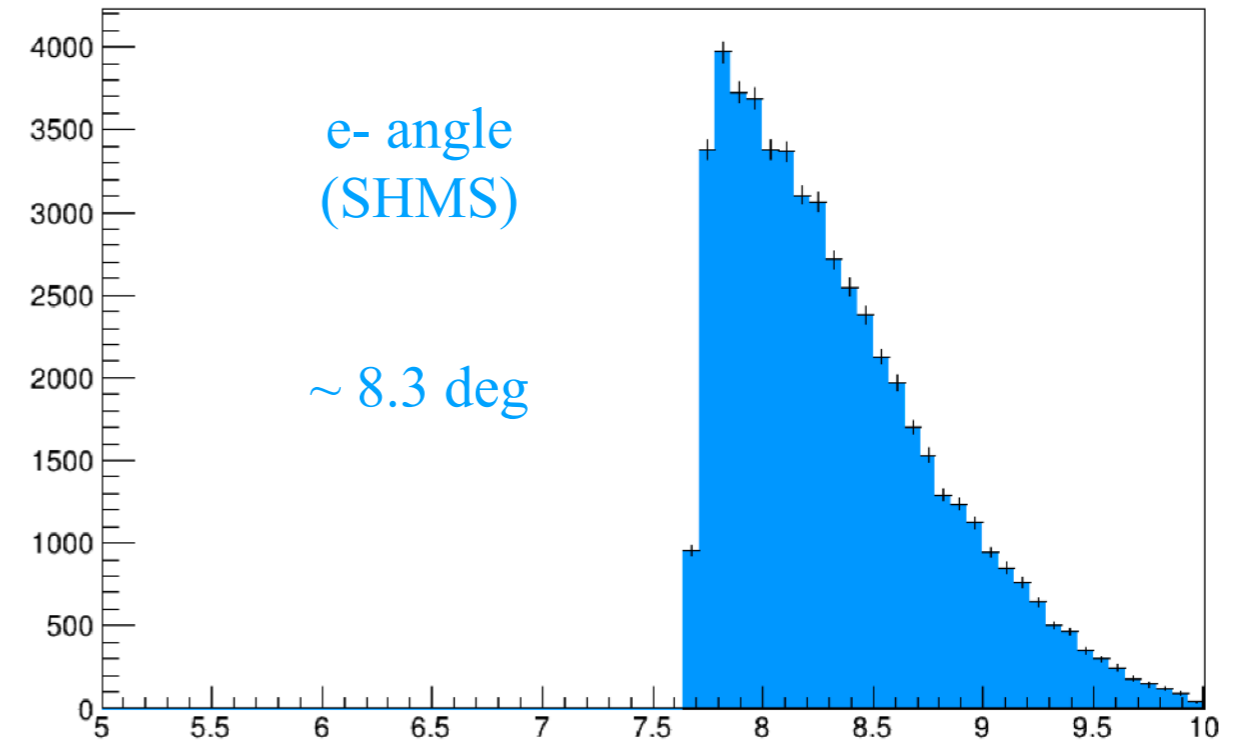
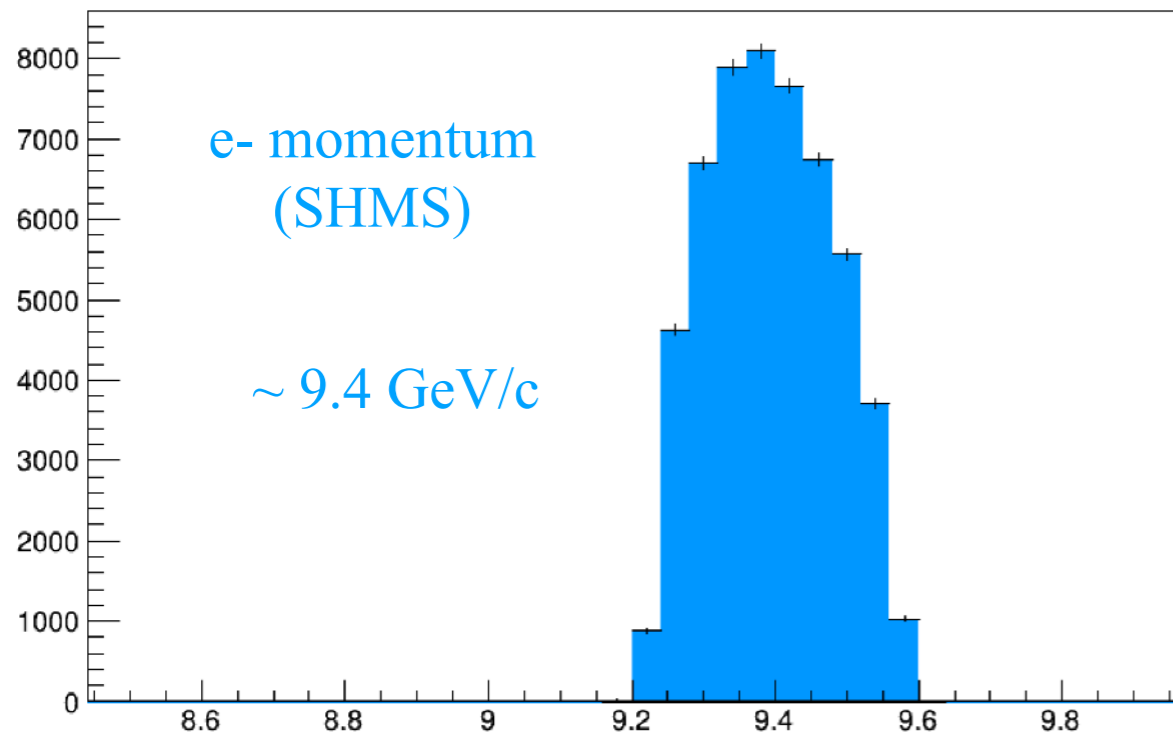
- $Q^2 > 1.8 \text{ GeV}^2$
- $P_{\text{miss}} < 0.270 \text{ GeV/c}$
- $-0.02 < E_{\text{miss}} < 0.09 \text{ (GeV)}$

## SRC Kinematics

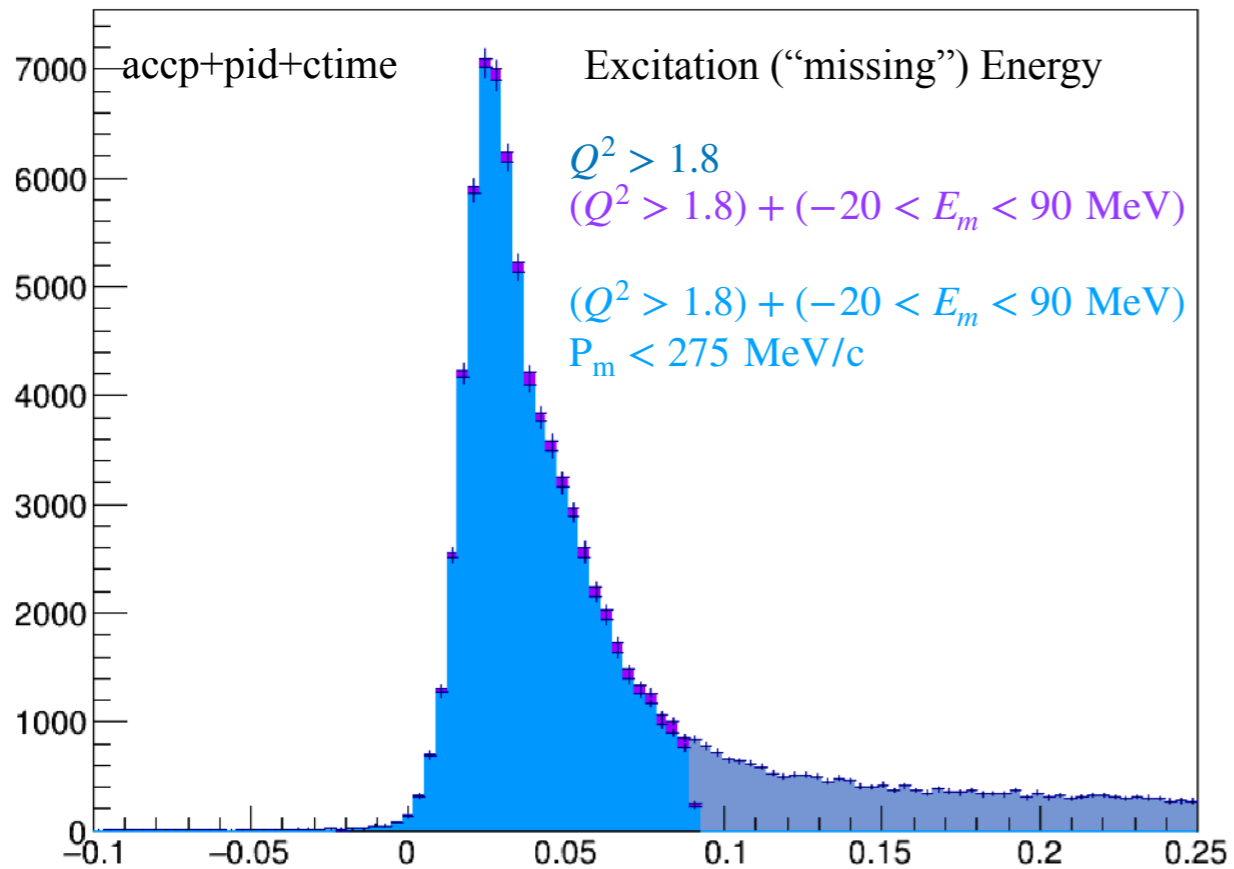
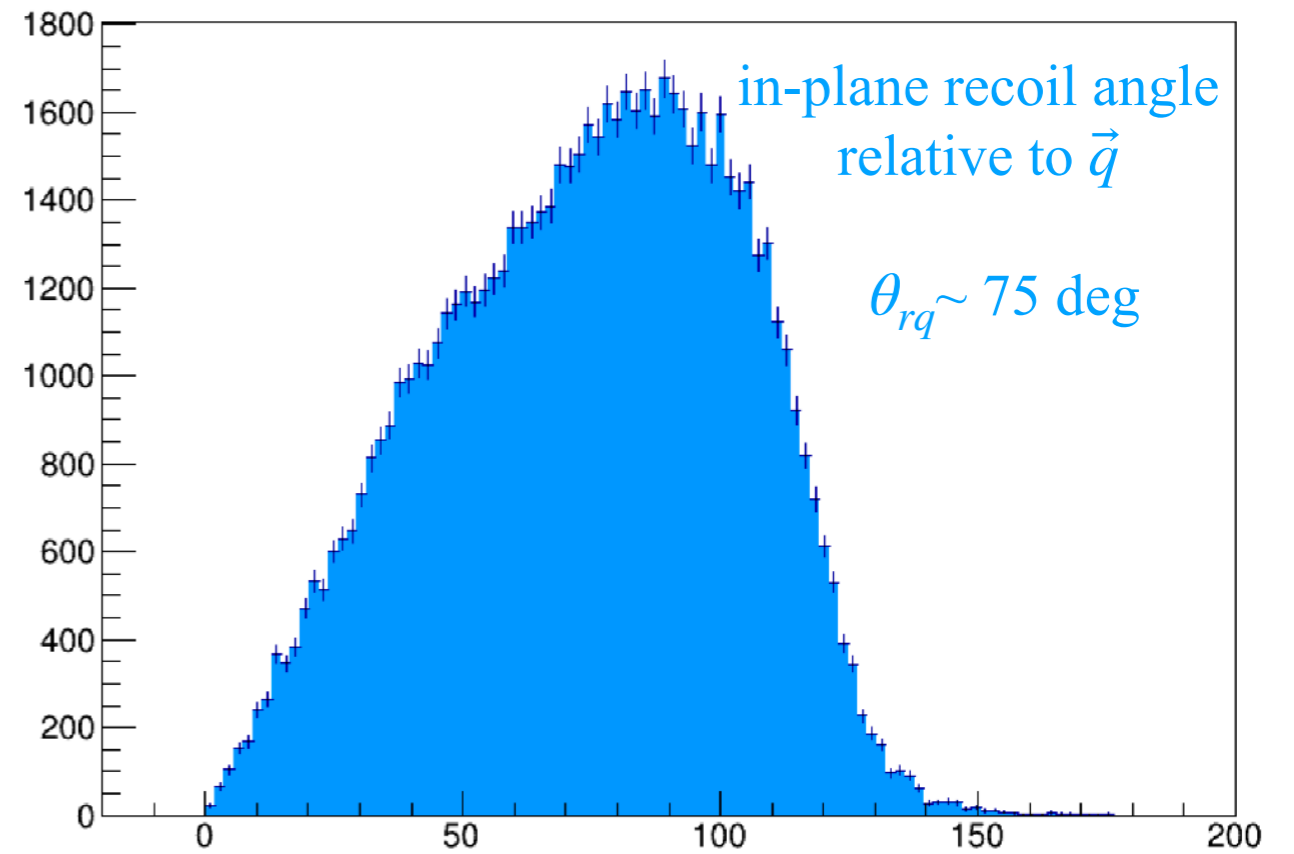
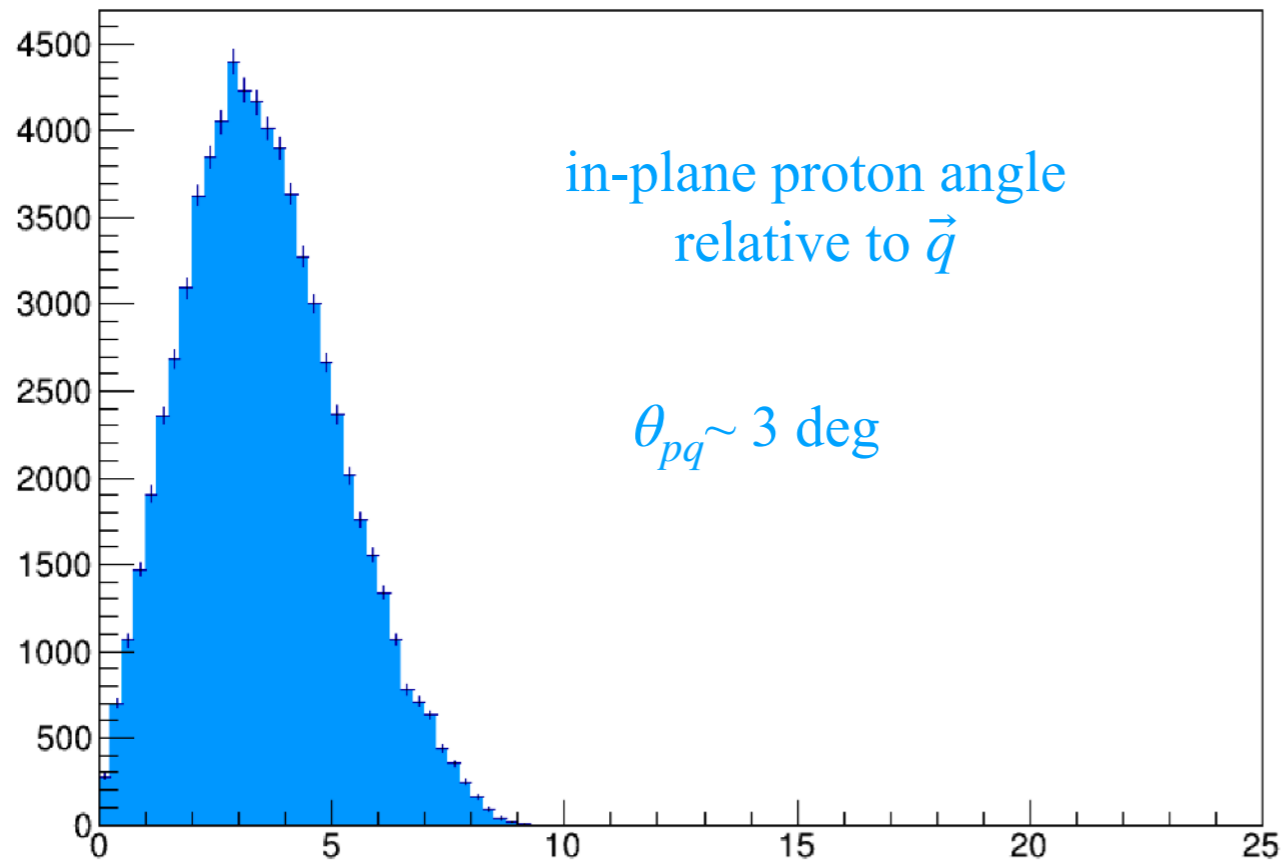
- $Q^2 > 1.8 \text{ GeV}^2$
- $x_B > 1.2$
- $\theta_{rq} < 40^\circ$
- $0.375 < p_{\text{miss}} < 0.7 \text{ GeV/c}$



# Kinematics ( C12 MF )

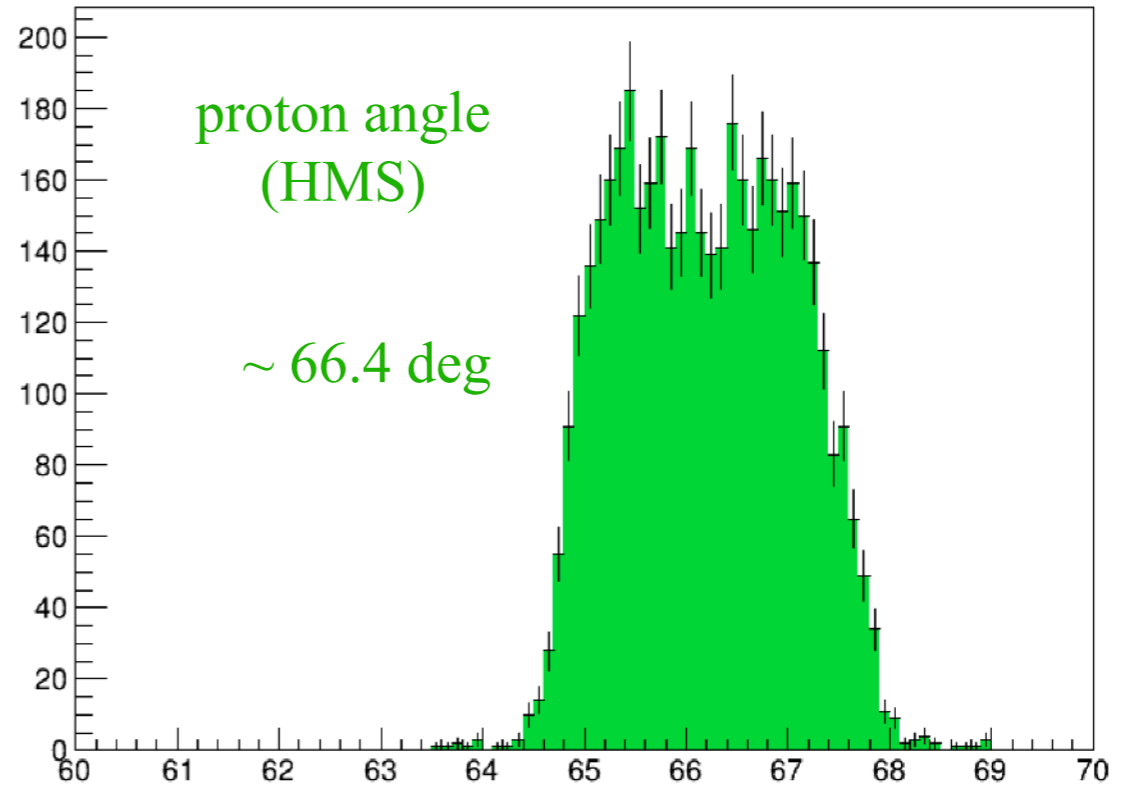
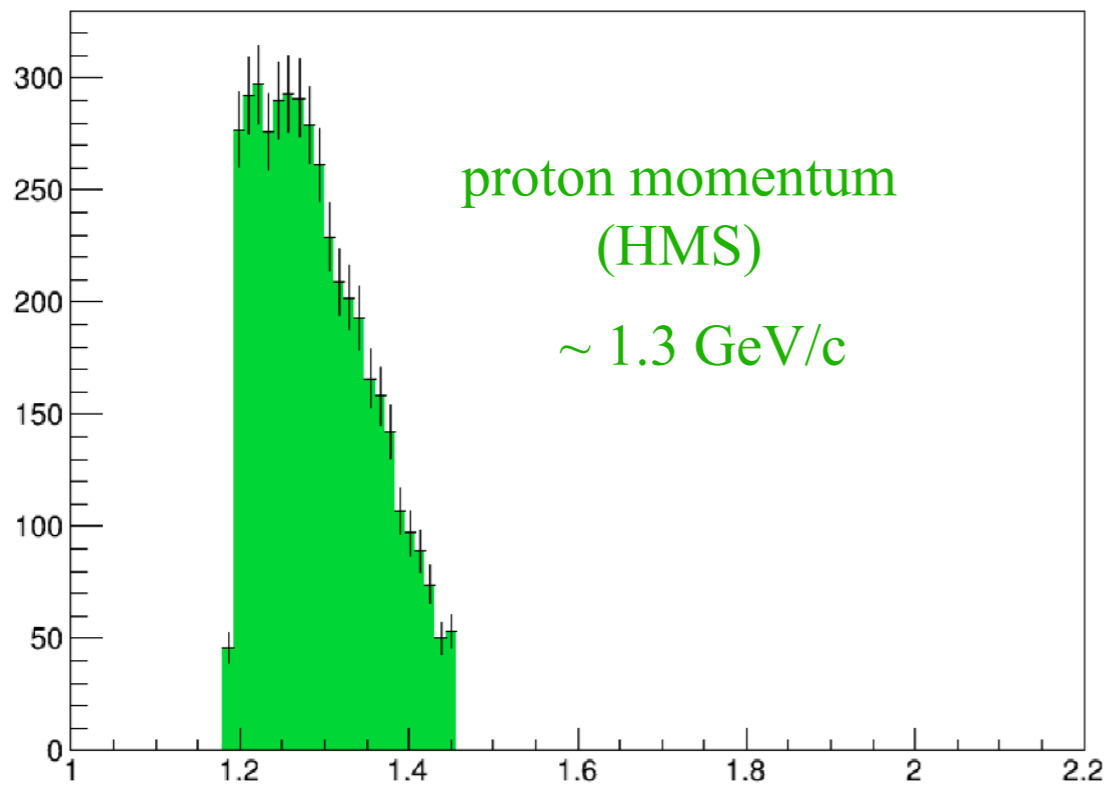
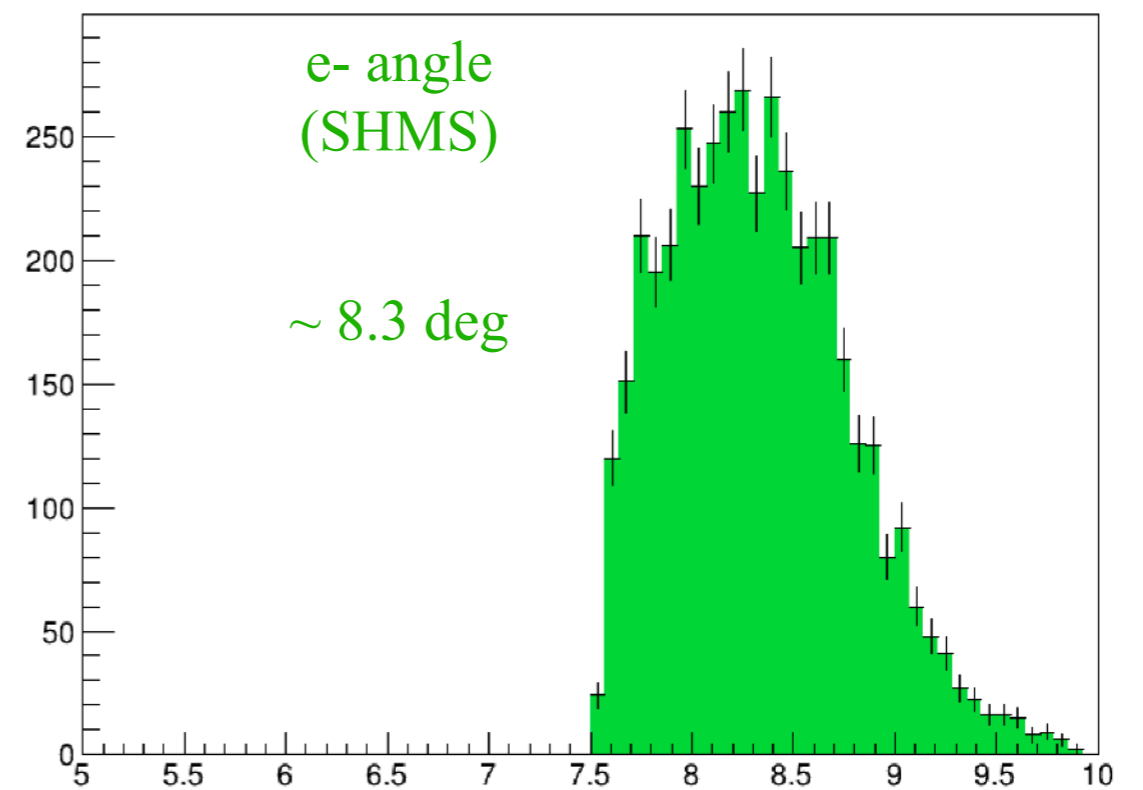
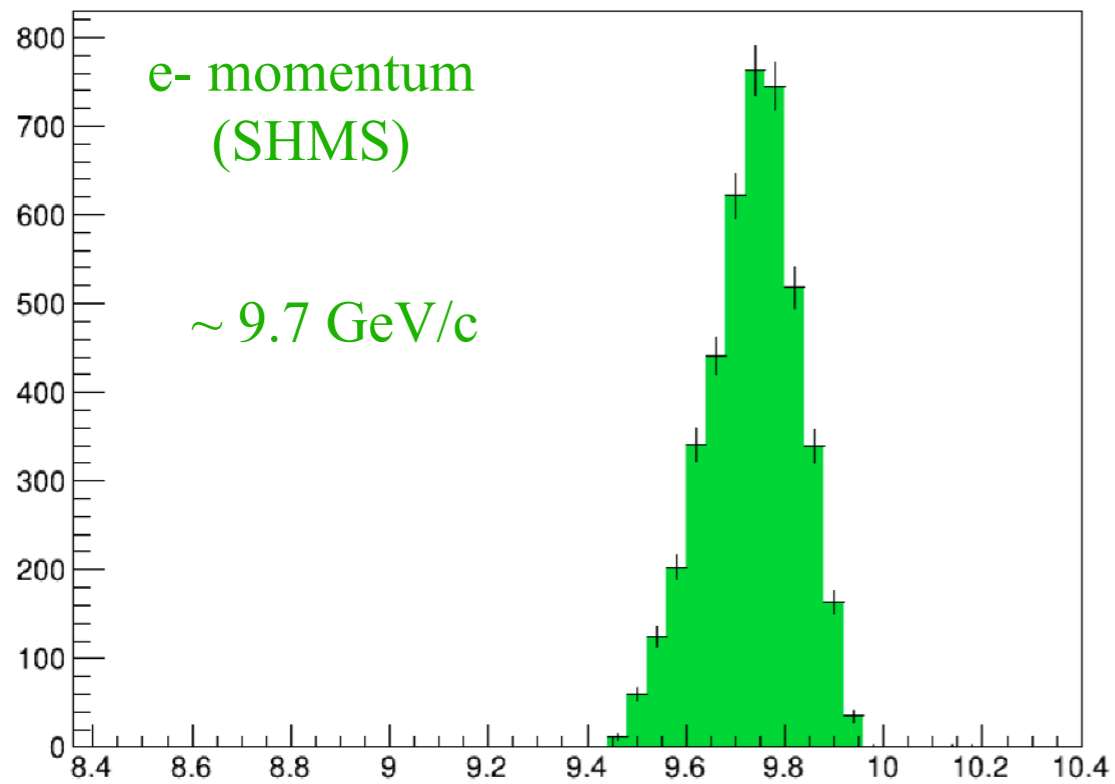


# Kinematics ( C12 MF )

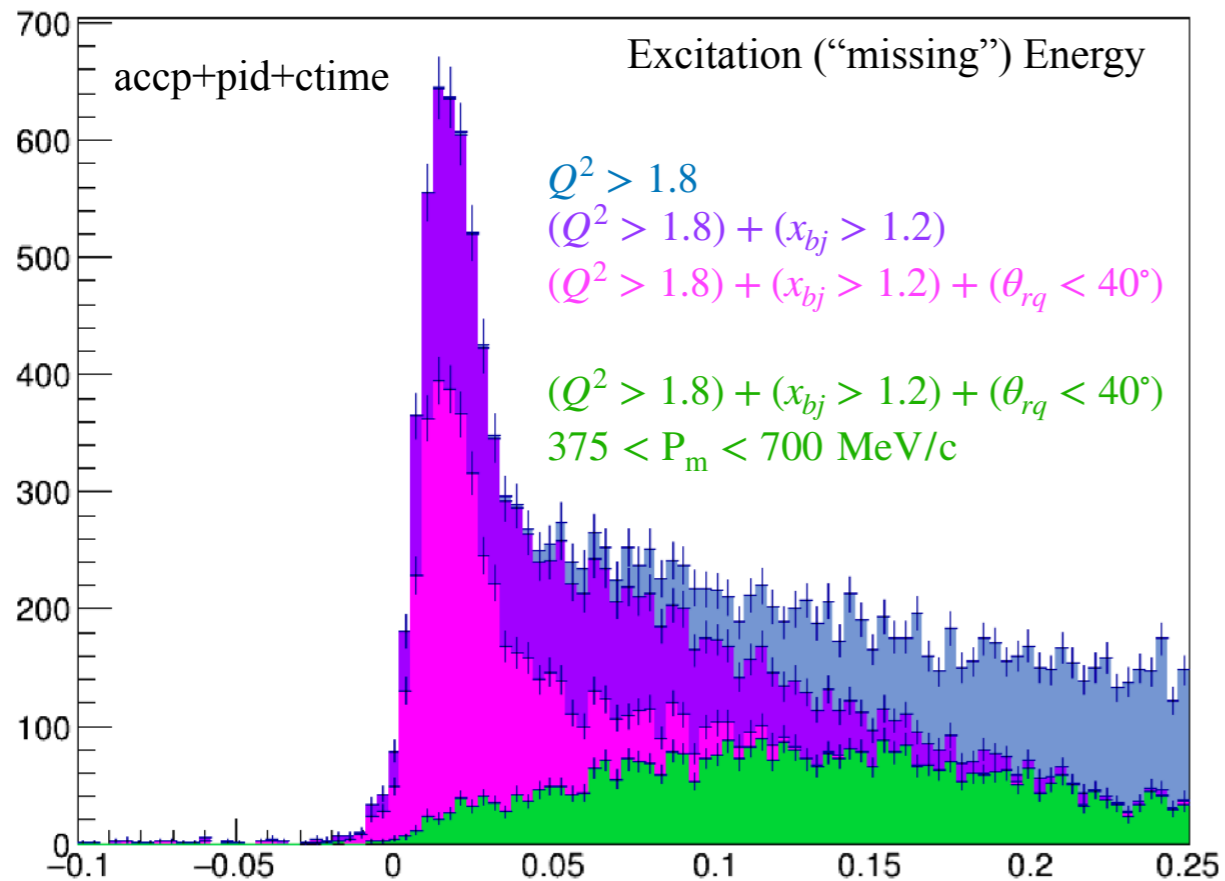
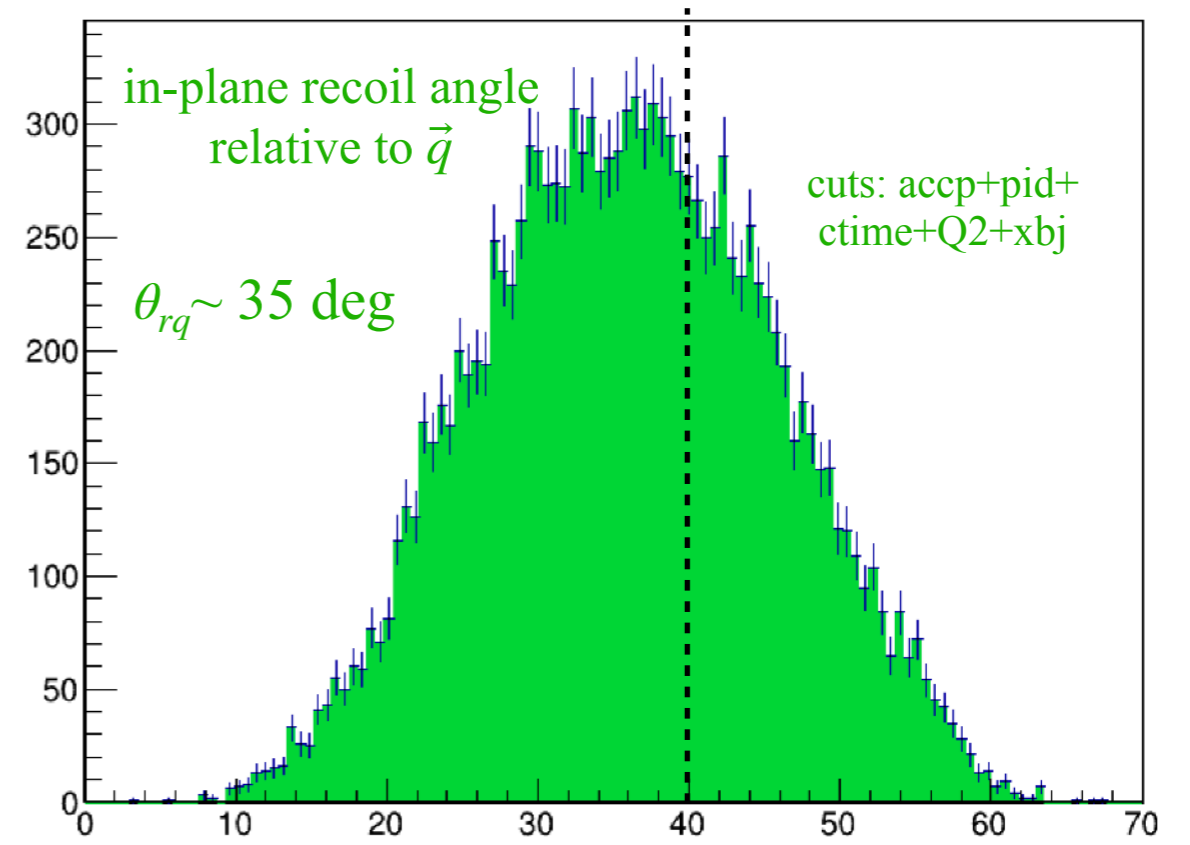
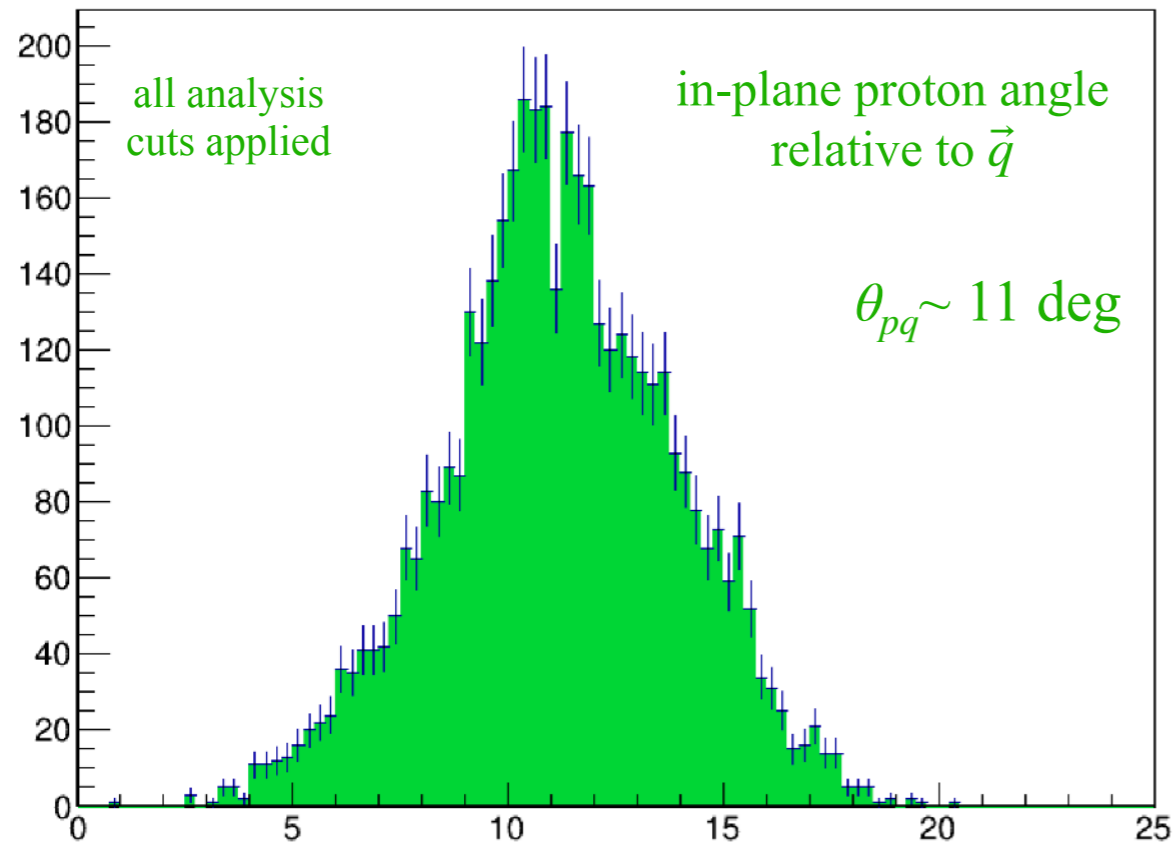


$$E_{\text{miss}} = \nu - T_p - T_{\text{rec}}$$

# Kinematics ( C12 SRC )

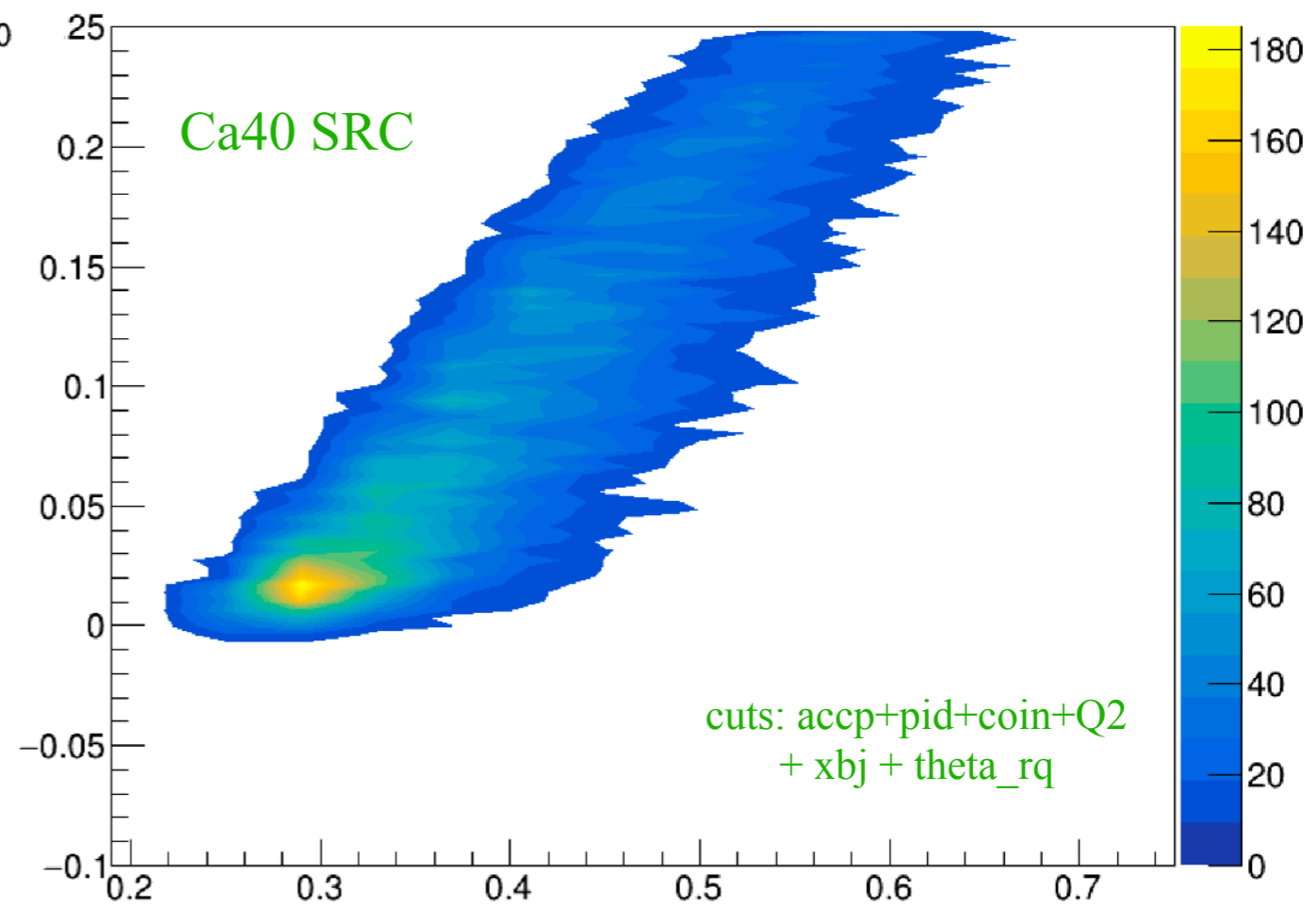
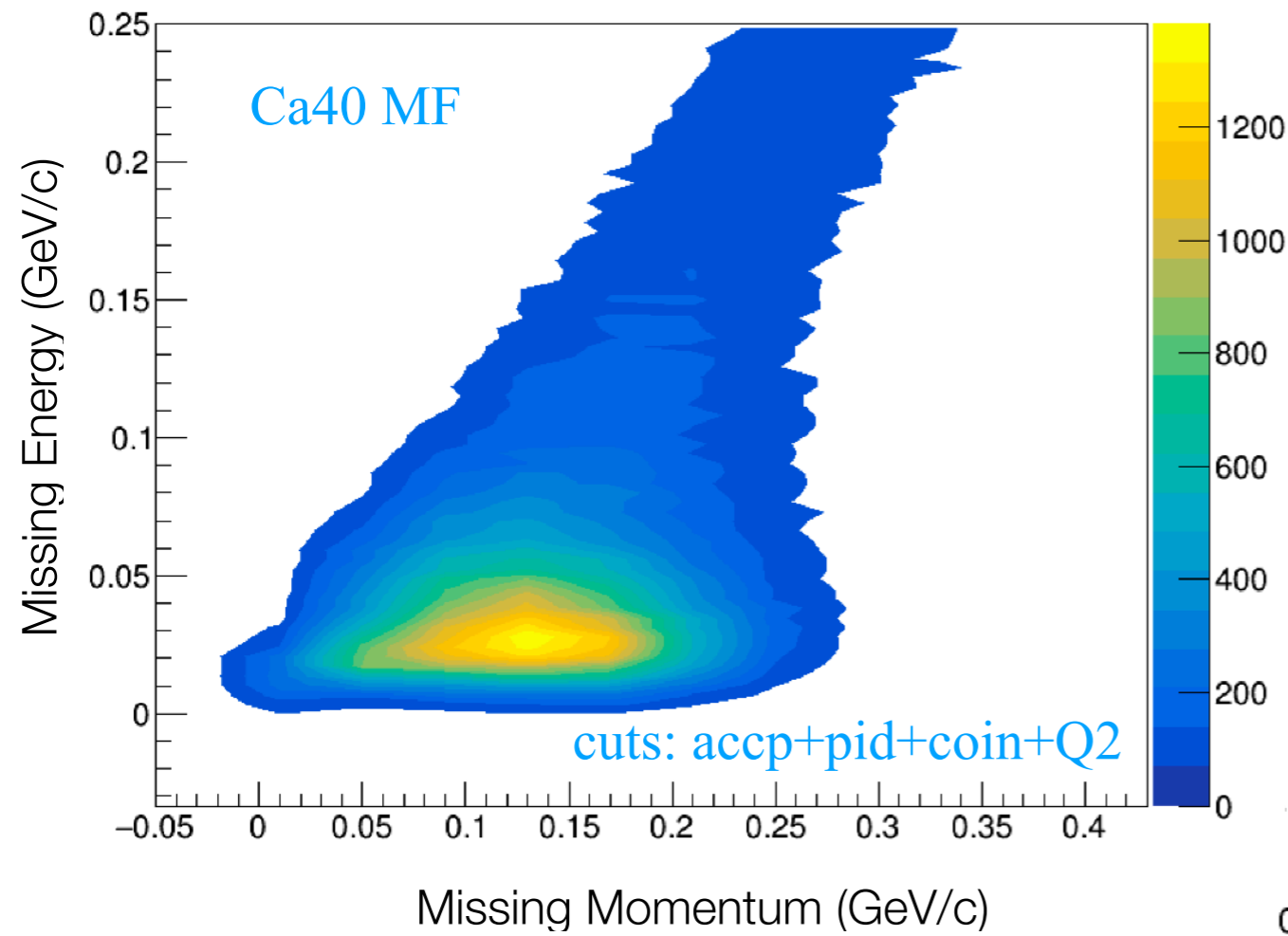


# Kinematics ( C12 SRC )



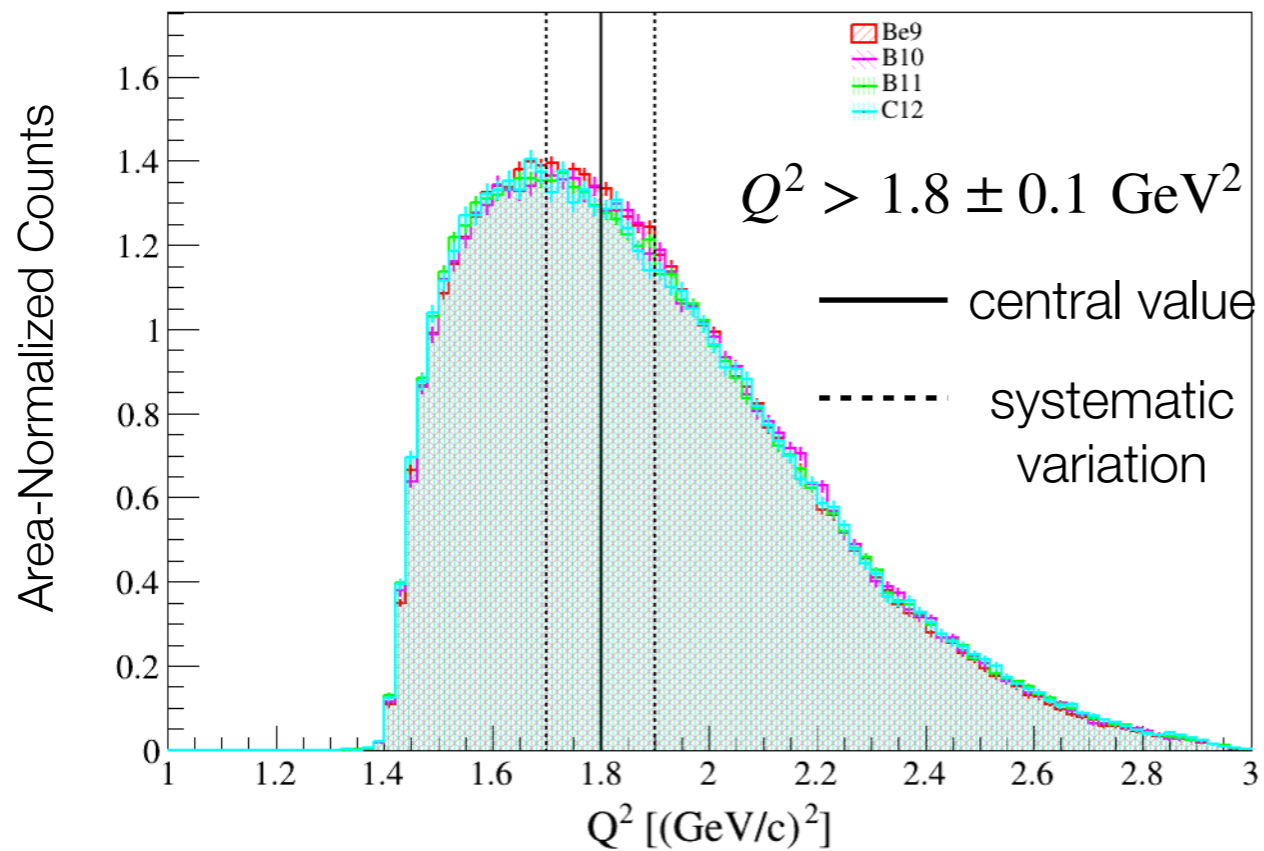
$$E_{\text{miss}} = \nu - T_p - T_{\text{rec}}$$

# Missing Energy vs. Missing Momentum



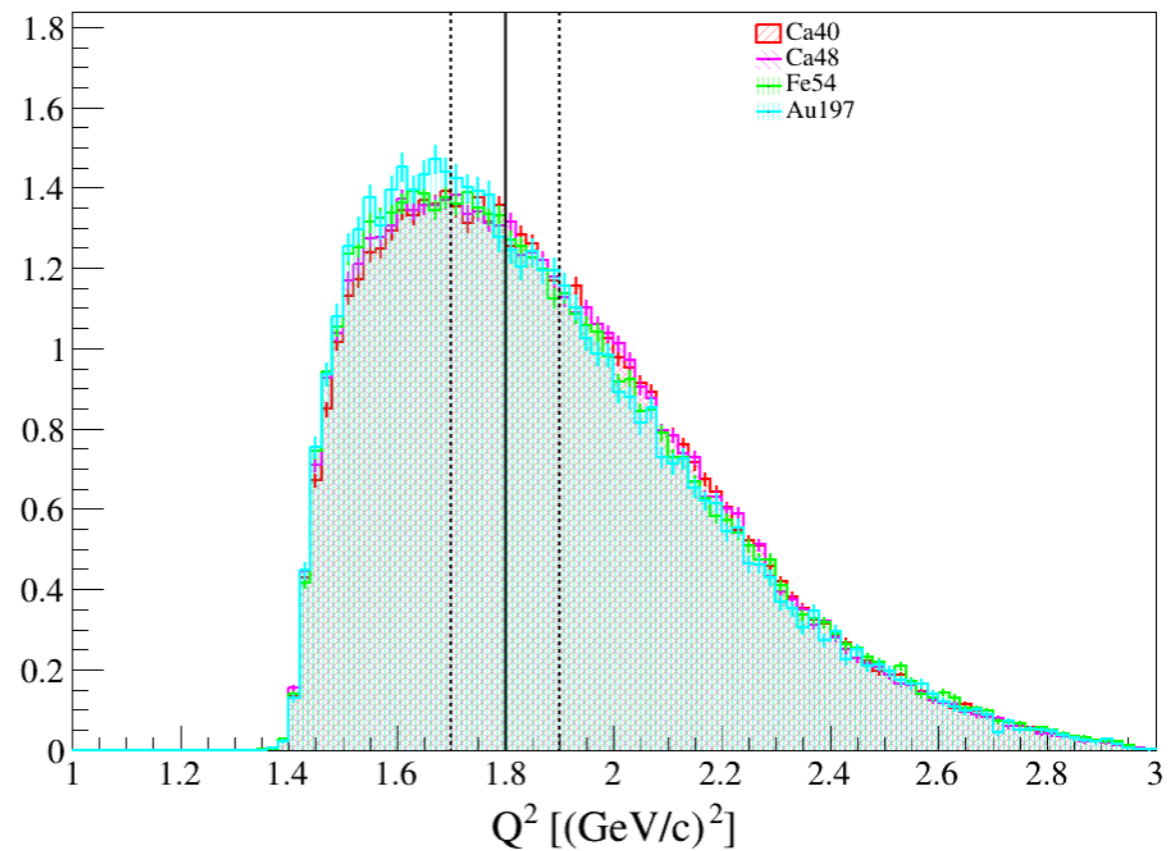
# Data Analysis Cuts

Light MF 4-Momentum Transfer

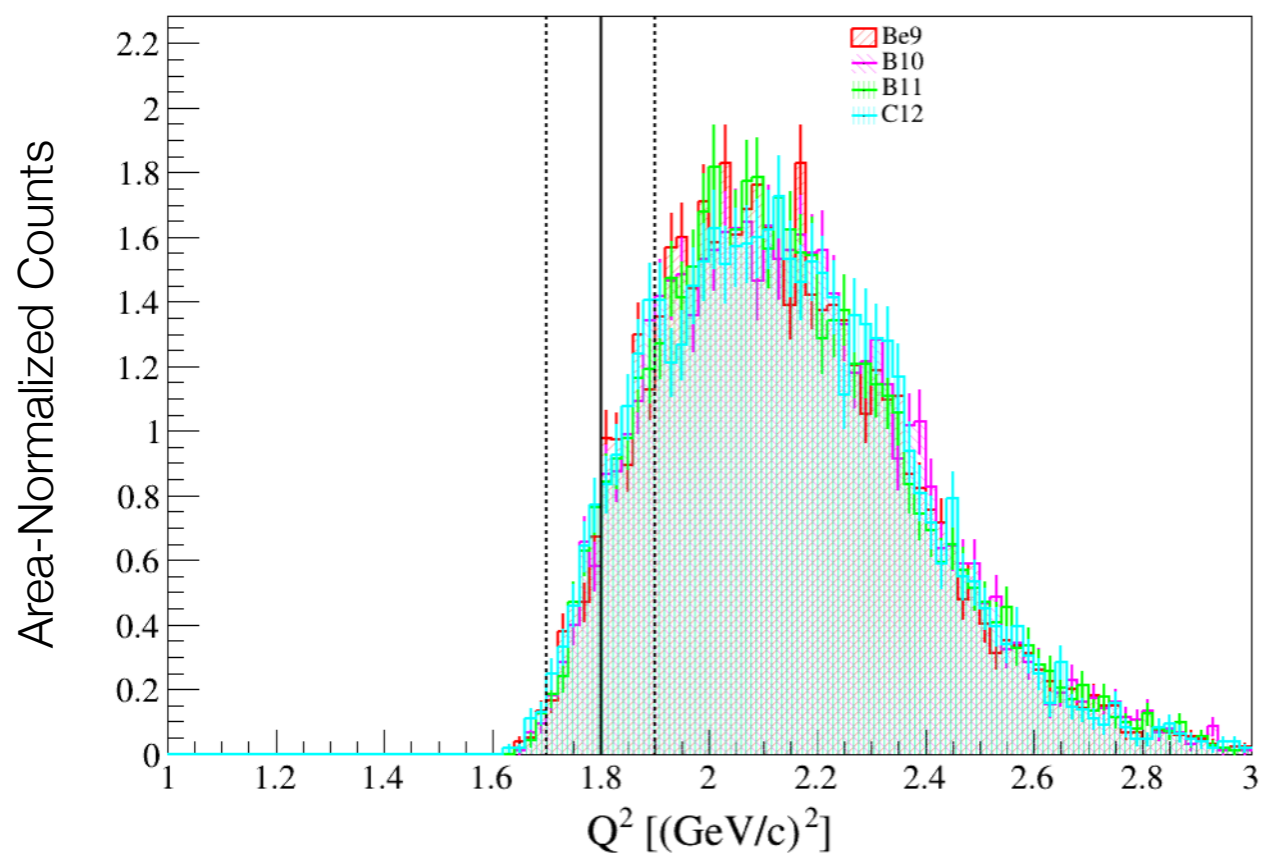


MF

Heavy MF 4-Momentum Transfer

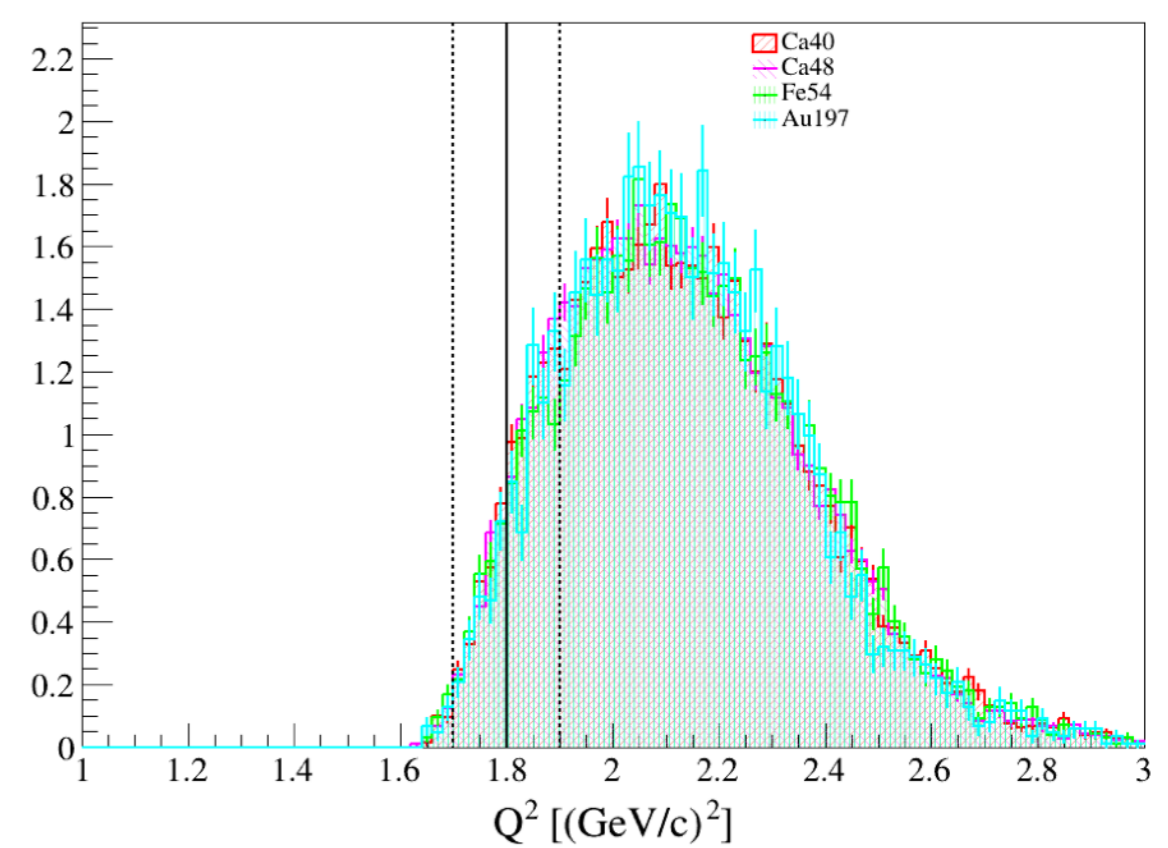


Light SRC 4-Momentum Transfer



SRC

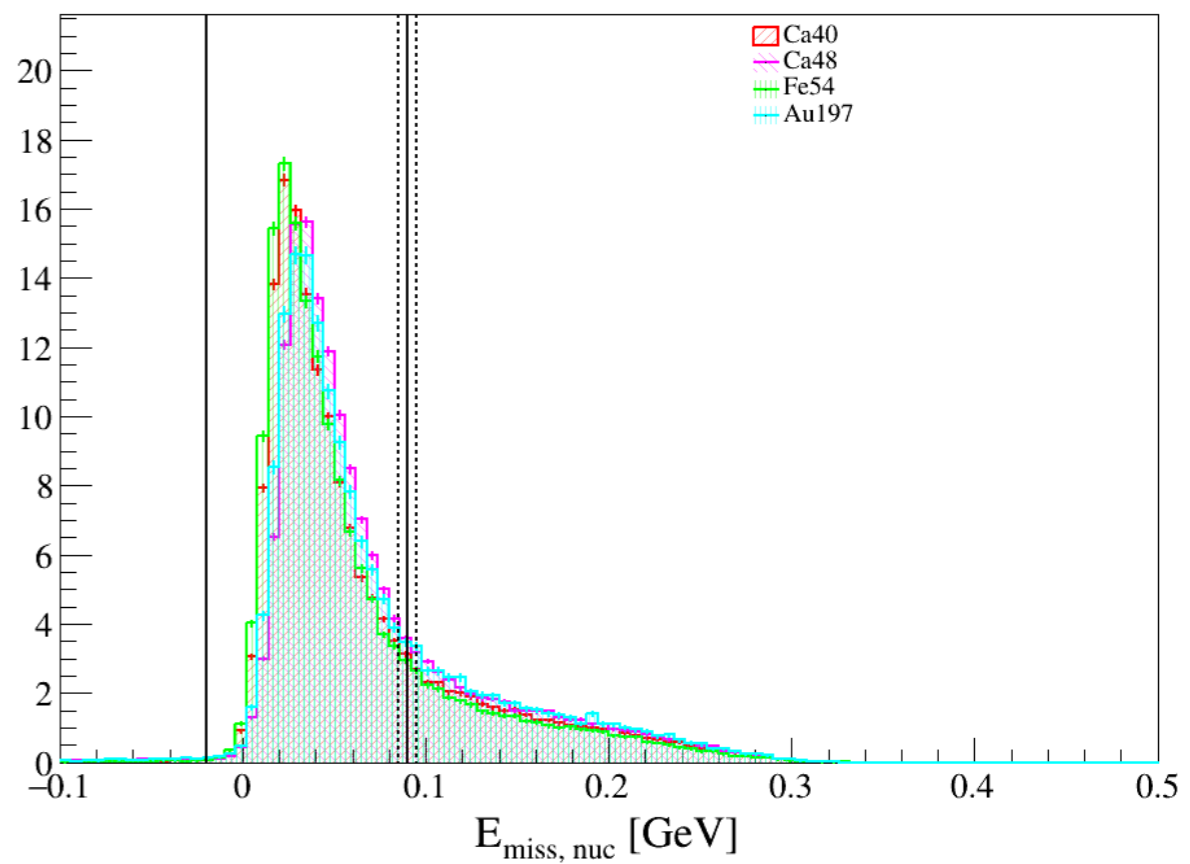
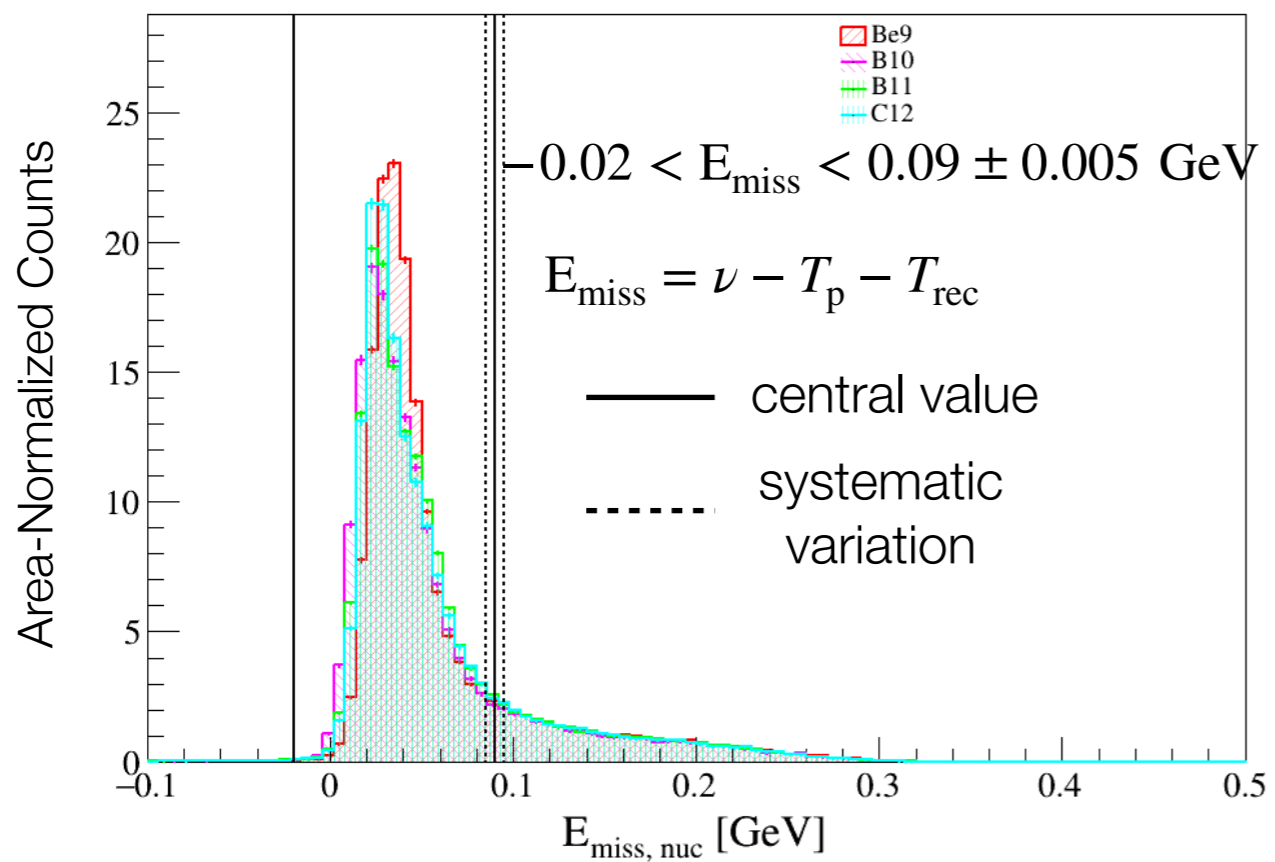
Heavy SRC 4-Momentum Transfer



Light MF Missing Energy (Nuclear Physics)

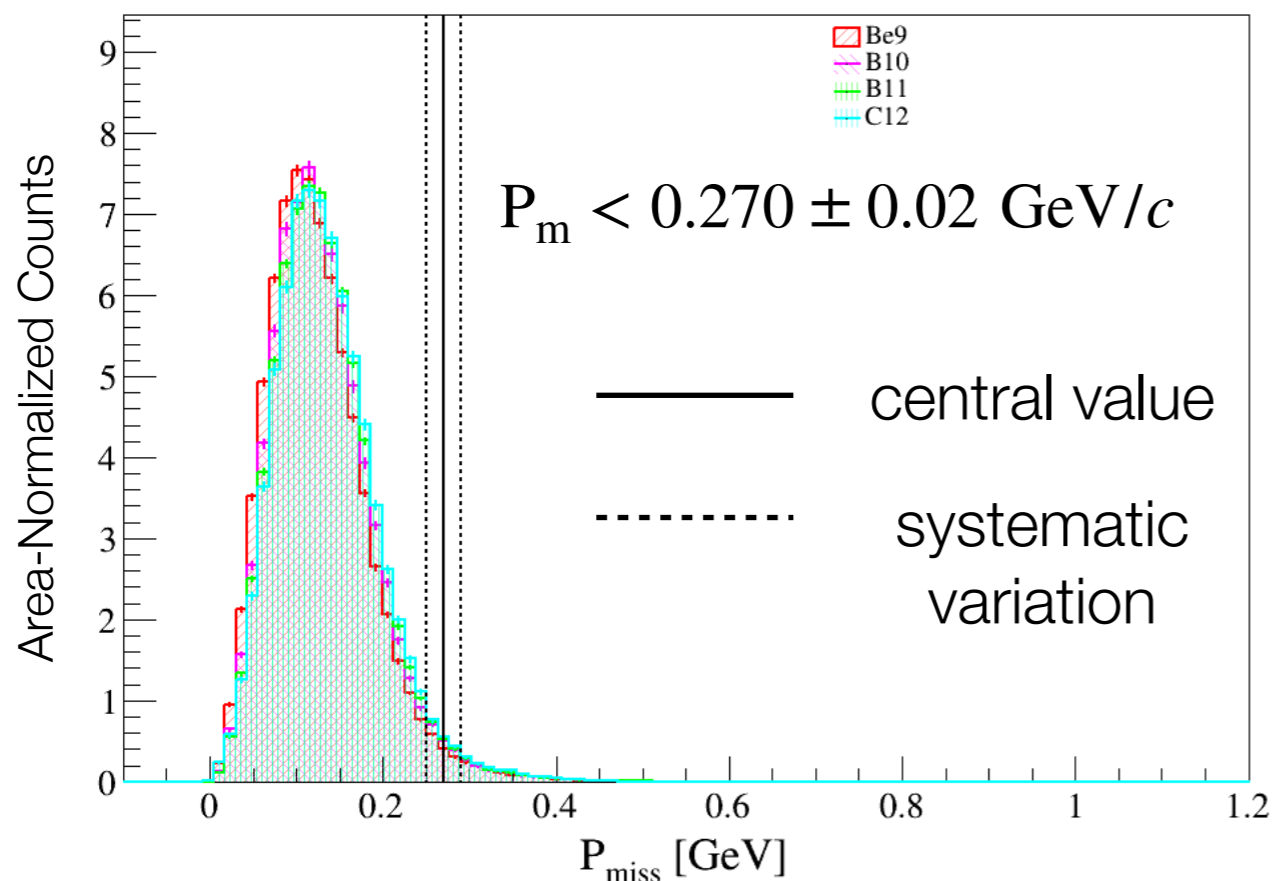
MF

Heavy MF Missing Energy (Nuclear Physics)



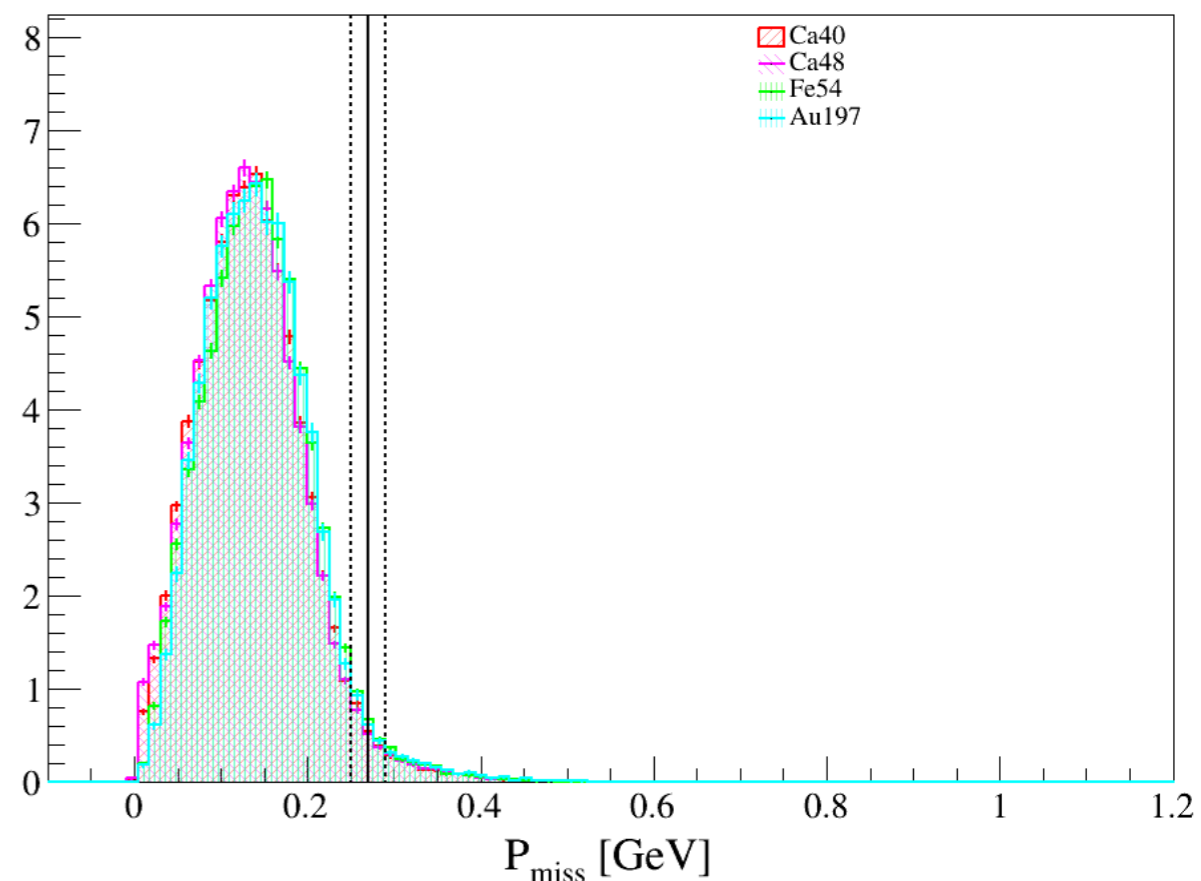


Light MF Missing Momentum

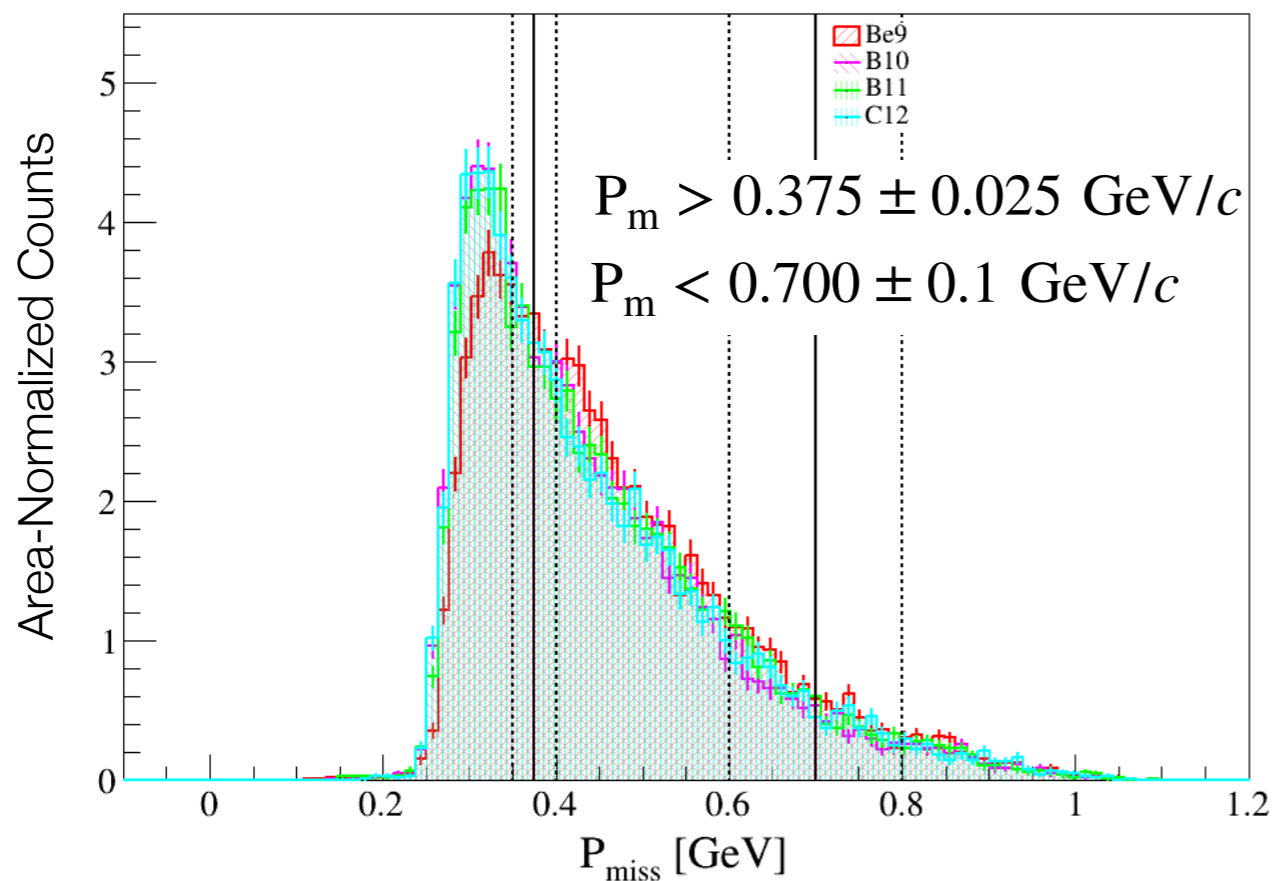


Heavy MF Missing Momentum

MF

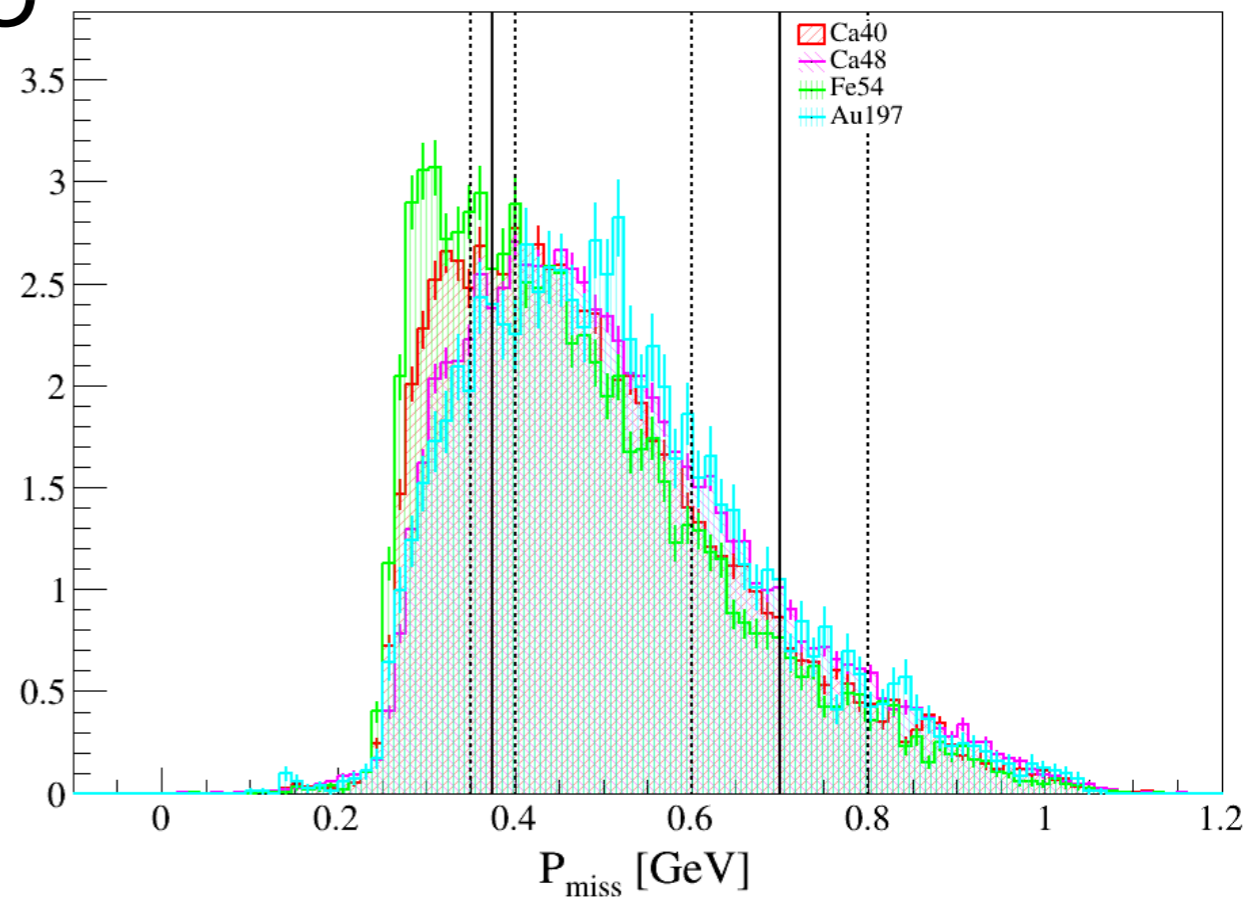


Light SRC Missing Momentum



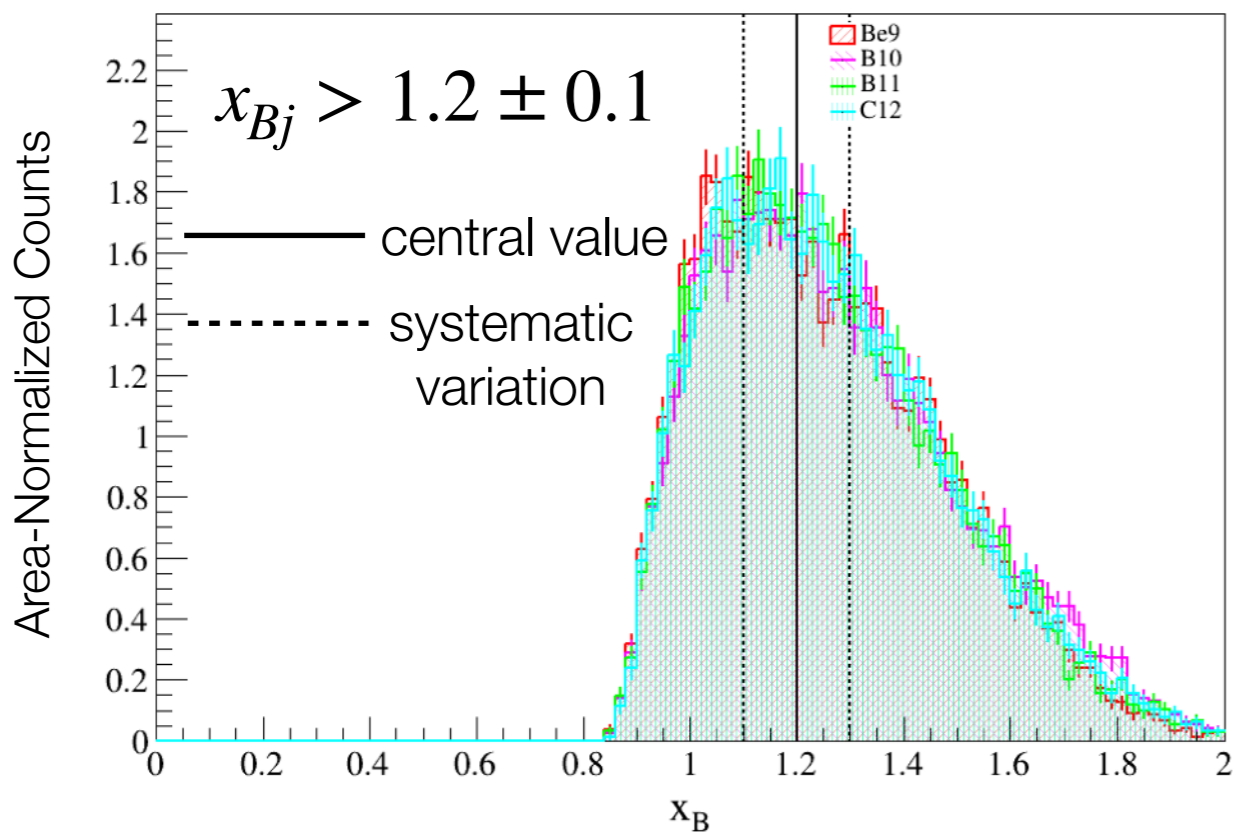
Heavy SRC Missing Momentum

SRC

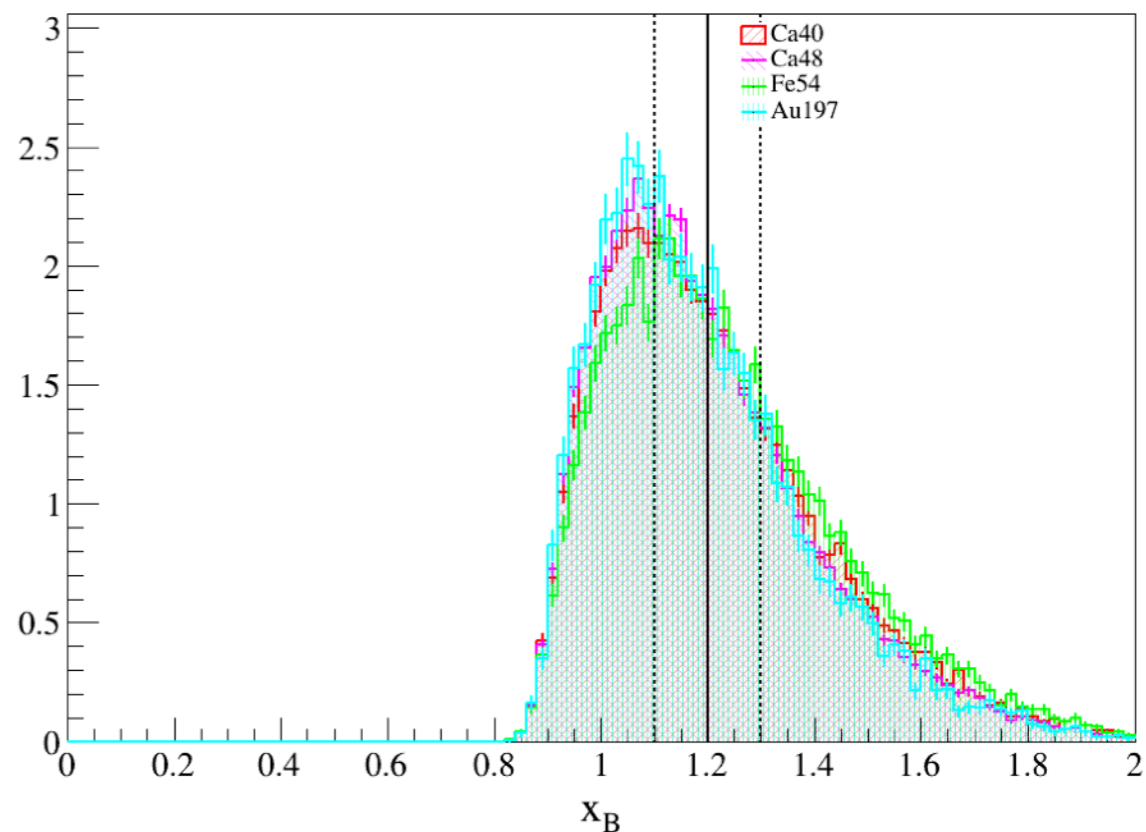


# SRC

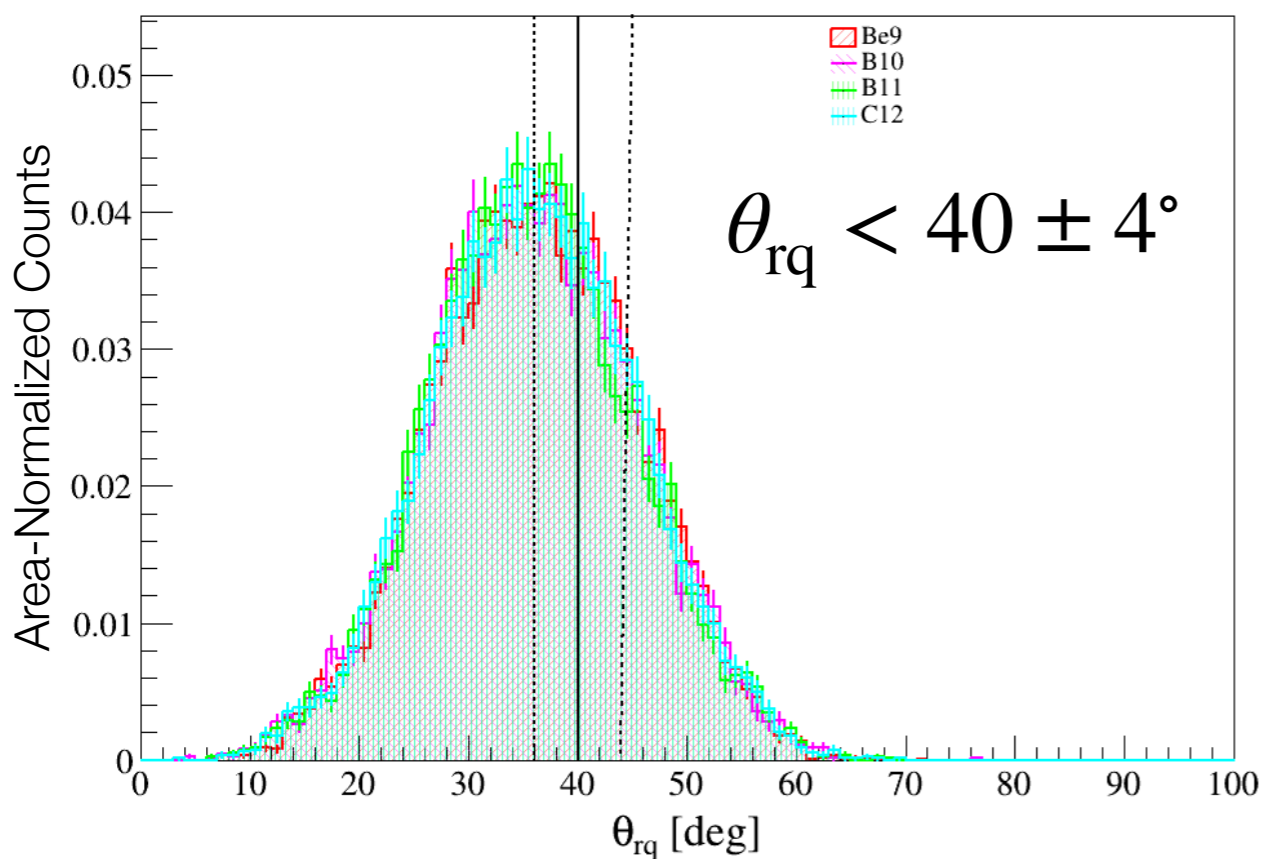
### Light SRC x-Bjorken



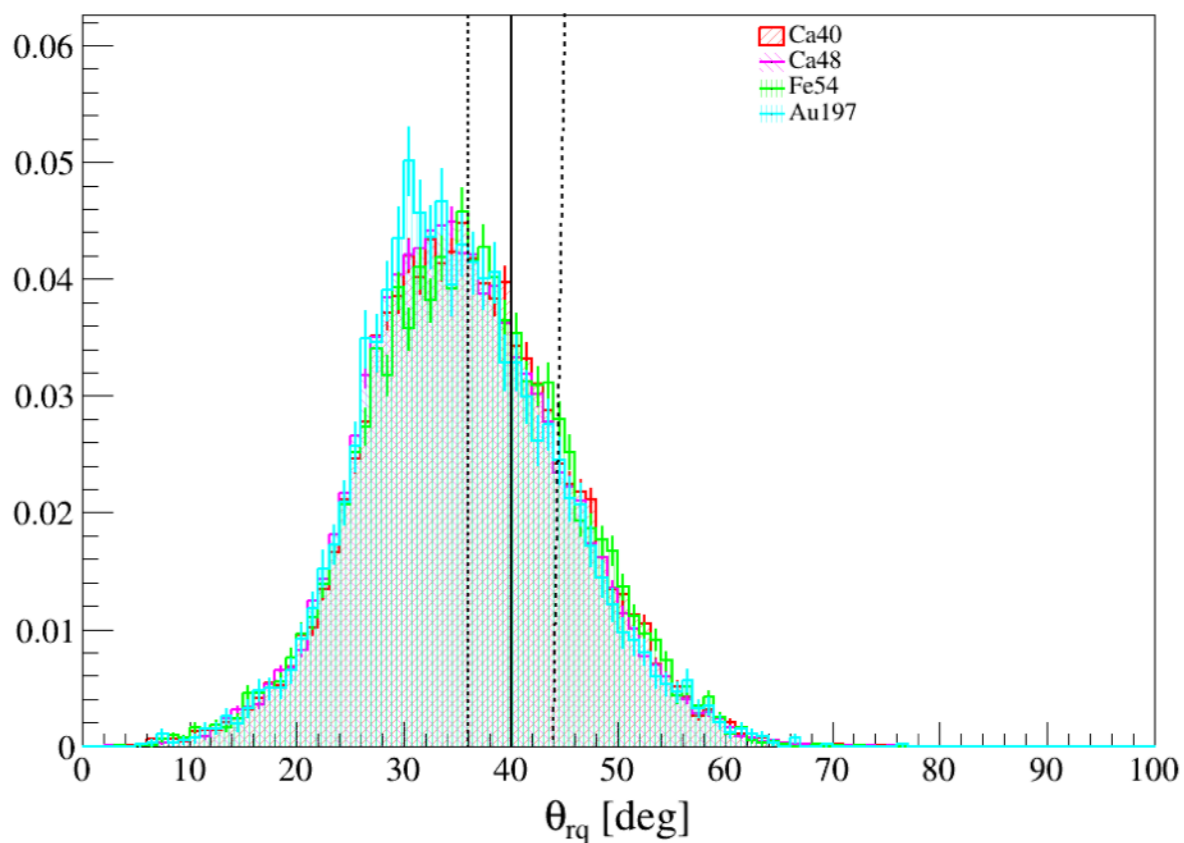
### Heavy SRC x-Bjorken



### Light SRC In-Plane (recoil) Angle



### Heavy SRC In-Plane (recoil) Angle



# Single Ratios to C12 (per proton)

$$R_{MF} = \frac{Y_A}{Y_{C12}} \Big|_{MF} \quad R_{SRC} = \frac{Y_A}{Y_{C12}} \Big|_{SRC}$$

$$Y_A : \frac{N}{Q \cdot \epsilon_i \cdot T_N \cdot \sigma_t \cdot Z/A}$$

$Y_A$  : nucleus A yield

$N$  : ( $e, e'p$ ) coincidence counts

$Q$  : total charge [mC]

$\epsilon_i$  : detector/DAQ efficiencies

$T_N$  : nuclear transparency

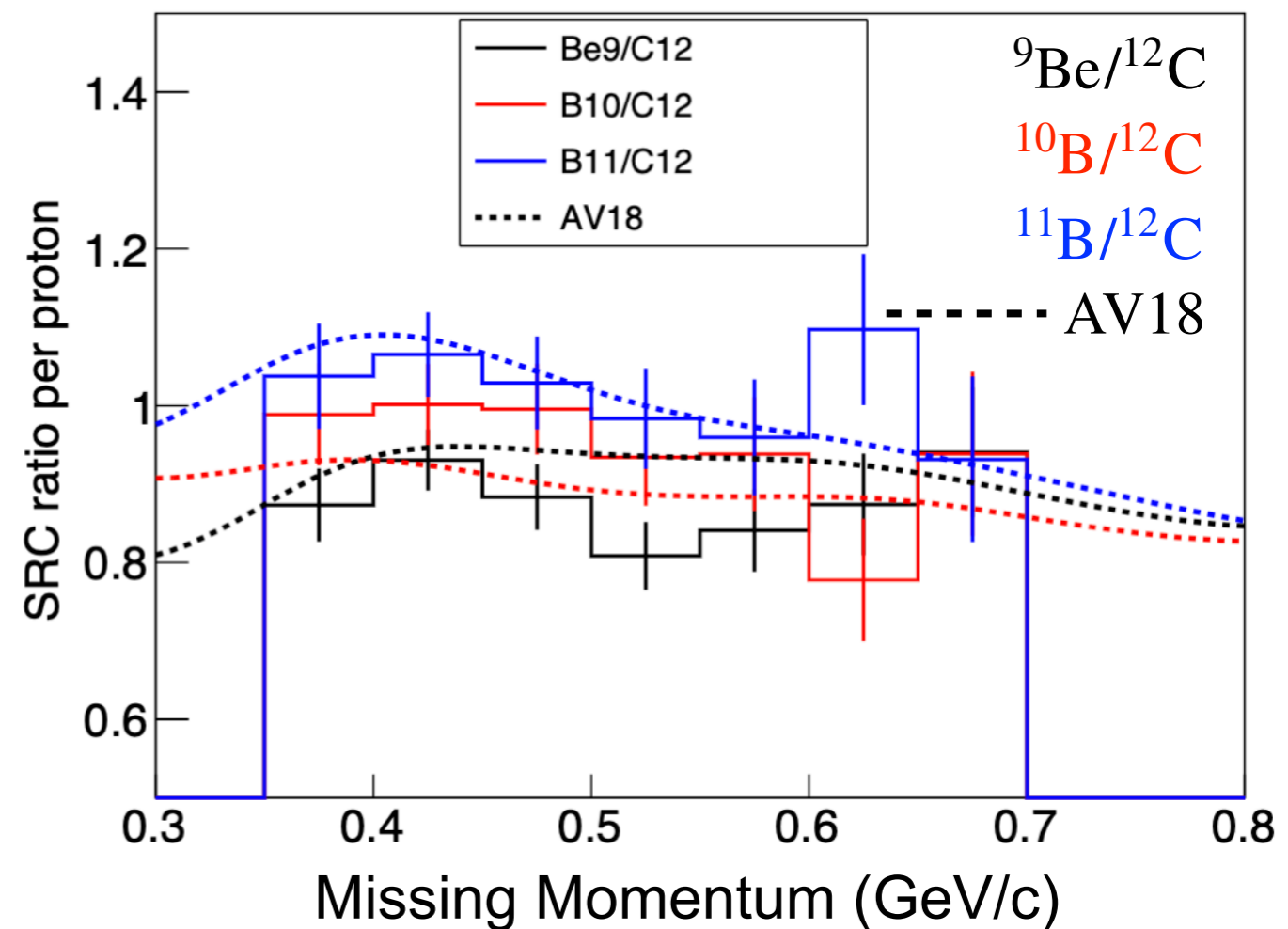
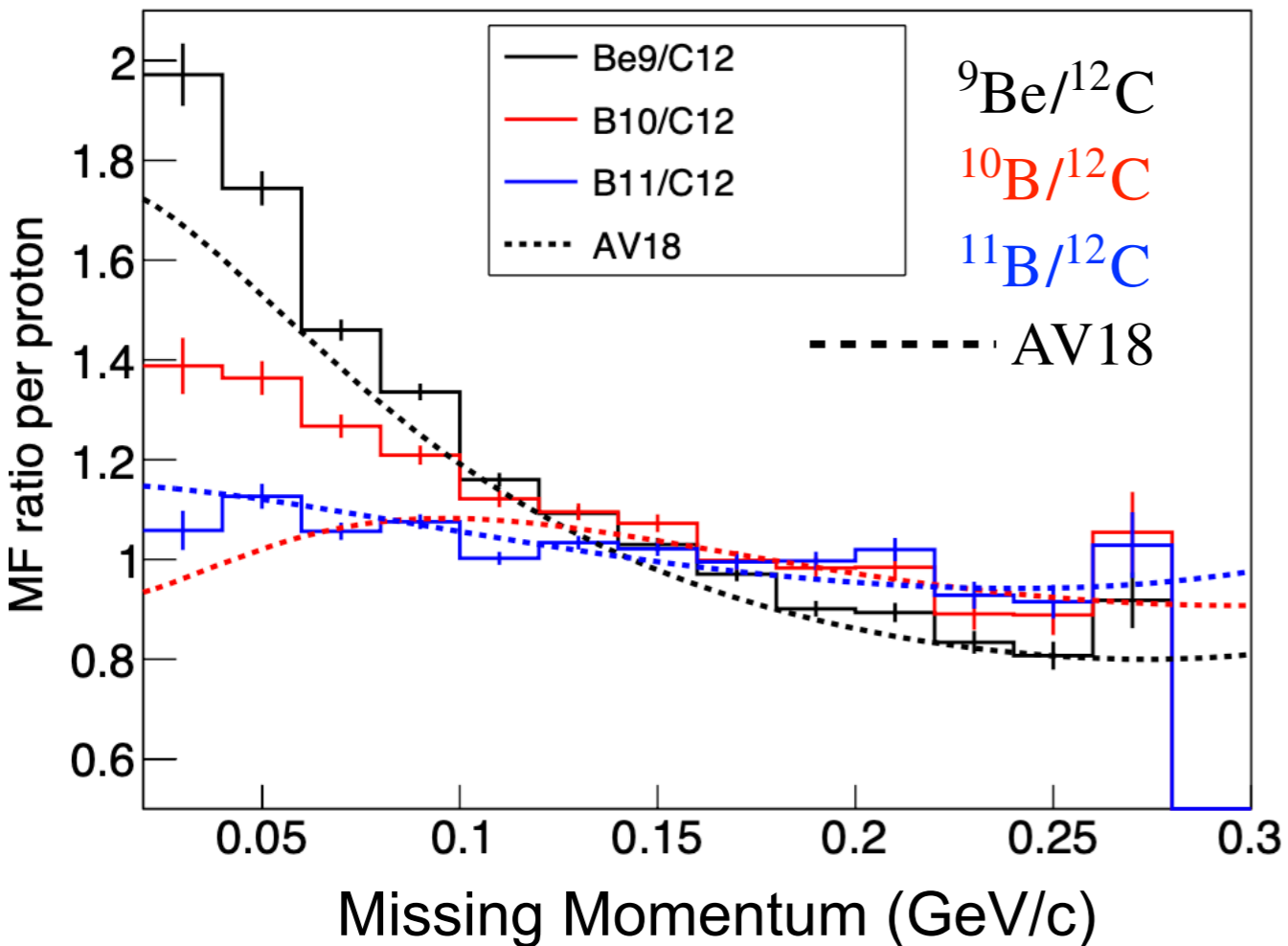
$\sigma_t$  : target thickness [g/cm<sup>2</sup>]

Radiative corrections were applied to ratios directly

Single Ratios to C12 (per proton)

Missing Momentum Distributions

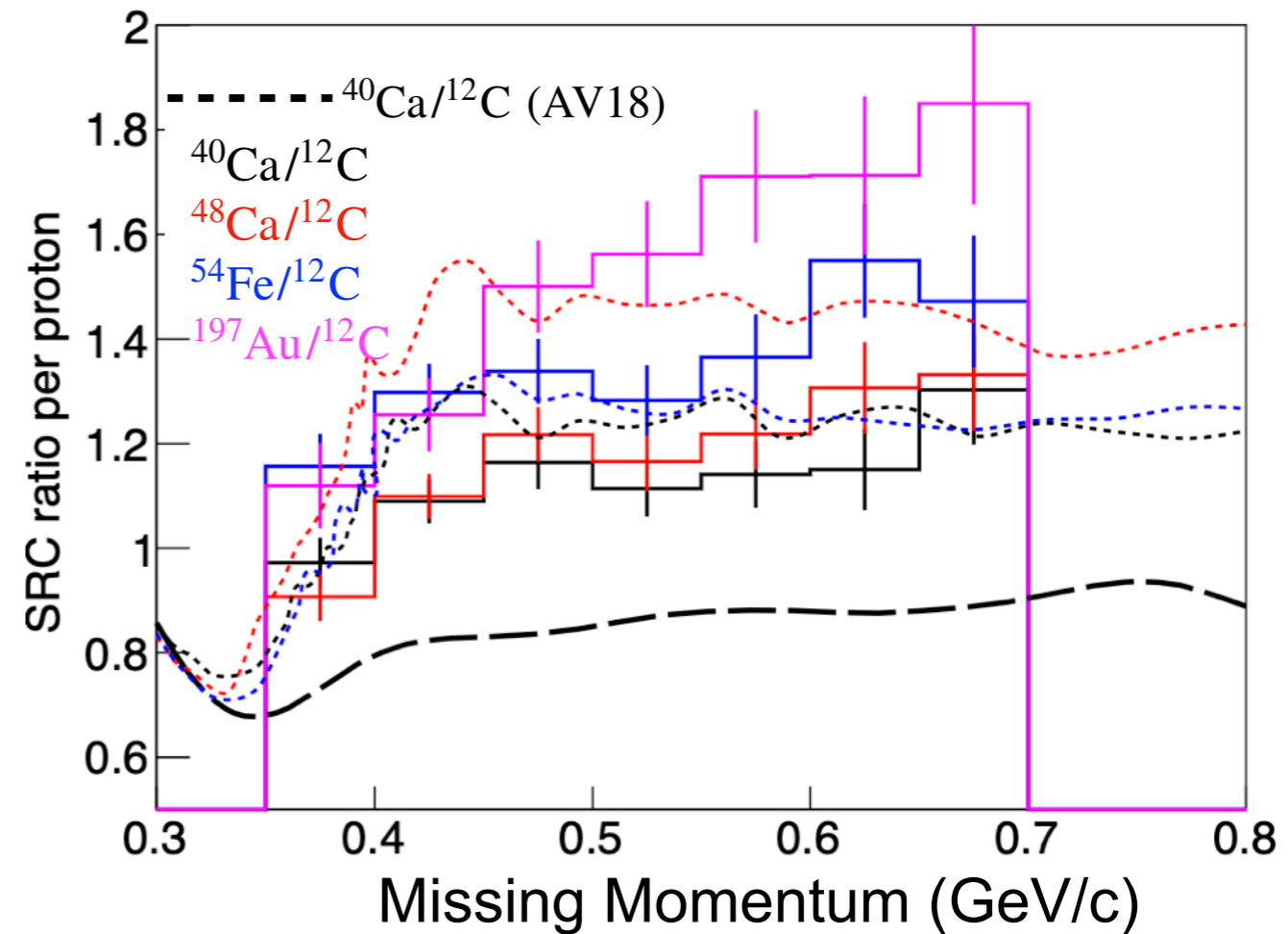
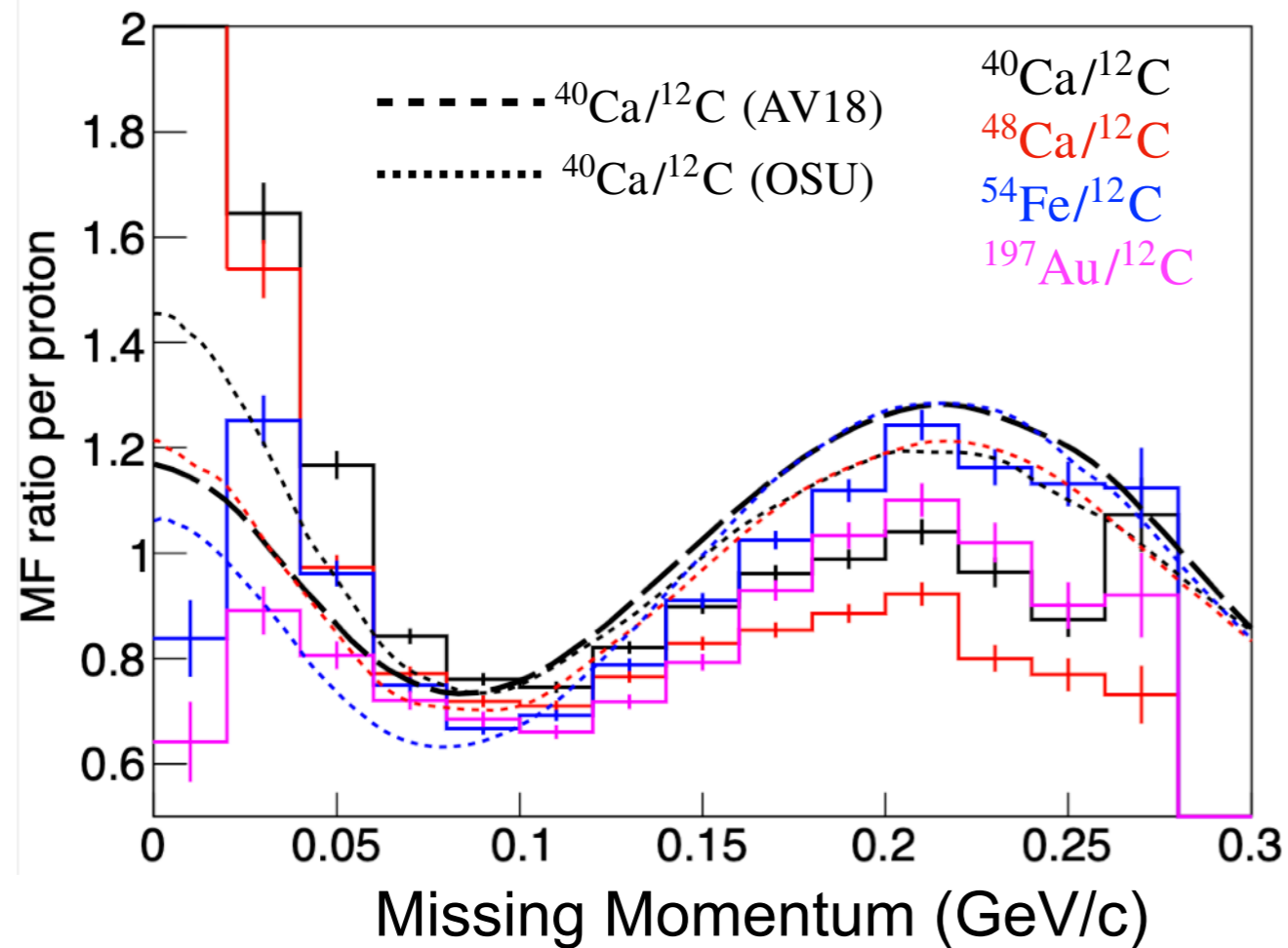
# Single Ratio to C12 (per proton): Light Nuclei



## Note:

- Radiative correction included
- ONLY statistical uncertainty
- data integrated over  $-20 < E_{\text{miss}} < 90$  MeV,  
calculations integrated over all  $E_{\text{miss}}$

# Single Ratio to C12 (per proton): Heavy Nuclei



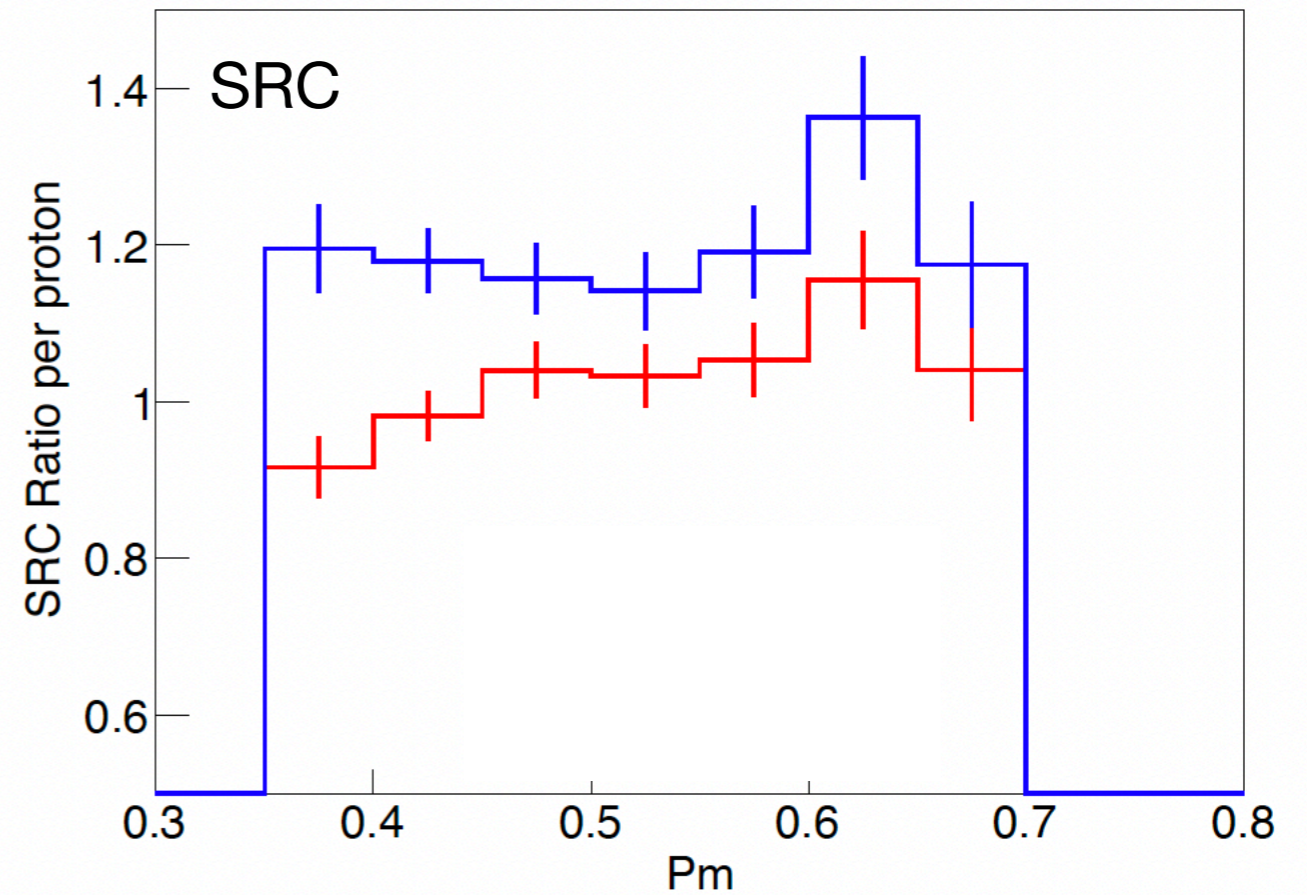
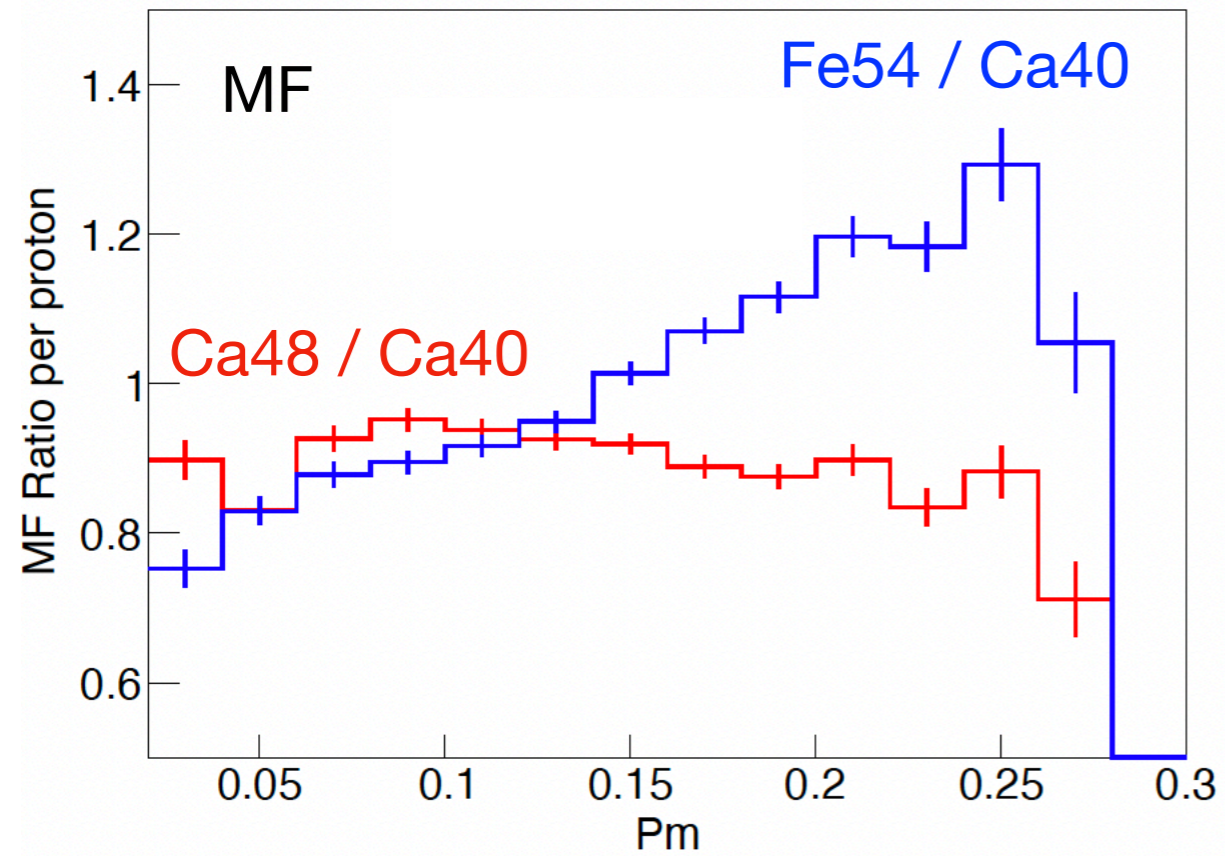
## Note:

- Radiative correction included
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R.J.Furnstahl et al. arXiv:2402.00634v2 (OSU)

Wiringa et al, Phys.Rev.C89 (AV18)

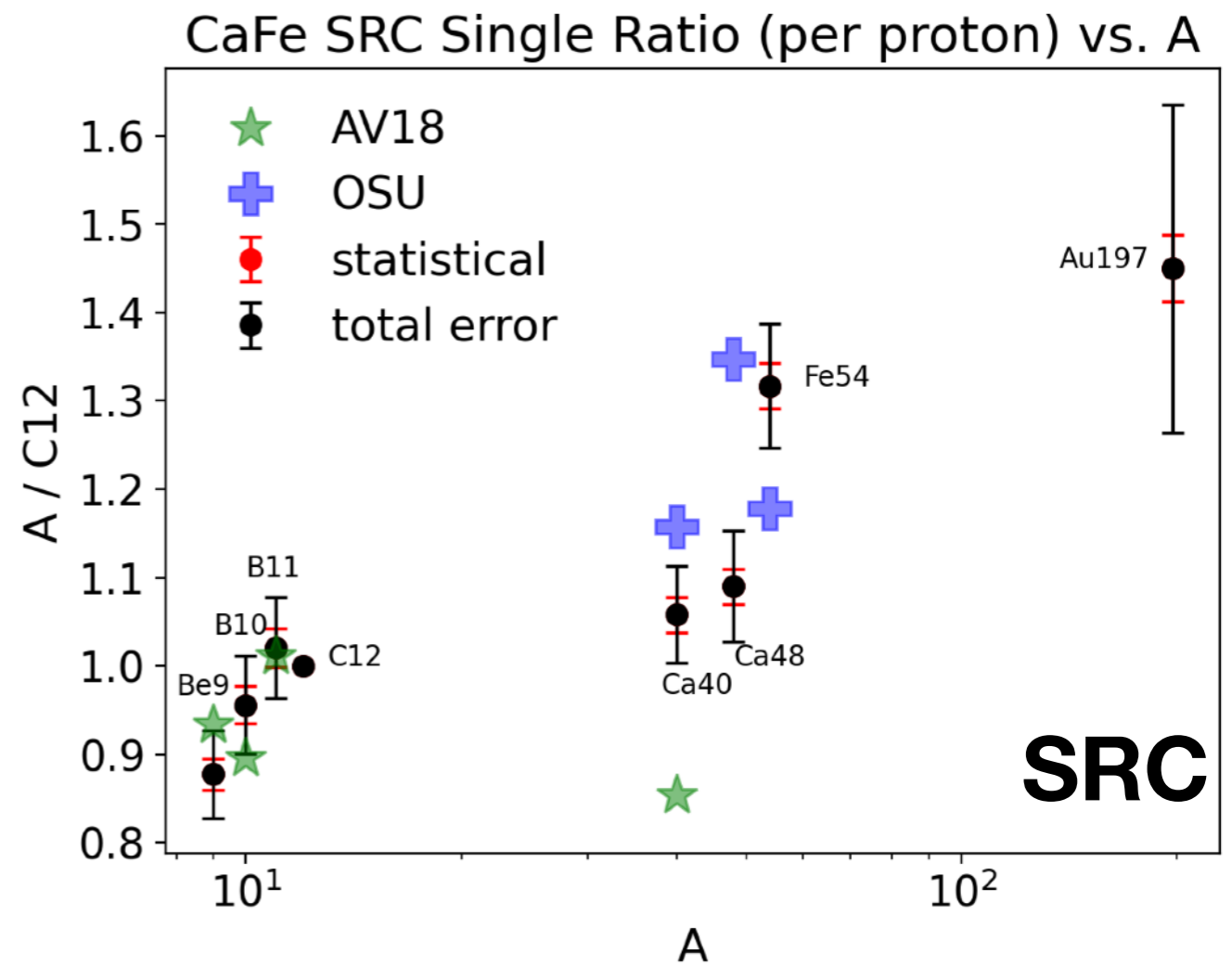
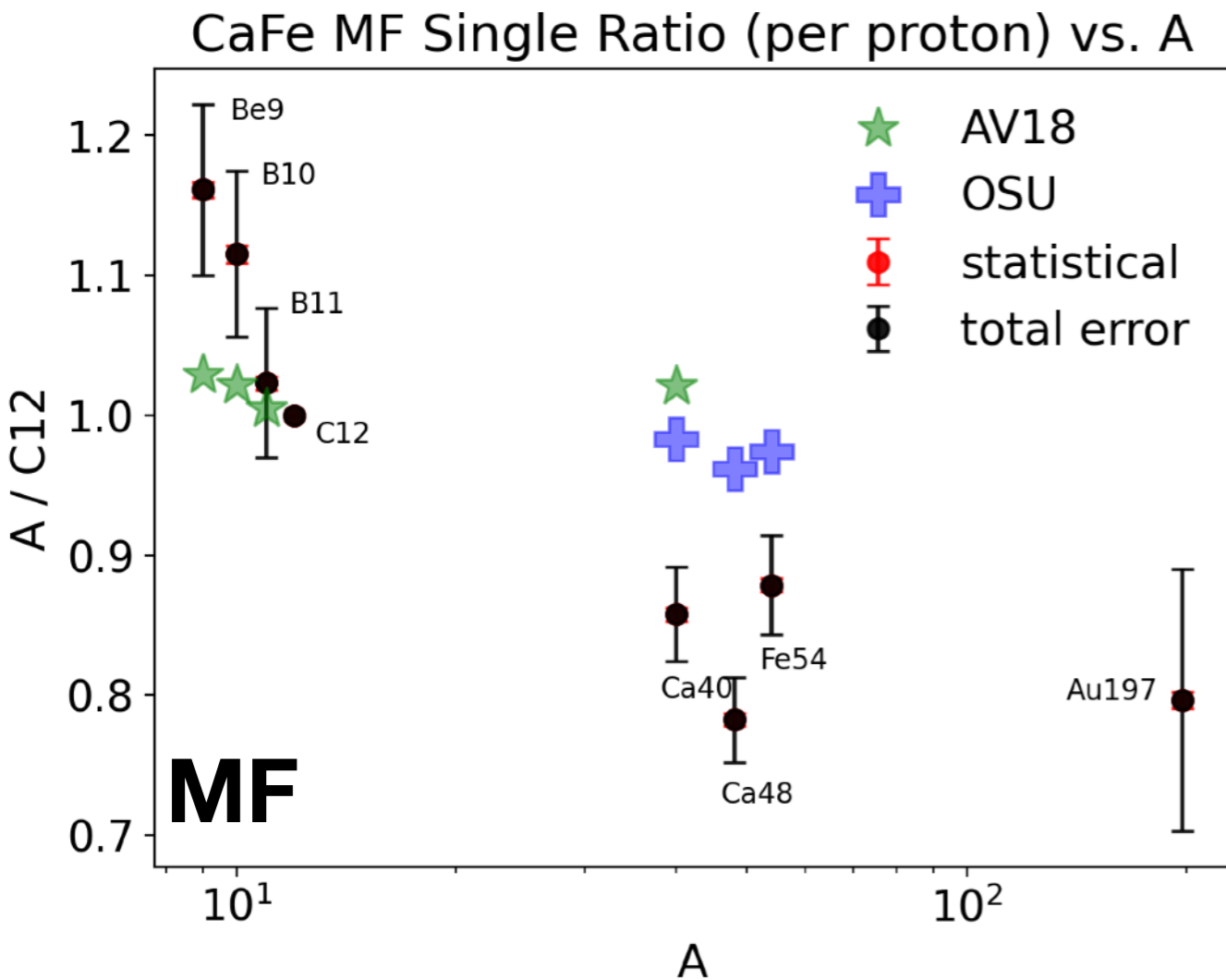
# Single Ratio to Ca40 (per proton)



Single Ratios to C12 (per proton)

Integrated over Missing Momentum





- the **data** MF single ratio decreases with  $A$ ; models are flat
- the **data** SRC single ratio increases with  $A$ ;

[R.J.Furnstahl et al. arXiv:2402.00634v2 \(OSU\)](https://arxiv.org/abs/2402.00634v2)

[Wiringa et al, Phys.Rev.C89 \(AV18\)](https://arxiv.org/abs/1903.04467)

# Double Ratios

$$\frac{A(e, e'p)^{SRC}}{A(e, e'p)^{MF}}$$
$$\frac{{}^{12}\text{C}(e, e'p)^{SRC}}{{}^{12}\text{C}(e, e'p)^{MF}}$$

*“a.k.a. high-momentum fraction”*

$$Y_A \equiv A(e, e'p) : \frac{N}{Q \cdot \epsilon_i \cdot T_N \cdot \sigma_t}$$

$N$  :  $(e, e'p)$  coincidence counts

$Q$  : total charge [mC]

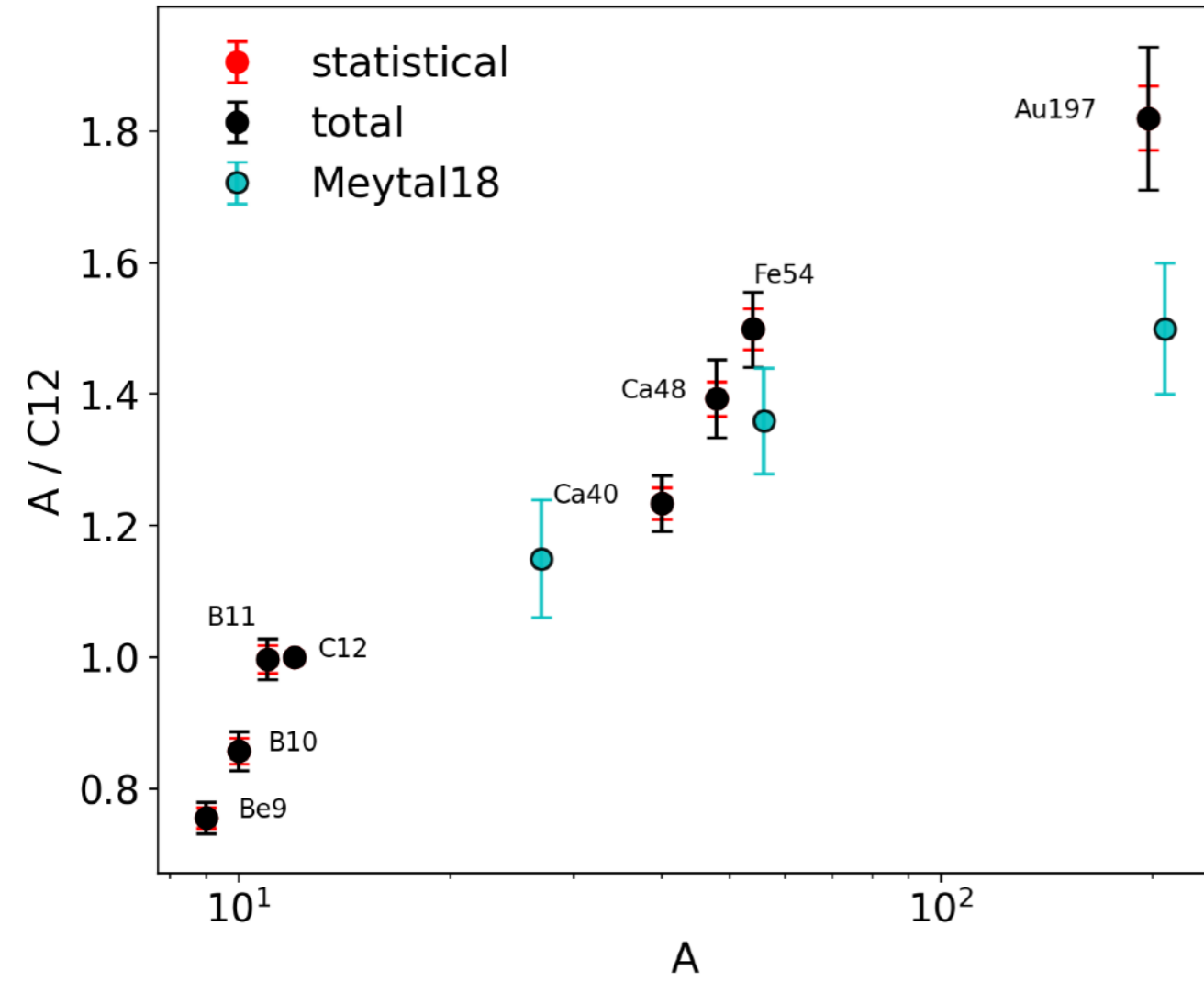
$\epsilon_i$  : detector/DAQ efficiencies

$T_N$  : nuclear transparency

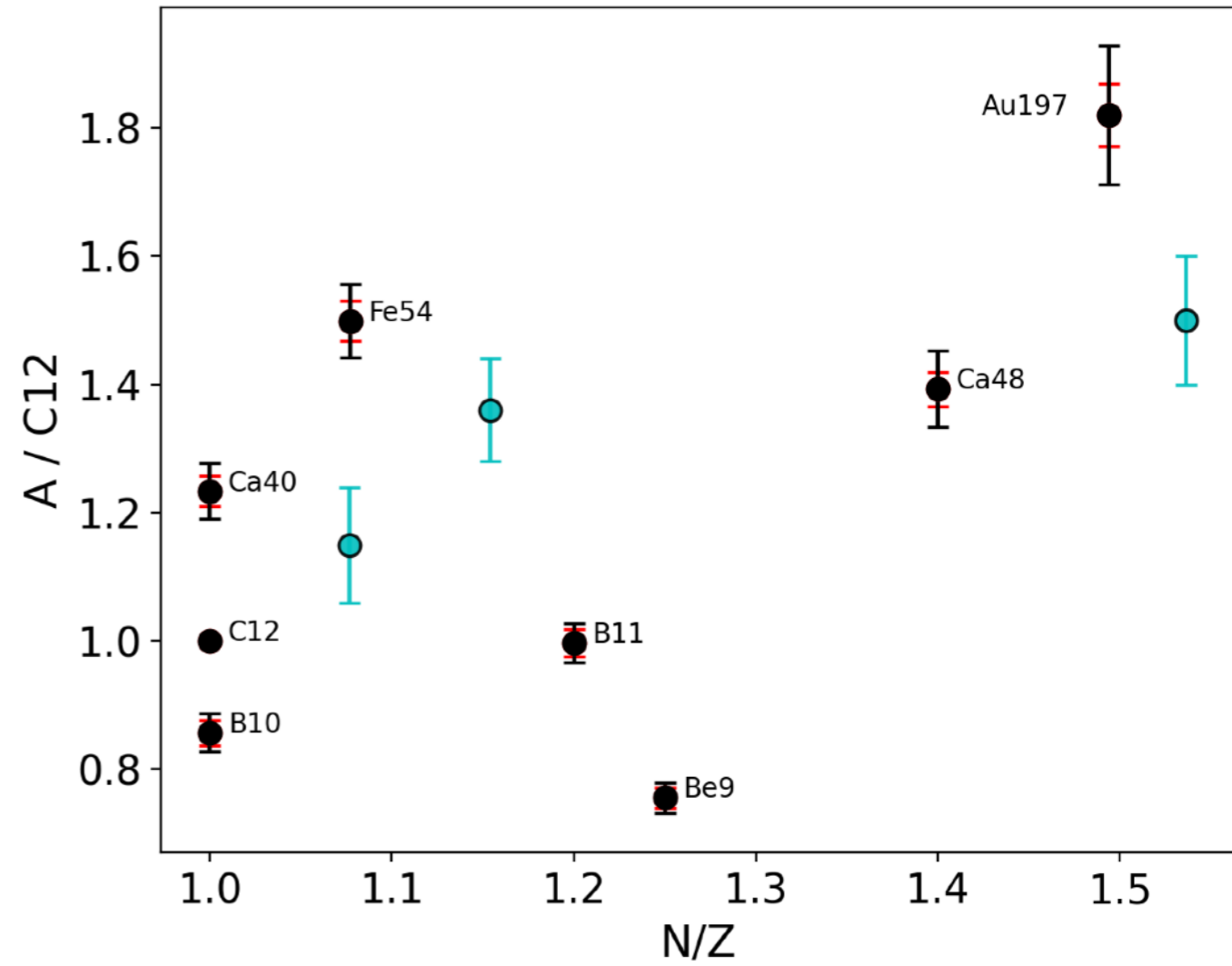
$\sigma_t$  : target thickness [g/cm<sup>2</sup>]

*cancel in double ratio*

CaFe Double Ratio vs. A

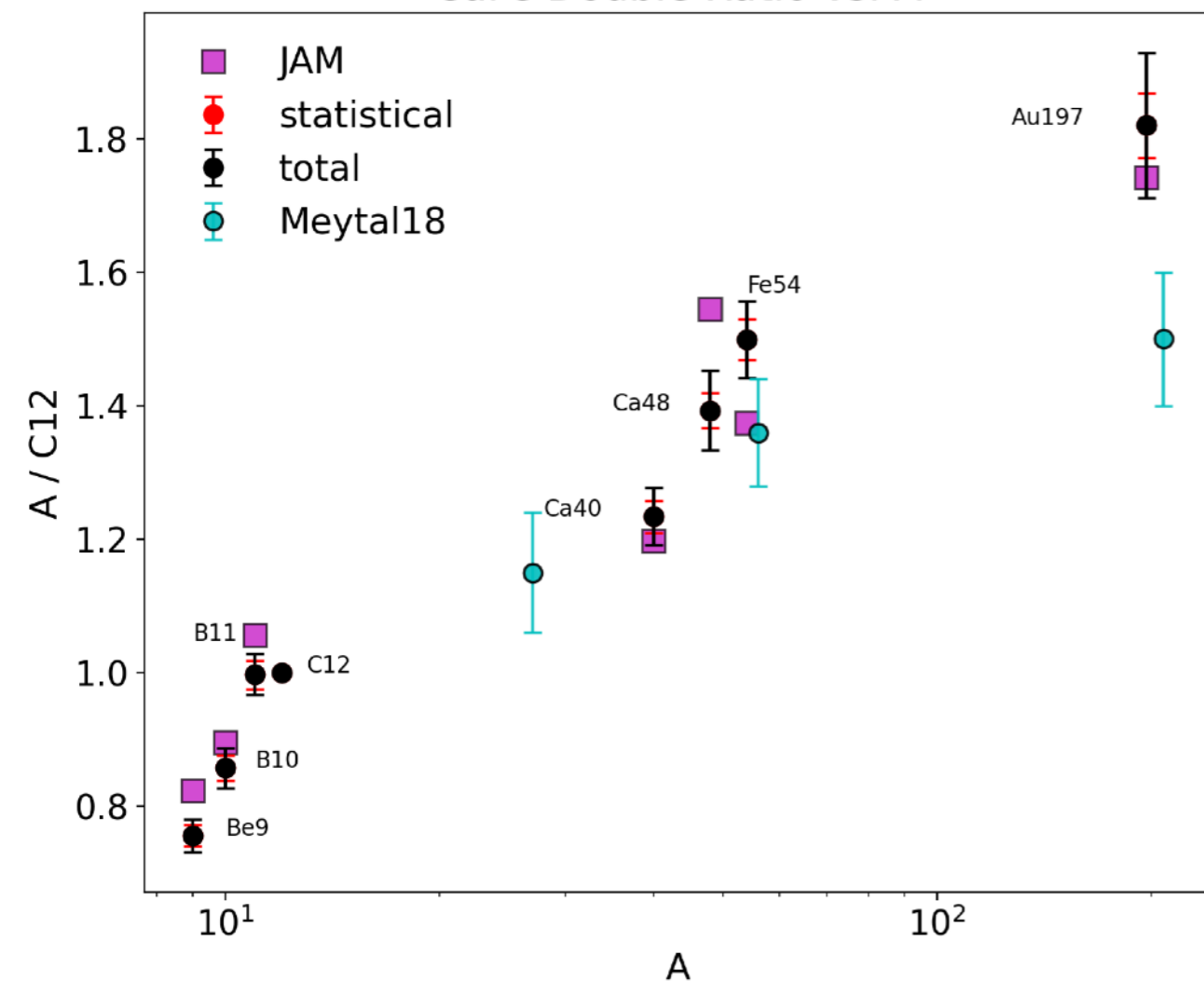


CaFe Double Ratio vs. N/Z

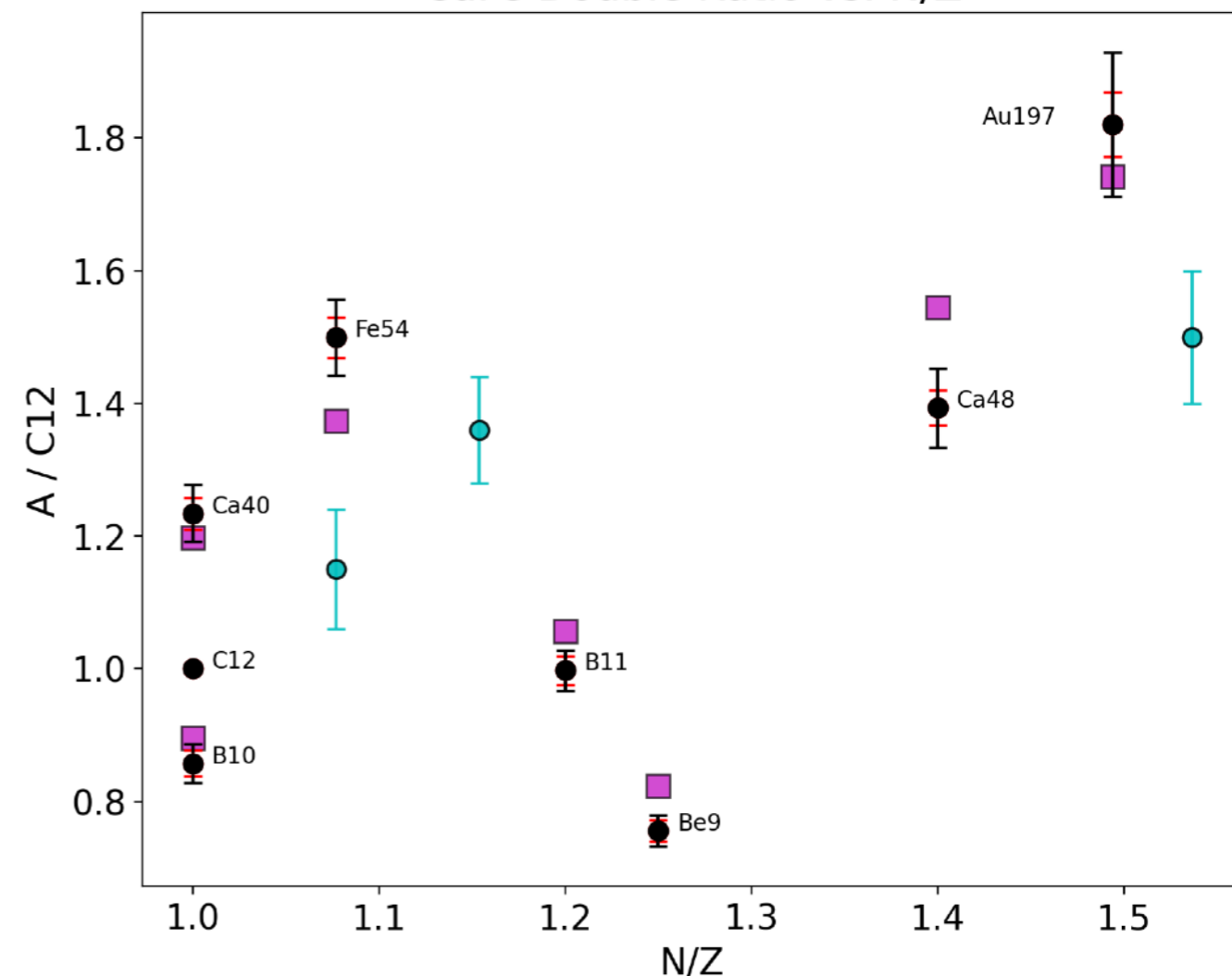


[M. Duer et al. \(CLAS collaboration\), Nature 560, 617 \(Meytal 18\)](#)

CaFe Double Ratio vs. A



CaFe Double Ratio vs. N/Z

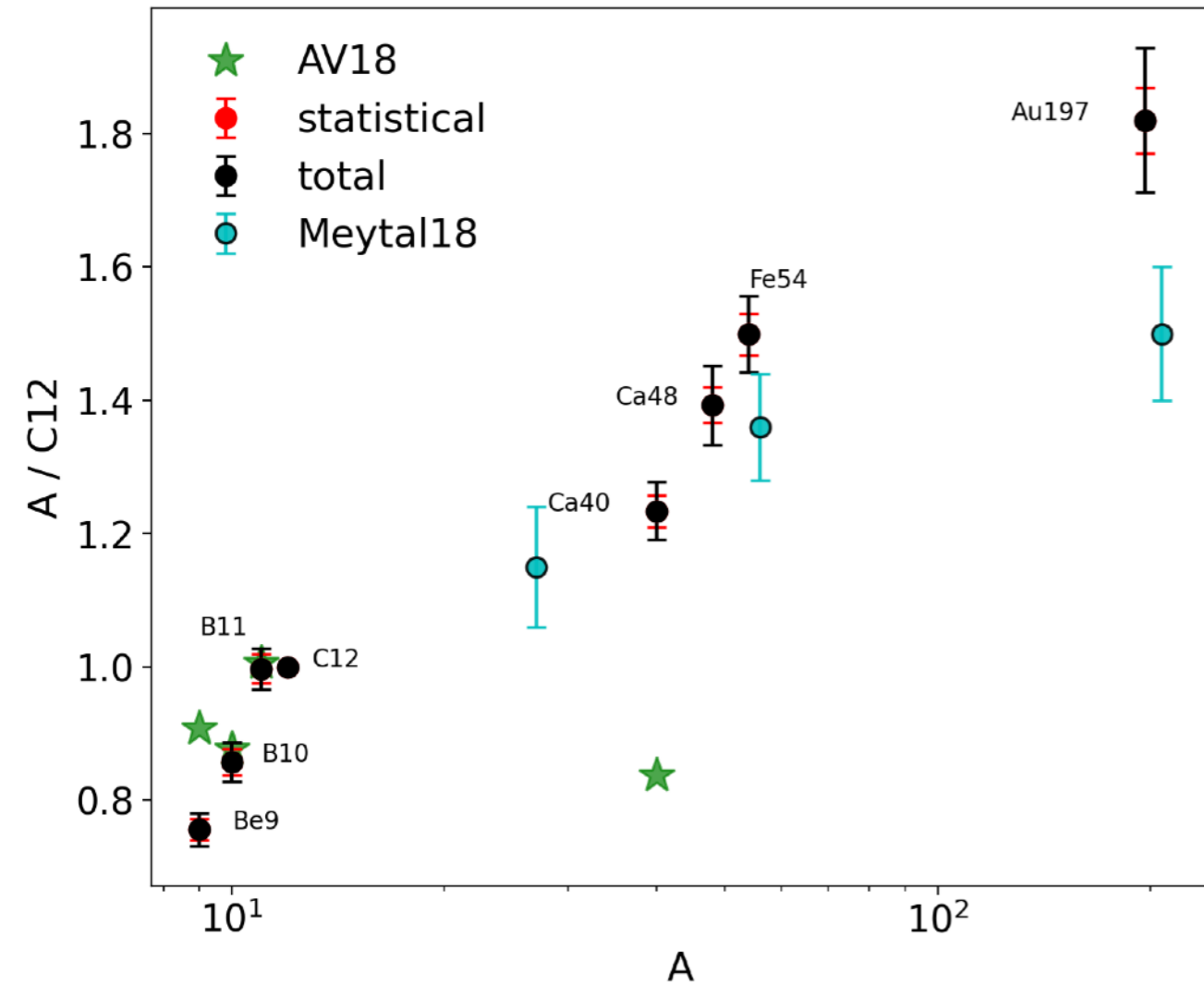


- The spatial-overlap **JAM** model describes the double-ratio data well, **BUT**
  - **OVER-PREDICTS** the Ca48 double ratio and **UNDER-PREDICTS** that of Fe54, indicating the importance of shell-closure effects

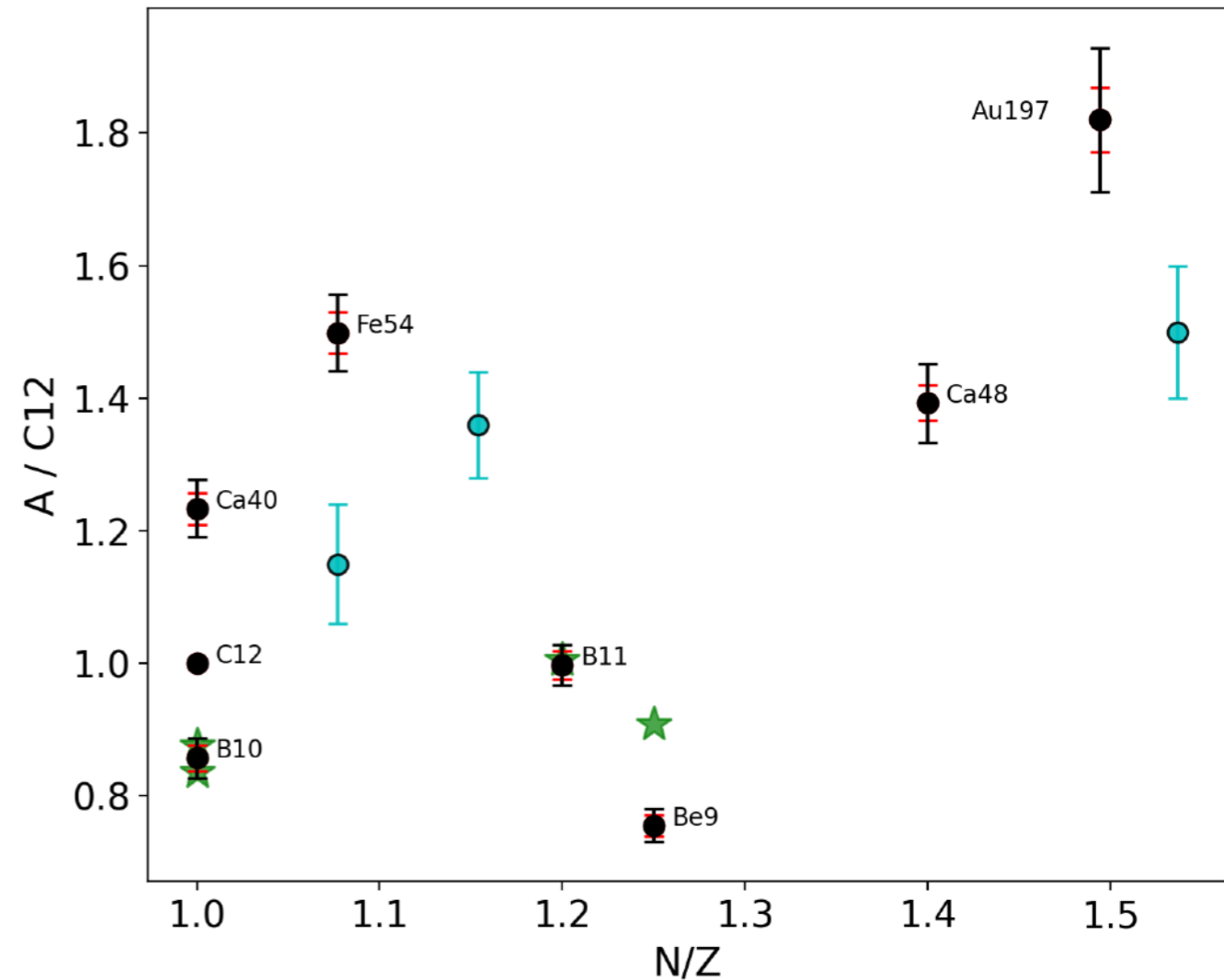
[M. Duer et al. \(CLAS collaboration\), Nature 560, 617 \(Meytal 18\)](#)

[Justin-Andrew Model \(JAM, 2023\)](#)

CaFe Double Ratio vs. A



CaFe Double Ratio vs. N/Z

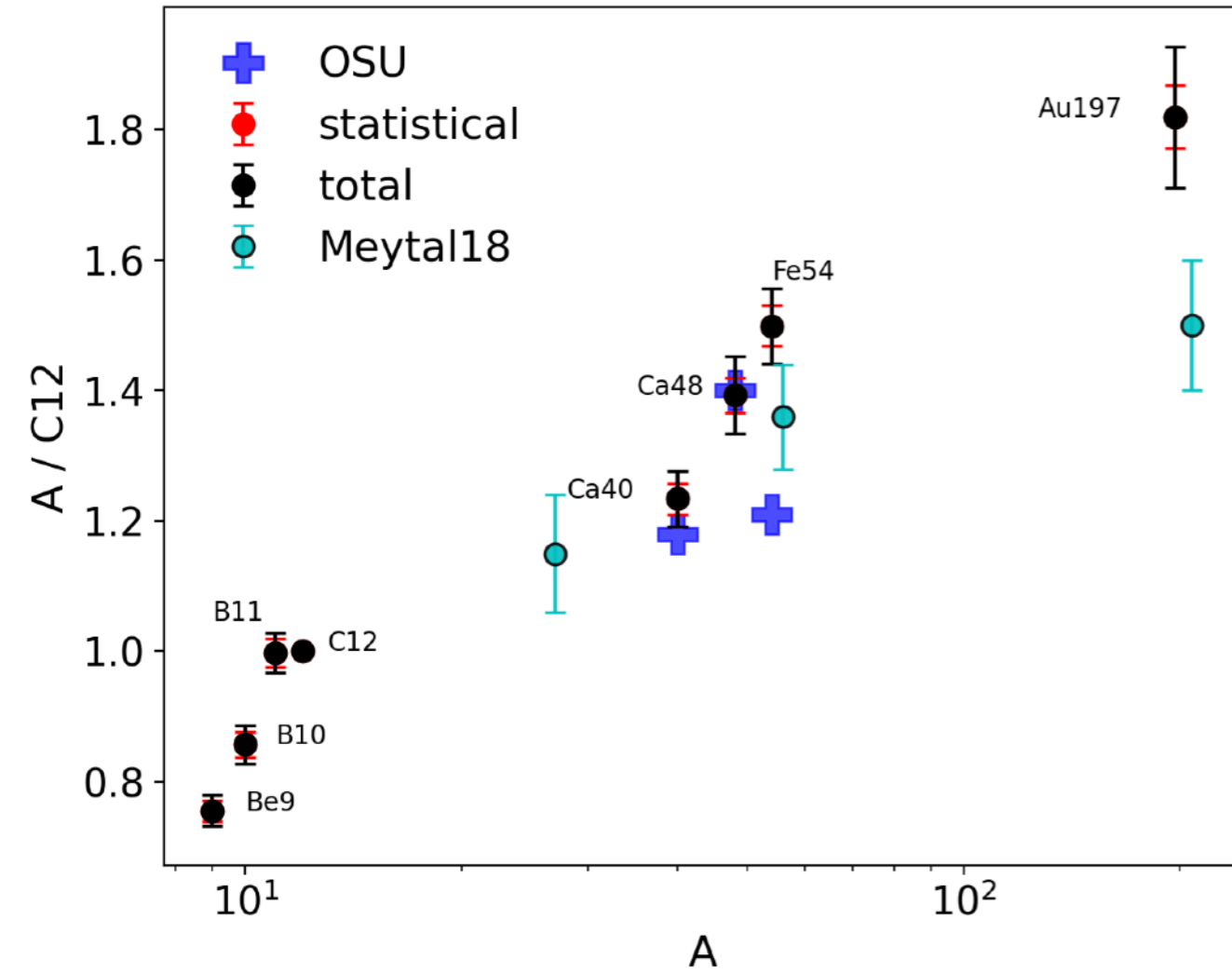


- ratios of **AV18** momentum distributions do not describe the data well; they describe B10, B11, but **DO NOT** describe Be9 or Ca40

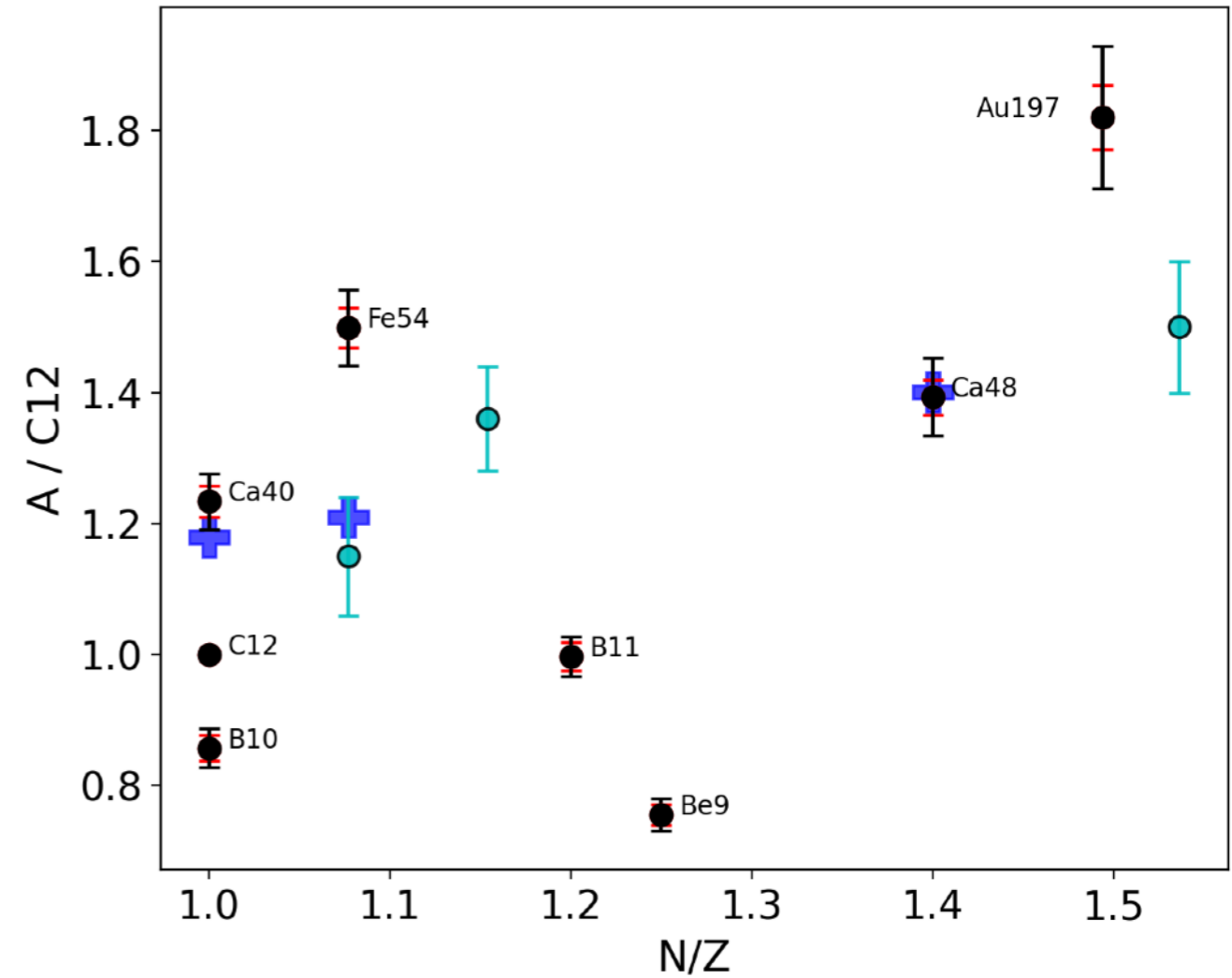
[M. Duer et al. \(CLAS collaboration\), Nature 560, 617 \(Meytal 18\)](#)

[Wiringa et al, Phys.Rev.C89 \(AV18\)](#)

CaFe Double Ratio vs. A



CaFe Double Ratio vs. N/Z

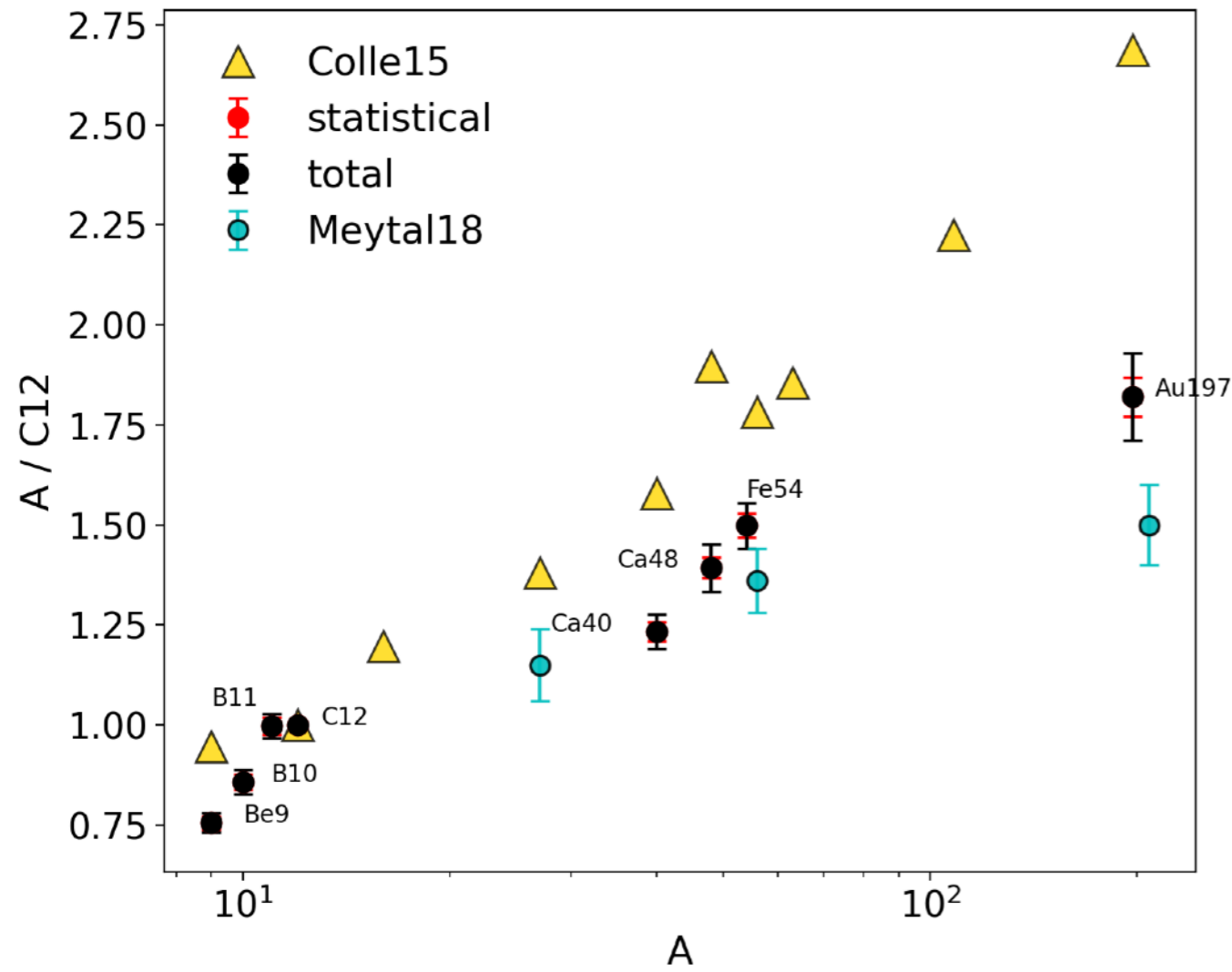


- ratios of **OSU** momentum distributions describe Ca40 and Ca48; but **DO NOT** describe well Fe54

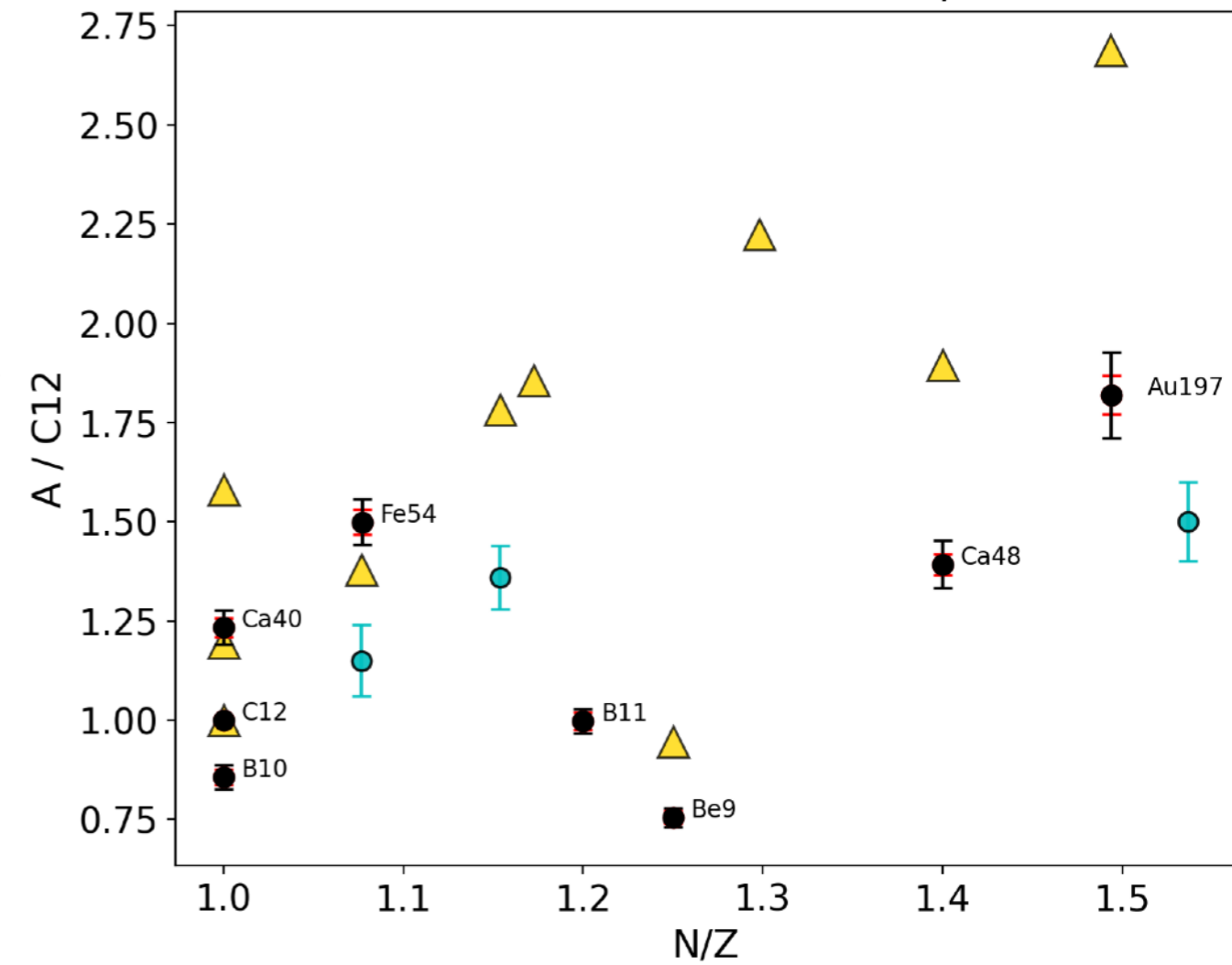
[M. Duer et al. \(CLAS collaboration\), Nature 560, 617 \(Meytal 18\)](#)

[R.J.Furnstahl et al. arXiv:2402.00634v2 \(OSU\)](#)

CaFe Double Ratio vs. A



CaFe Double Ratio vs. N/Z

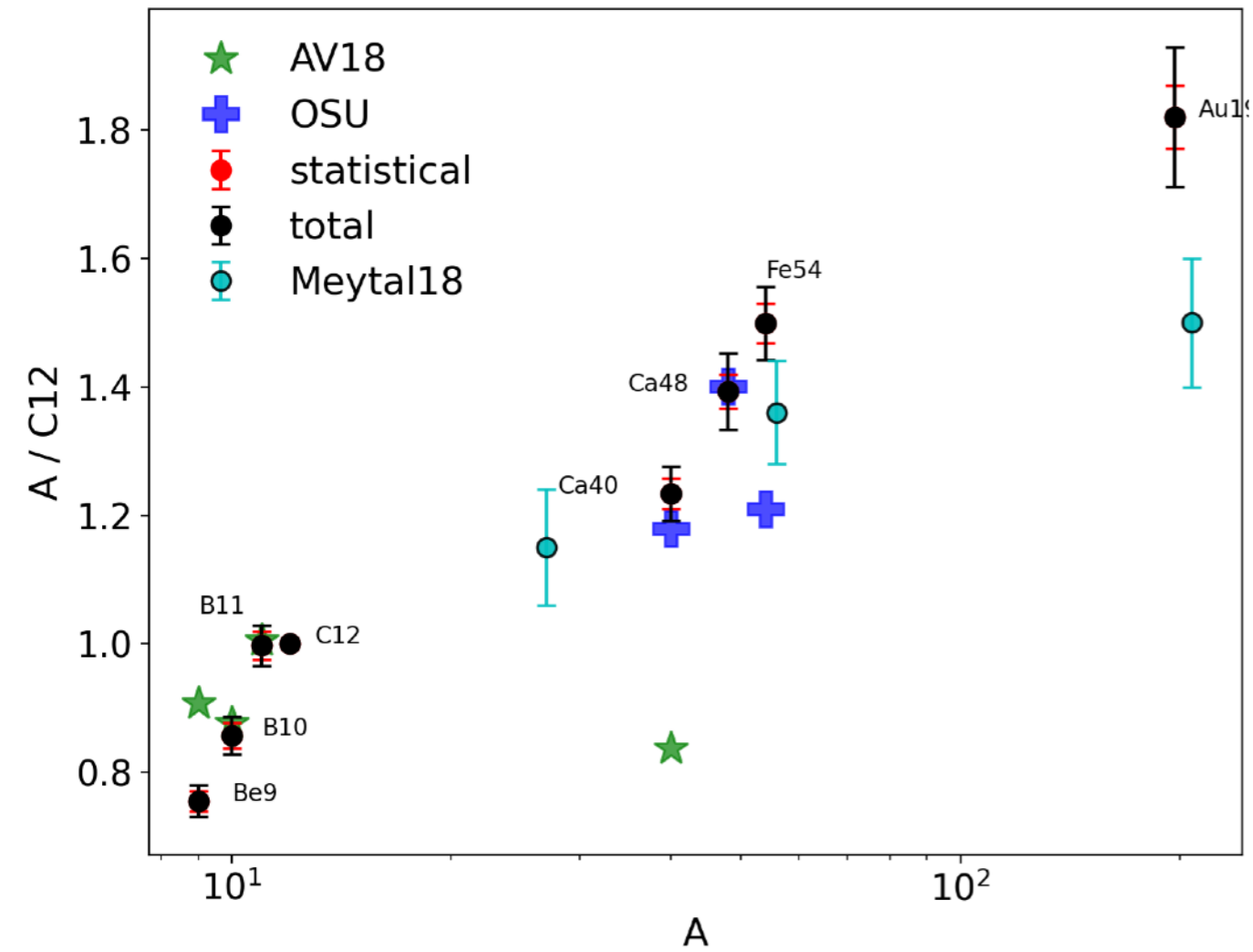


- ratios of **Colle15** **OVER-PREDICTS** almost all nuclei

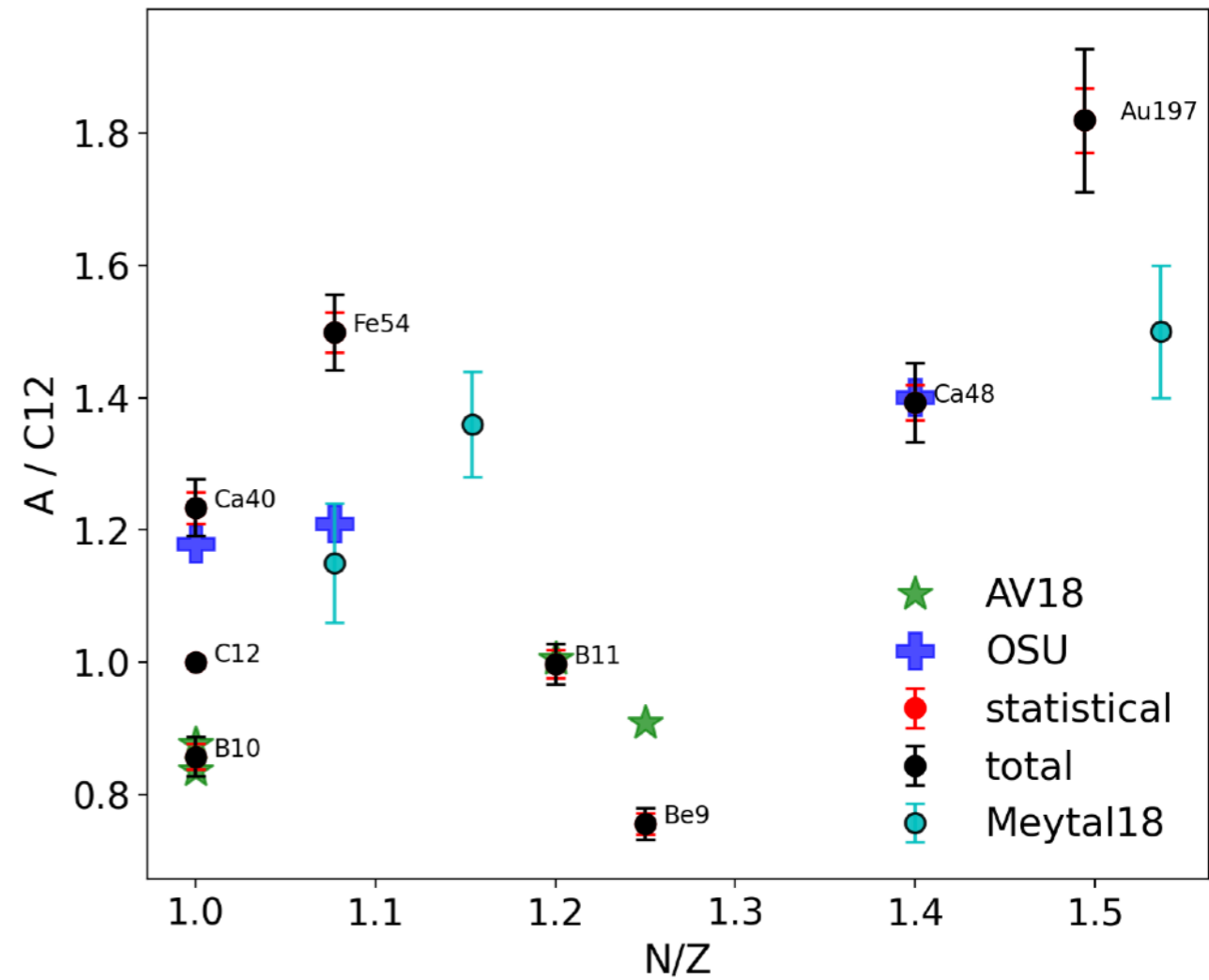
[M. Duer et al. \(CLAS collaboration\), Nature 560, 617 \(Meytal 18\)](#)

[Colle et al. Phys.Rev.C92 \(Colle 15\)](#)

CaFe Double Ratio vs. A



CaFe Double Ratio vs. N/Z



- models overlay: **OSU** + **AV18**

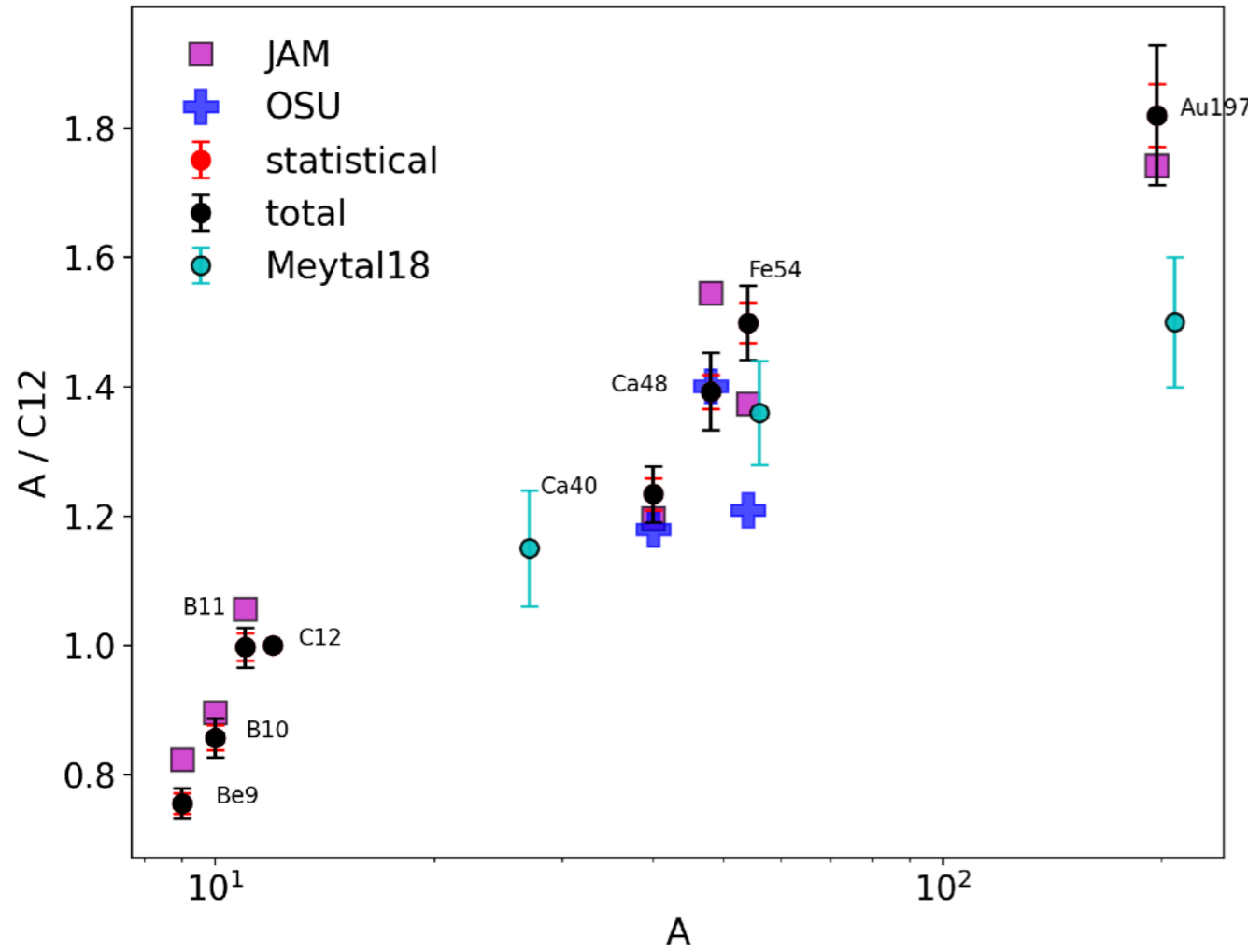
[M. Duer et al. \(CLAS collaboration\), Nature 560, 617 \(Meytal 18\)](#)

[R.J.Furnstahl et al. arXiv:2402.00634v2 \(OSU\)](#)

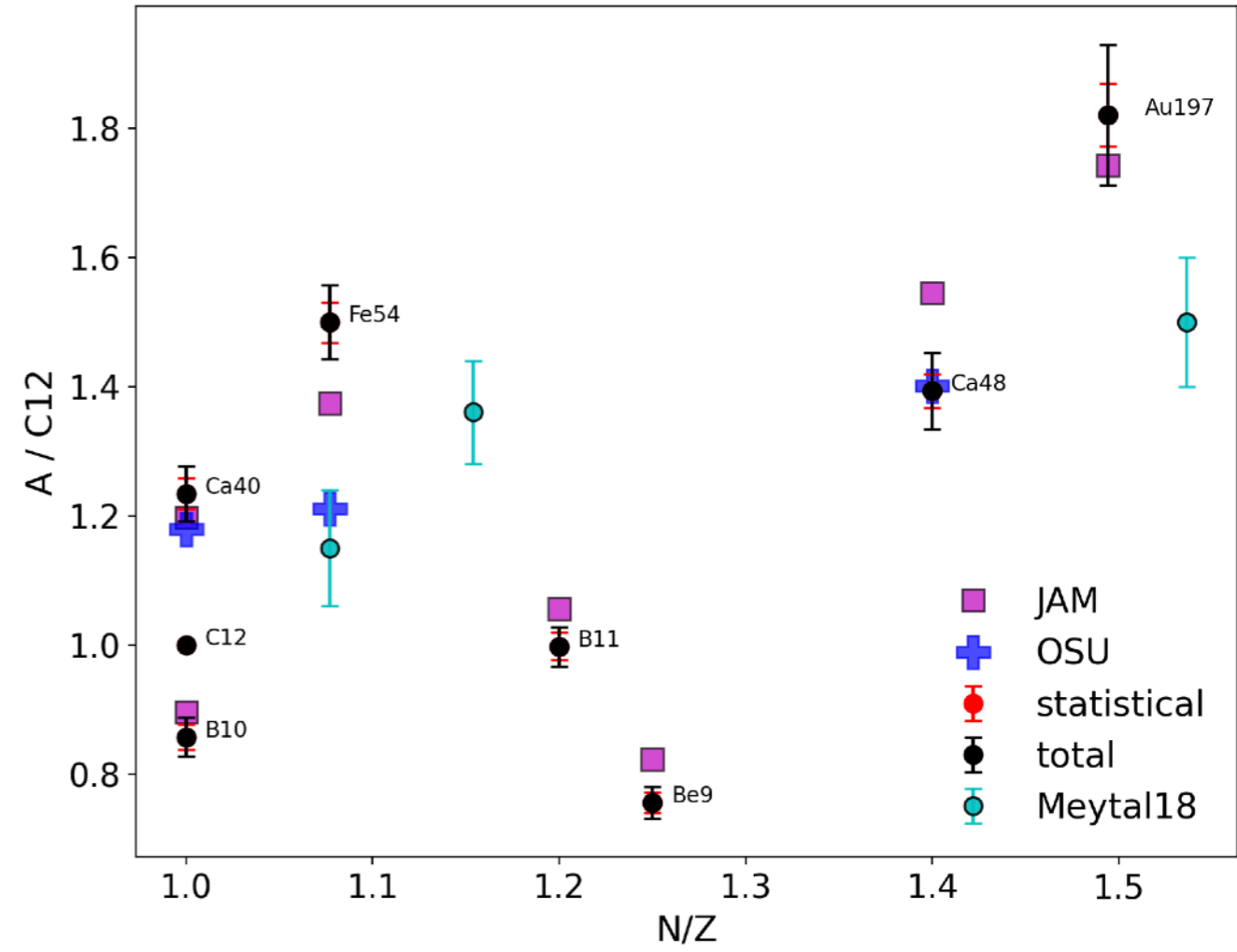
[Wiringa et al, Phys.Rev.C89 \(AV18\)](#)



CaFe Double Ratio vs. A



CaFe Double Ratio vs. N/Z



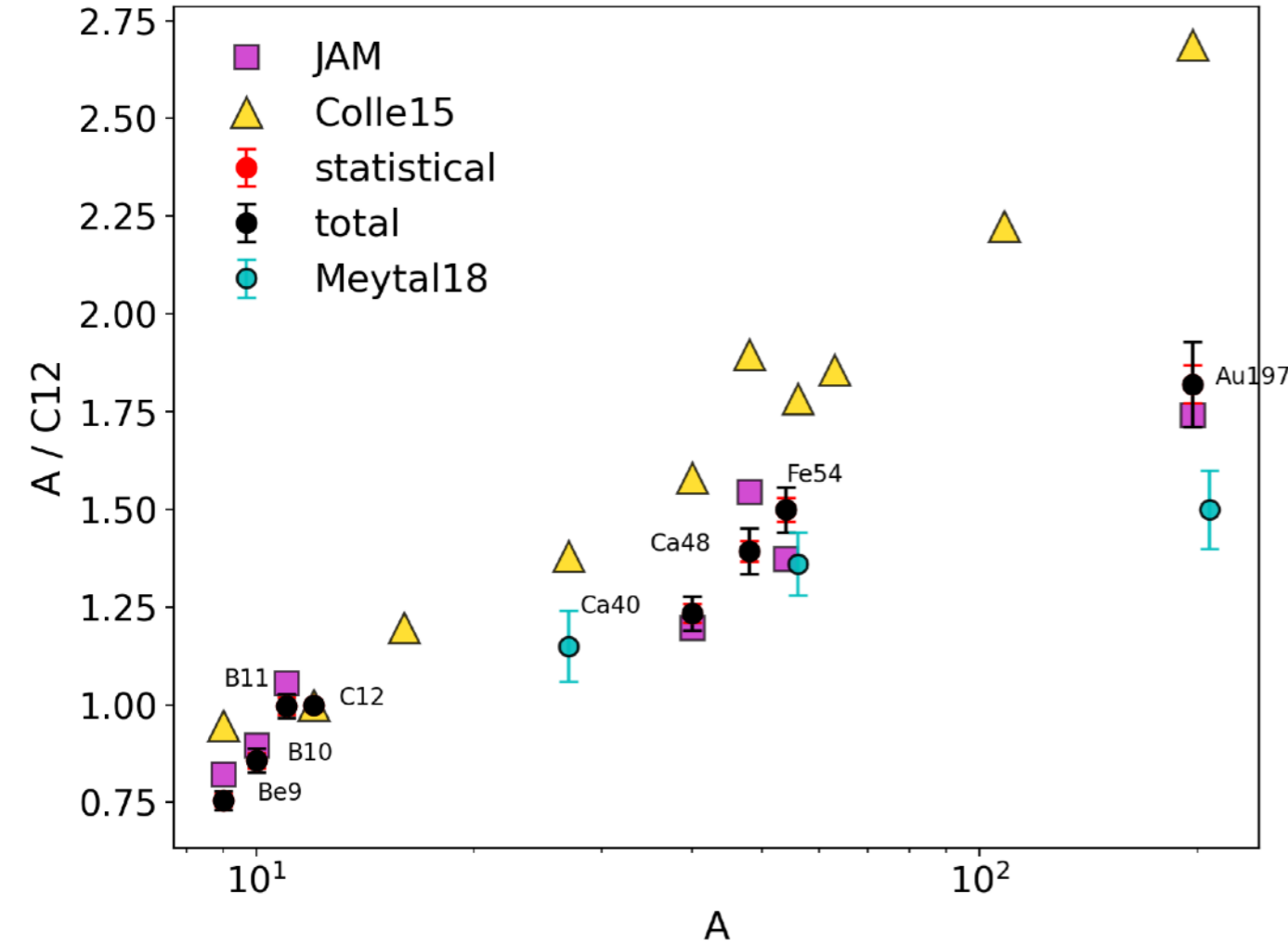
- models overlay: **OSU** + **JAM**

[M. Duer et al. \(CLAS collaboration\), Nature 560, 617 \(Meytal 18\)](#)

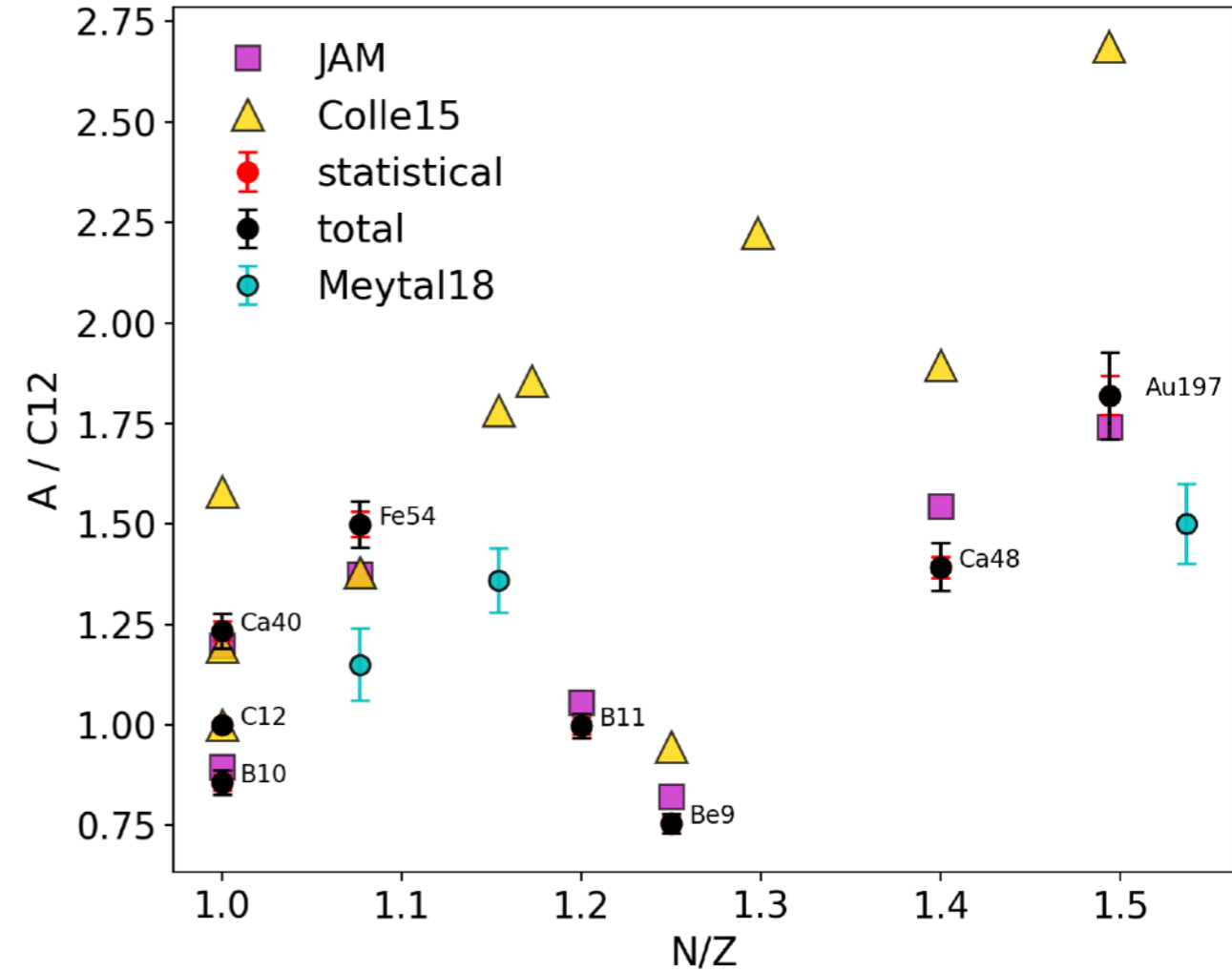
[R.J.Furnstahl et al. arXiv:2402.00634v2 \(OSU\)](#)

[Justin-Andrew Model \(JAM, 2023\)](#)

CaFe Double Ratio vs. A



CaFe Double Ratio vs. N/Z



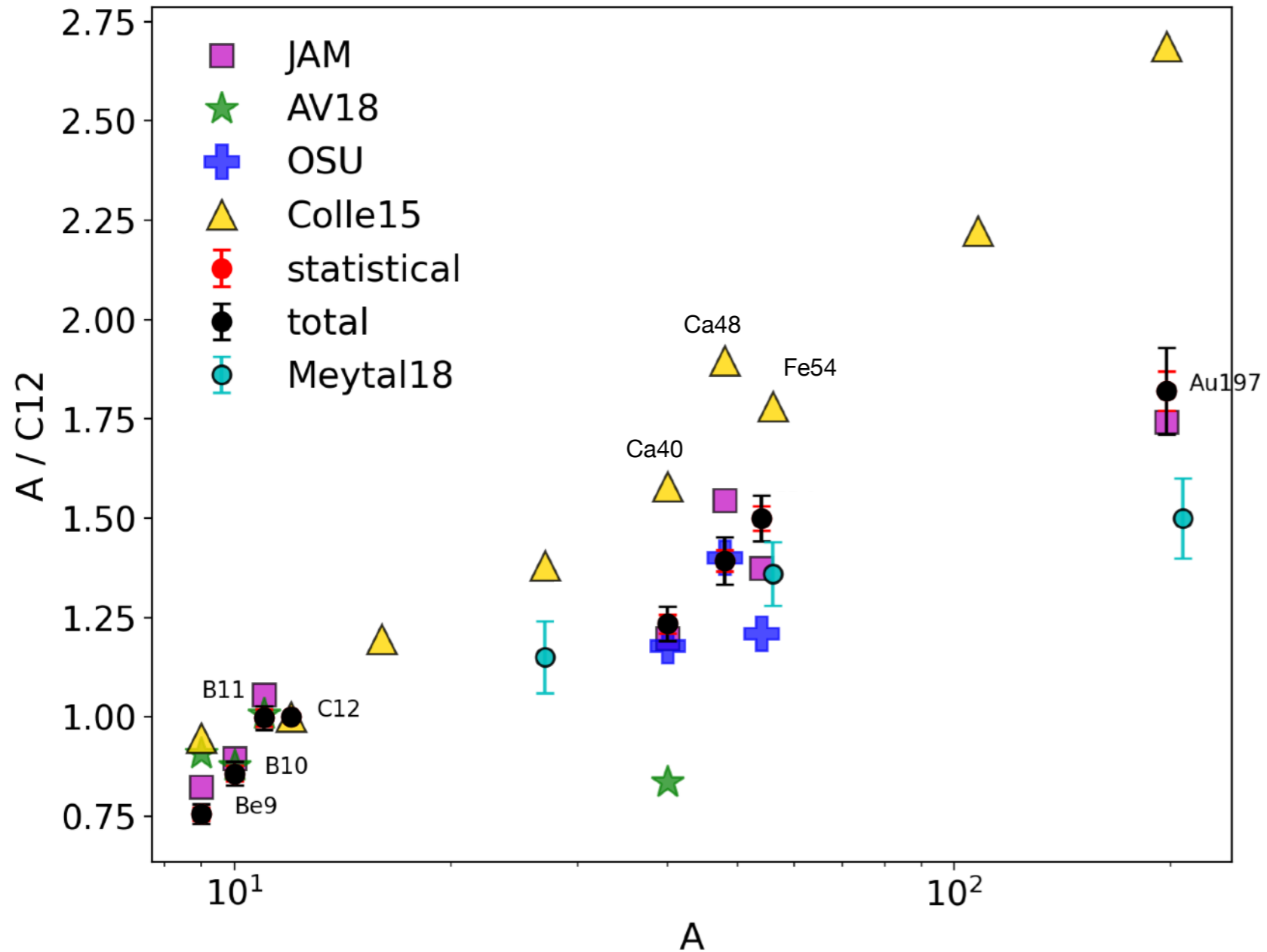
- models overlay: **JAM** + **Colle15**

[M. Duer et al. \(CLAS collaboration\), Nature 560, 617 \(Meytal 18\)](#)

[Justin-Andrew Model \(JAM, 2023\)](#)

[Colle et al. Phys.Rev.C92 \(Colle 15\)](#)

CaFe Double Ratio vs. A



- all models overlay

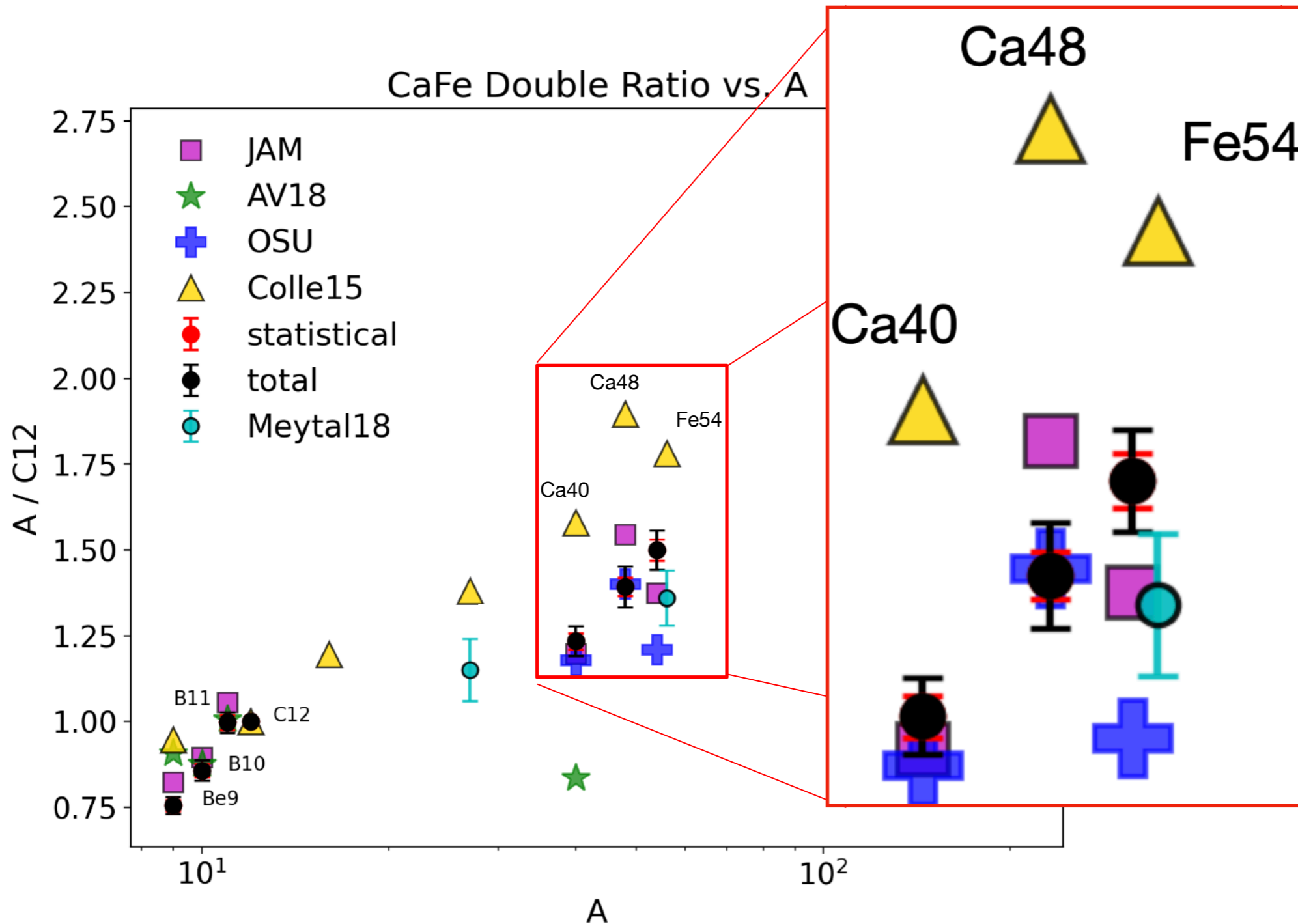
[M. Duer et al. \(CLAS collaboration\), Nature 560, 617 \(Meytal 18\)](#)

[Justin-Andrew Model \(JAM, 2023\)](#)

[Colle et al. Phys.Rev.C92 \(Colle 15\)](#)

[Wiringa et al, Phys.Rev.C89 \(AV18\)](#)

[R.J.Furnstahl et al. arXiv:2402.00634v2 \(OSU\)](#)



- **OSU + JAM + Colle15** predict less pairing in Fe54 compared to Ca48
- **data** does NOT show this decrease
  - stronger  $1f_{7/2} - 1f_{7/2}$  pairing for Fe54?

- all models overlay;

[M. Duer et al. \(CLAS collaboration\), Nature 560, 617 \(Meytal 18\)](#)

[Justin-Andrew Model \(JAM, 2023\)](#)

[Wiringa et al, Phys.Rev.C89 \(AV18\)](#)

[Colle et al. Phys.Rev.C92 \(Colle 15\)](#)

[R.J.Furnstahl et al. arXiv:2402.00634v2 \(OSU\)](#)

# Summary

## Conclusions:

1. the MF single ratio to C data decreases with A; models are flat; we **DO NOT** understand this !
2. the SRC single ratio to C increases with A; models **DO NOT** show this trend;
3. the SRC/MF double ratio to C increases with A as expected  
it does not increase with N/Z; different from [Duer \(2018\)](#)
4. Models:
  - a. The spatial-overlap (**JAM**) model describes the double-ratio data well
  - b. ratios of **AV18** momentum distributions describe B10, B11, but not Be9 or Ca40
  - c. ratios of **OSU** momentum distributions describe Ca40 and Ca48 but not Fe54
  - d. **OSU** + **JAM** + **Colle15** predict weaker pairing for Ca48  $\rightarrow$  Fe54; **data** predict stronger pairing

Failure of models to describe Ca40, Ca48 and Fe54 double ratios

$\Rightarrow$  important of shell effects in SRC pairing !

More data on  $(e, e'p)$ ,  $(e, e'n)$ ,  $(e, e'np)$ ,  $(e, e'pp)$  coming soon from CLAS12 on C, Ca40, Ca48

Holly Szumila-Vance  
(Staff)



Florian Hauenstein  
(Staff)



Dien Nguyen  
(Isgur Fellow)



Carlos Yero  
(NSF Fellow)



Noah Swan  
(PhD student)



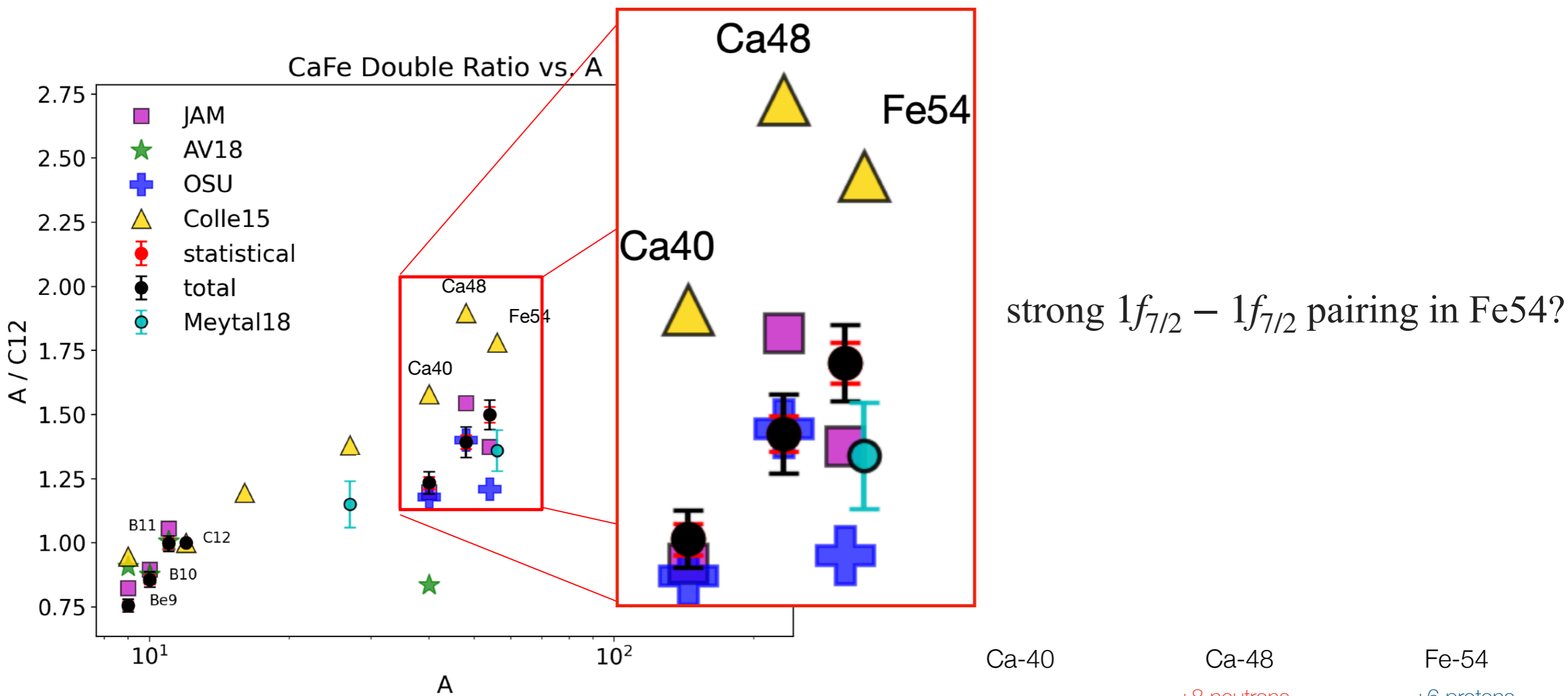
National  
Science  
Foundation

# Thanks !

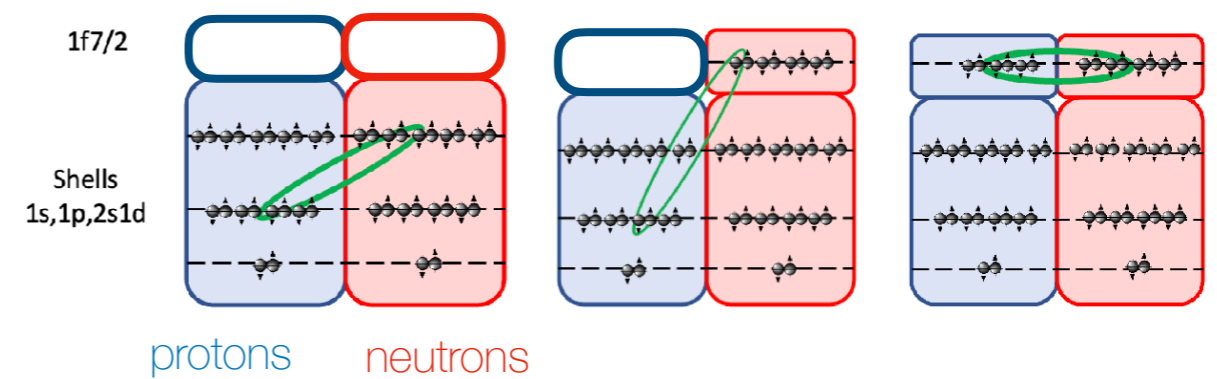
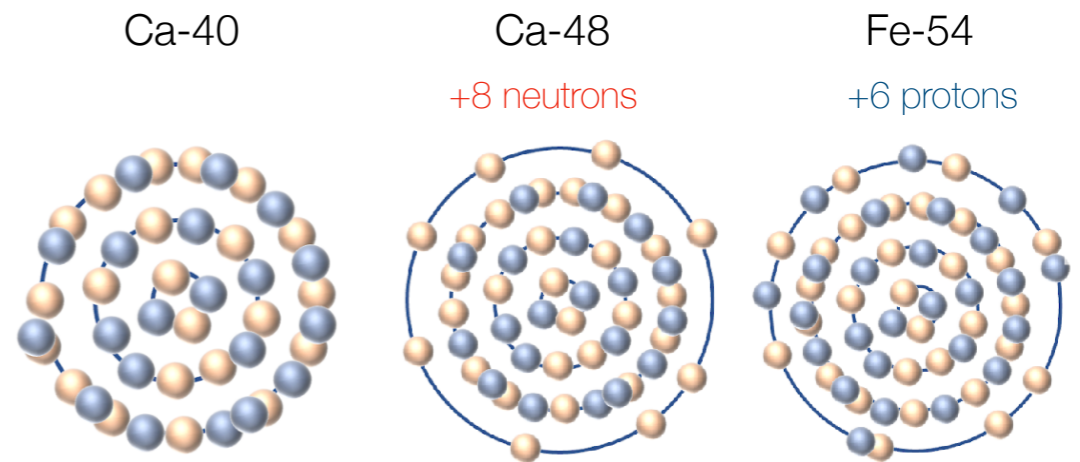
**Spokespeople:** D. Higinbotham (JLab), F. Hauenstein (JLab), O. Hen (MIT), L. Weinstein (ODU)

"This material is based upon work supported by the National Science Foundation under Grant No. 2137604"

# Backup Slides

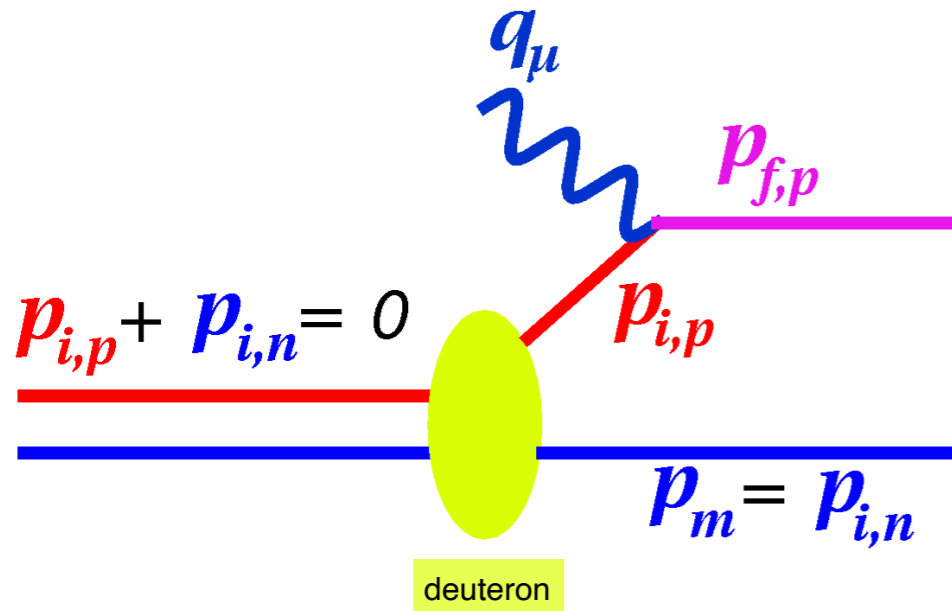


**OSU + JAM + Colle15**  
 predict less pairing in  
 Fe54 compared to Ca48;

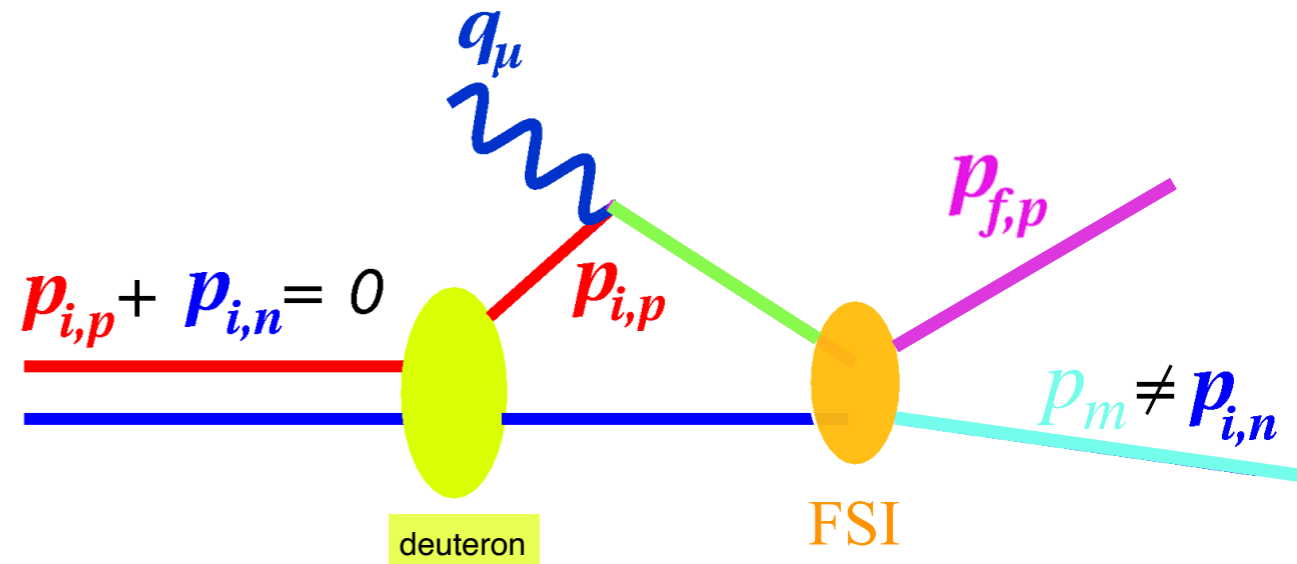




# virtual photon - nucleus interactions

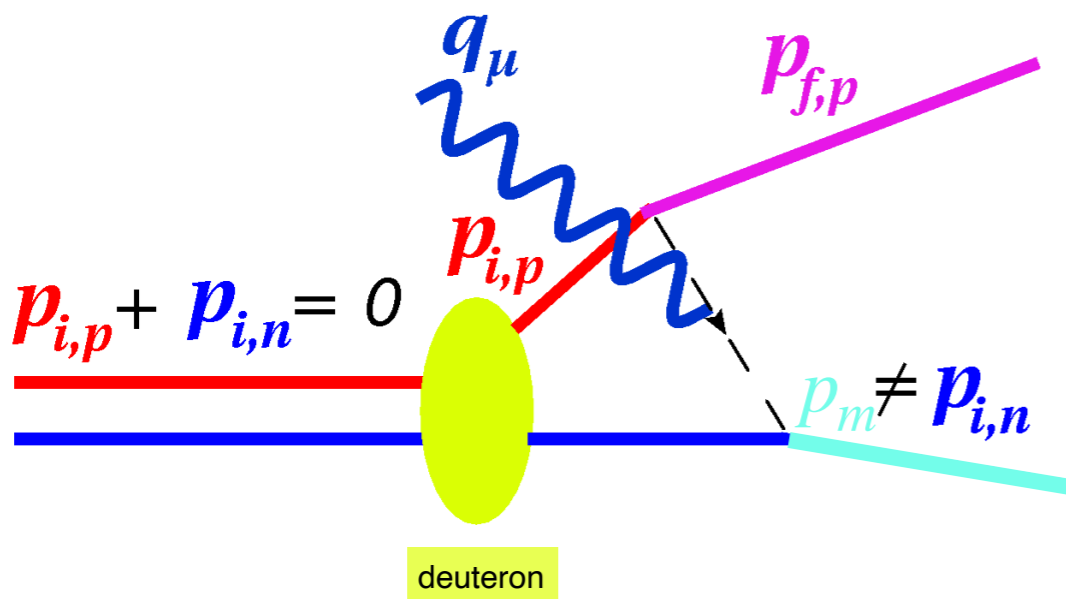


Plane Wave Impulse Approximation (PWIA)



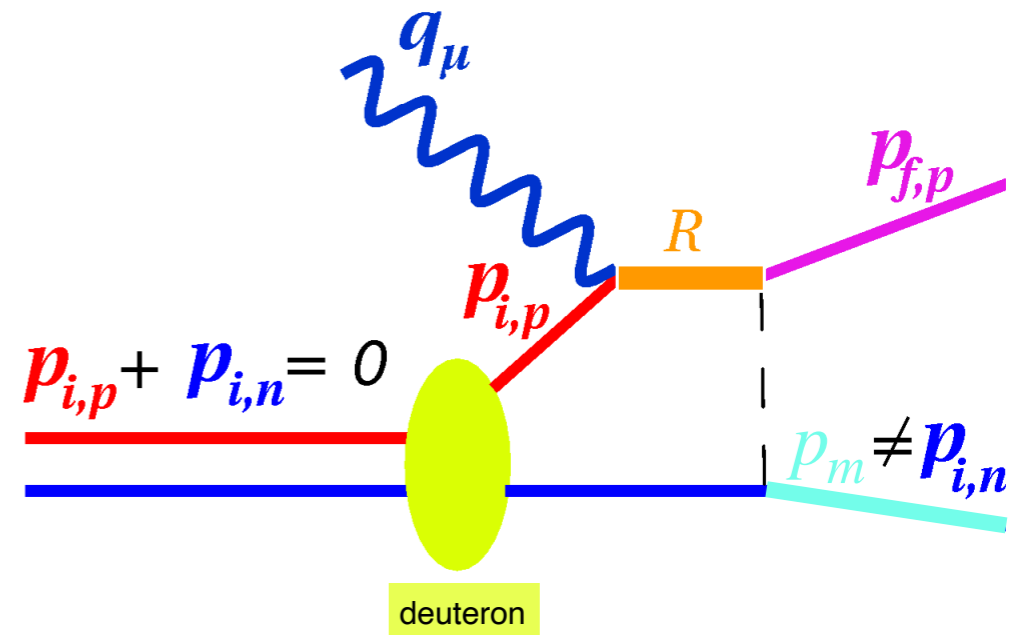
Final State Interactions (FSI)

suppressed at specific  $\theta_{nq} < 40$  deg



Meson-Exchange Currents (MEC)

suppressed at  $Q^2 > 1(\text{GeV}/c)^2$



Delta,  $N^*$  Resonance Excitations (IC)

suppressed at  $x_{Bj} > 1$

# Data/SIMC Single MF Ratios (per proton)

SIMC: Hall C standard  $A(e, e'p)$  simulation program

Purpose: Check SIMC per-proton raw cross sections  
for C12, Fe56, Au197 MF kinematics

$$Y = \frac{N_{e,e'p}}{T \cdot \sigma_{thick} \cdot Z/A}$$

Charge Q = 1 mC

Target (Z, A)	T	Target thickness (g/cm2)	raw counts	Yield
C12 (6, 12)	0.551	0.5738	1081	6838 . +/- 208
Fe56 (56, 26)	0.381	0.367	370.6	5708 . +/- 297
Au197 (79, 197)	0.281	0.4047	264.9	5808 . +/- 356

**SIMC Cuts (exactly same as data):**

**Kinematical**

-20 < Em < 90 MeV

Q2 > 1.8 GeV<sup>2</sup>

Pm < 270 MeV

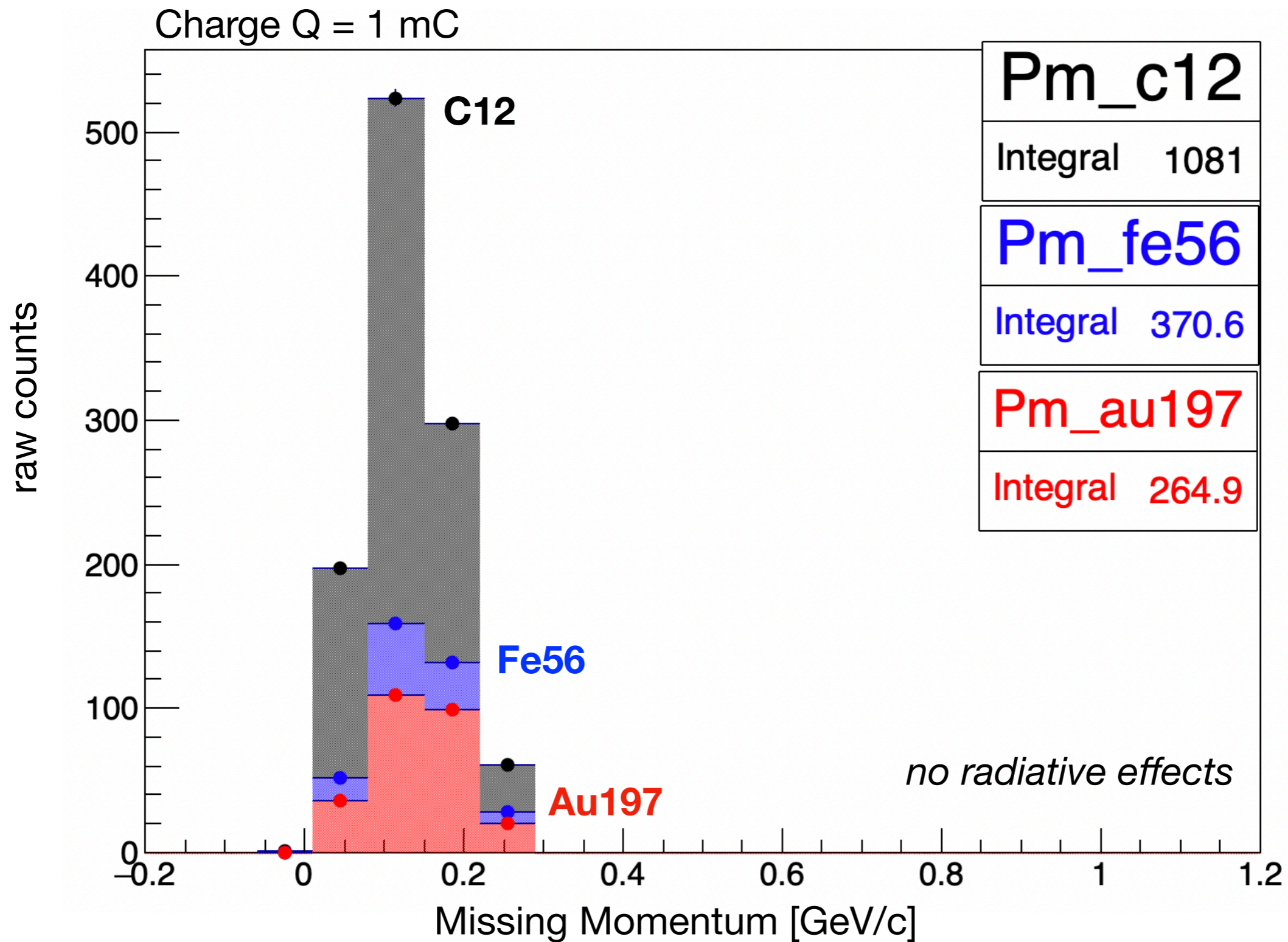
**Acceptance**

0 < SHMS delta < 22 %

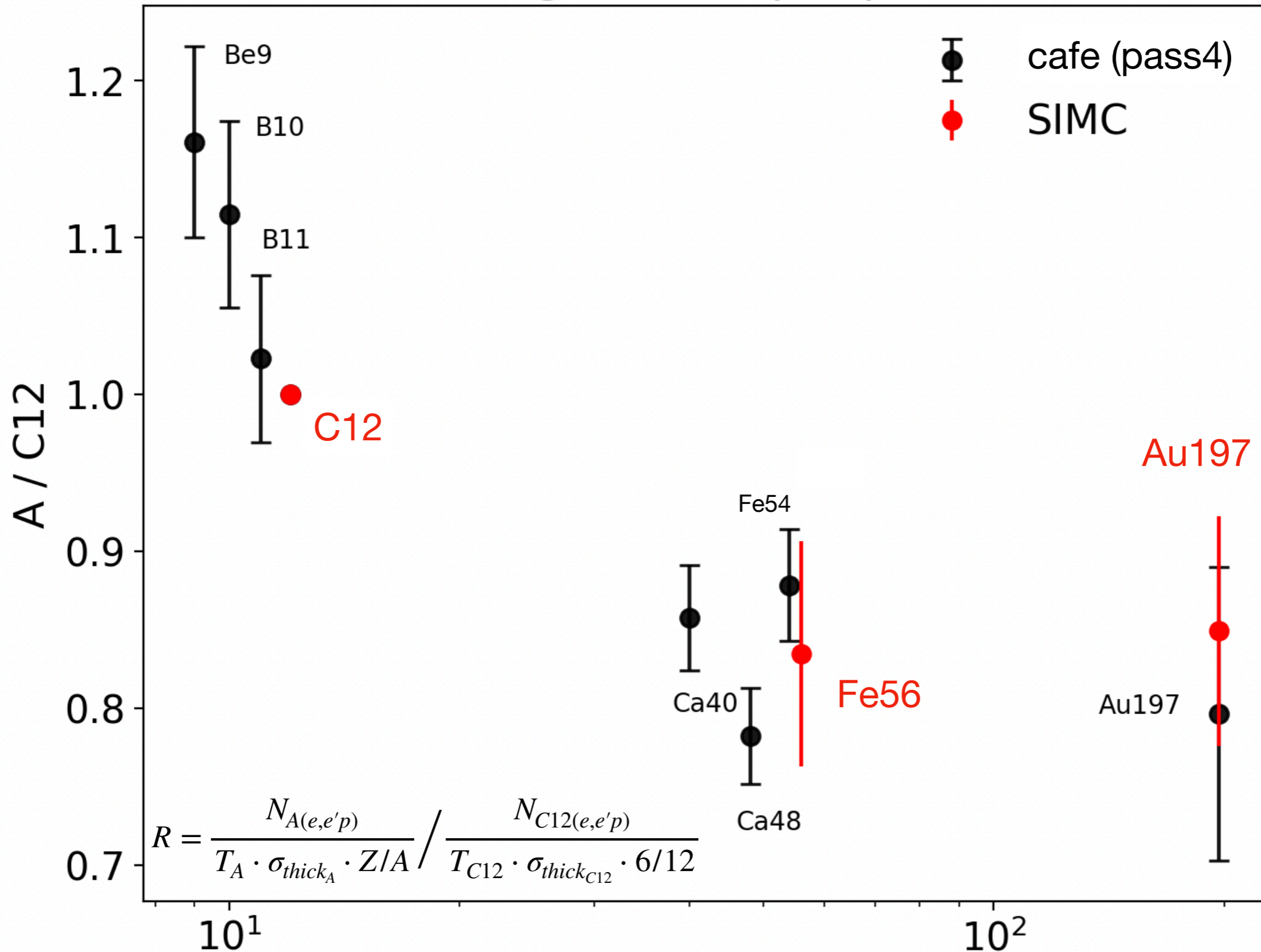
| HMS delta | < 10 %

HMS/SHMS collimator (was not done in SIMC)

Purpose: Check SIMC per-proton raw cross sections  
for C12, Fe56, Au197 MF kinematics



# CaFe MF Single Ratio (per proton) vs. A

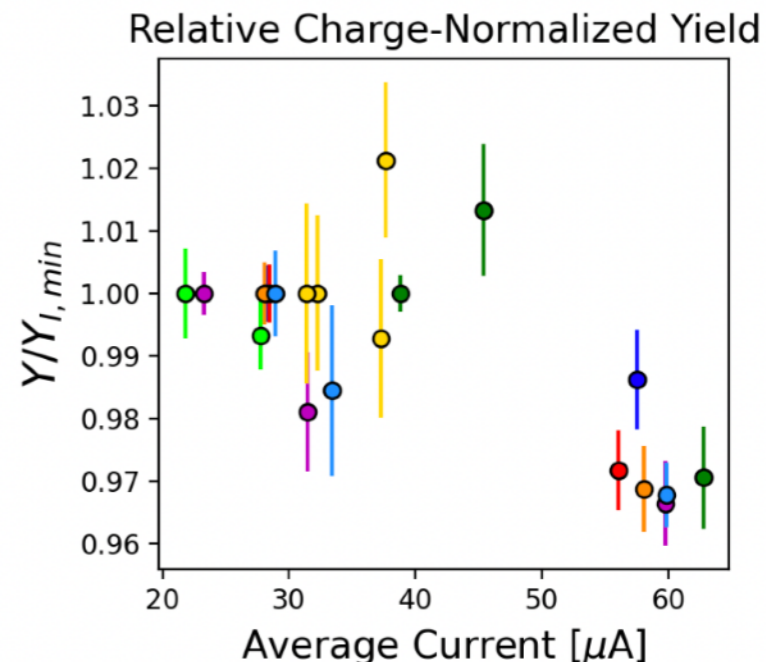
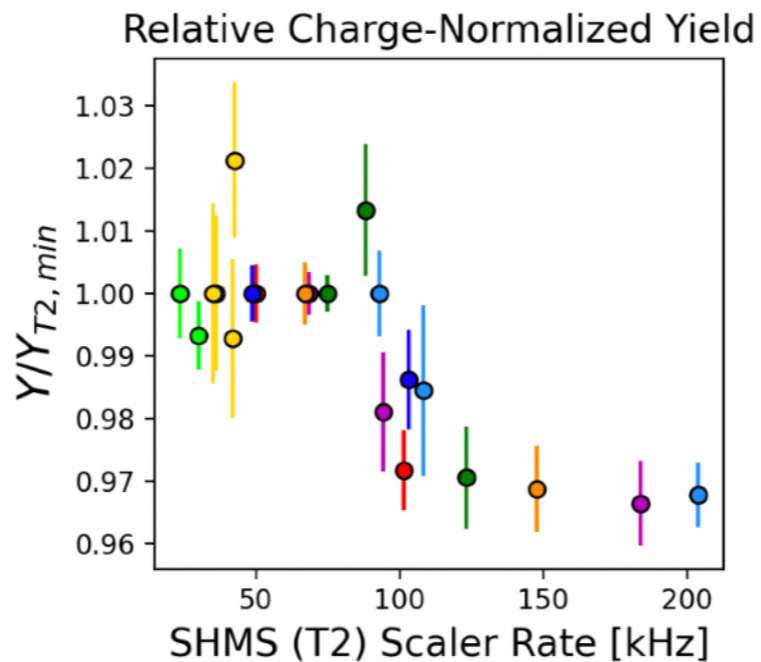
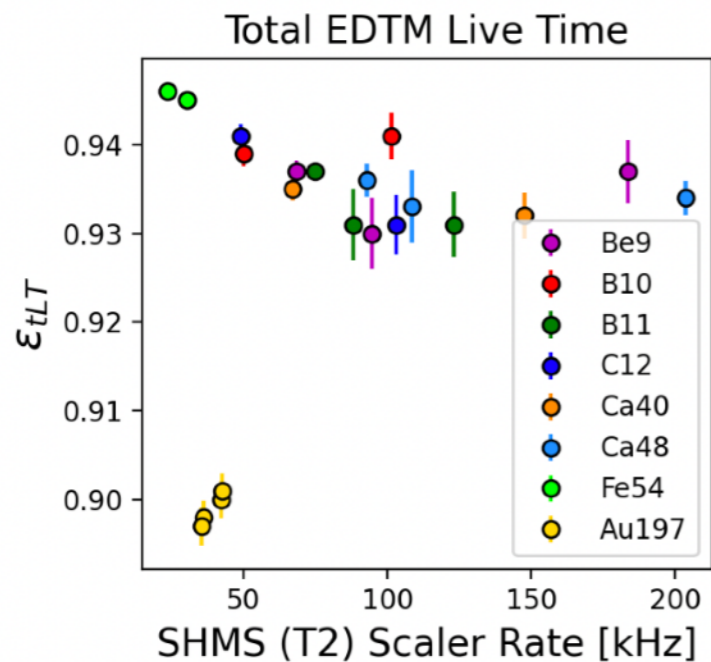
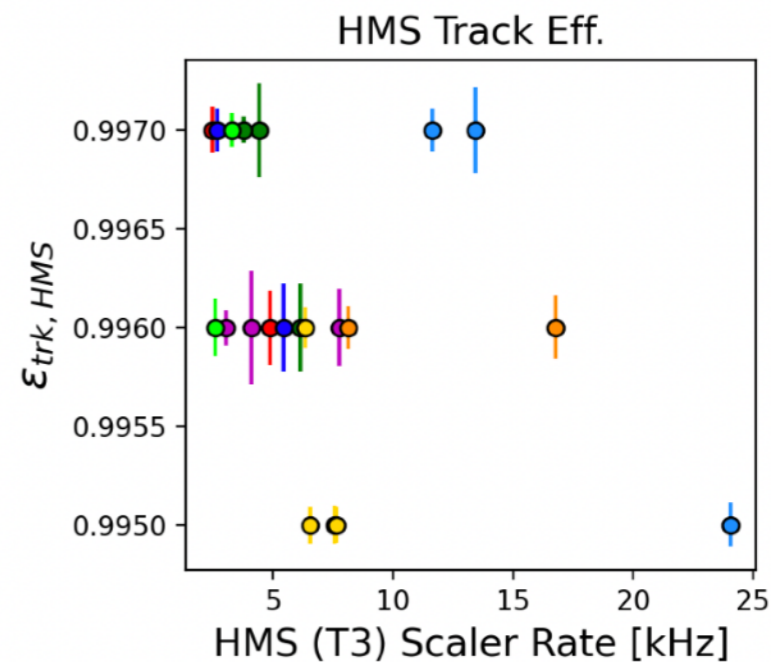
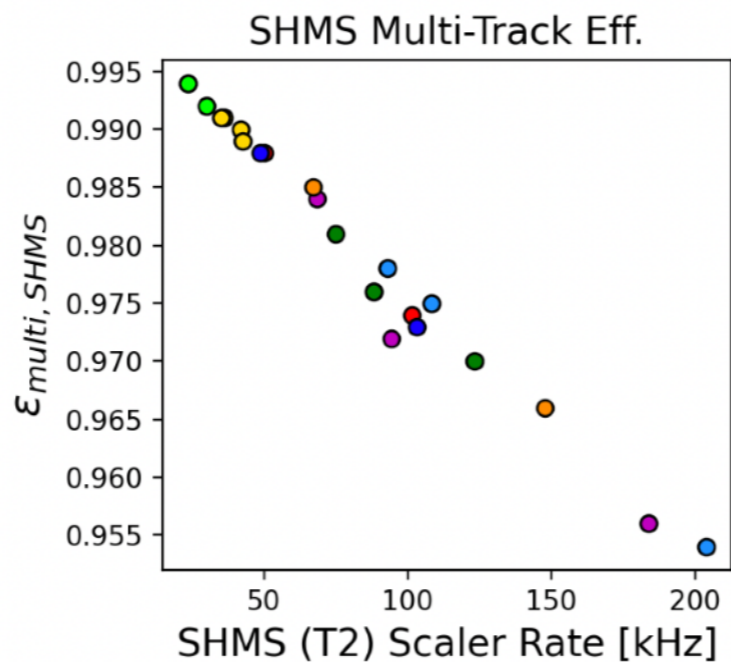
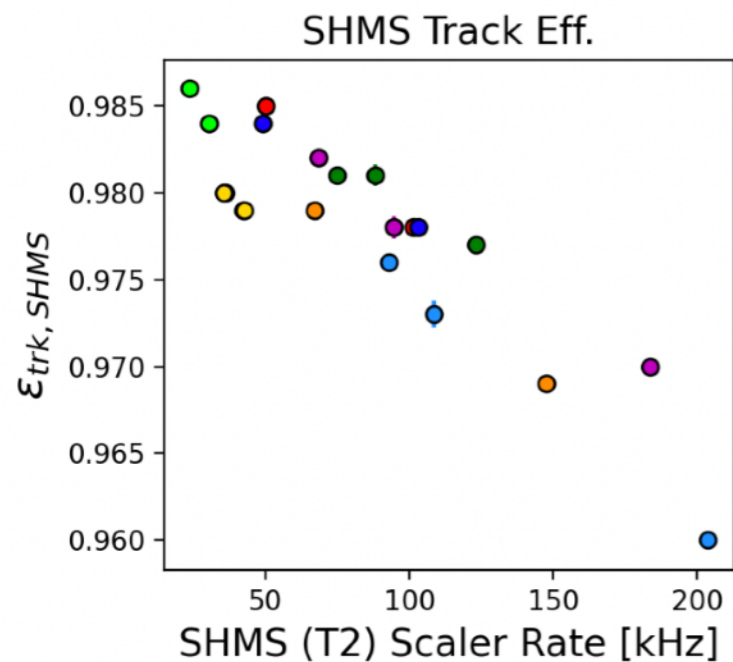


similar trend in decrease of single MF ratios between **data** and **SIMC** (why **NOT** flat ?)

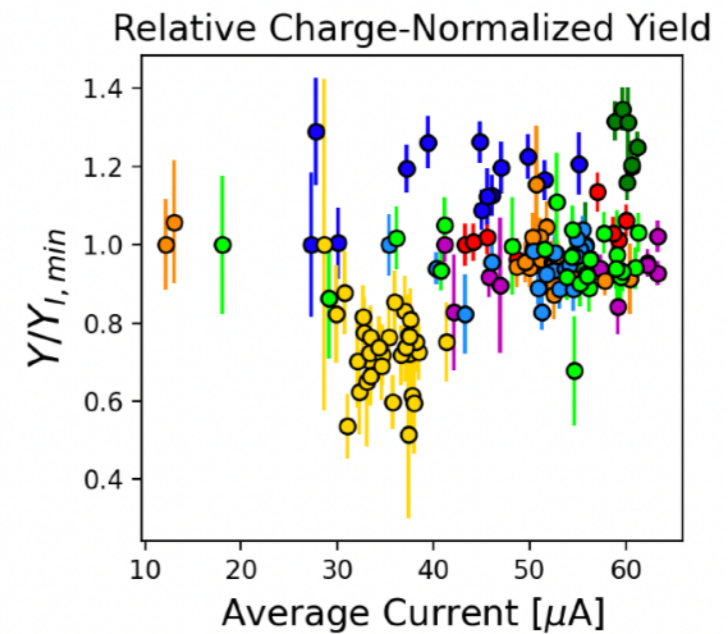
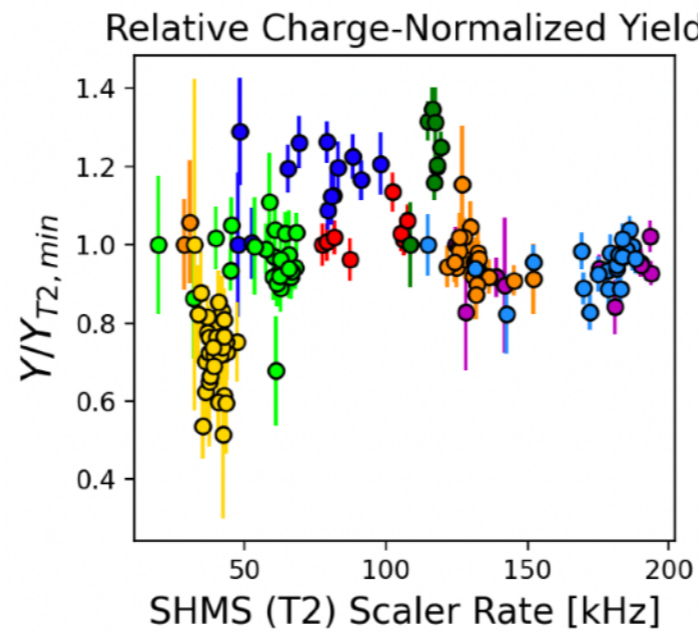
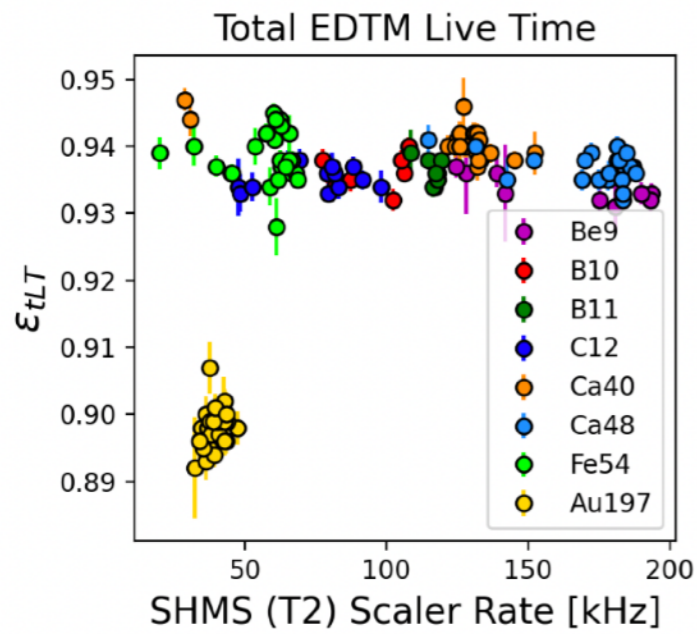
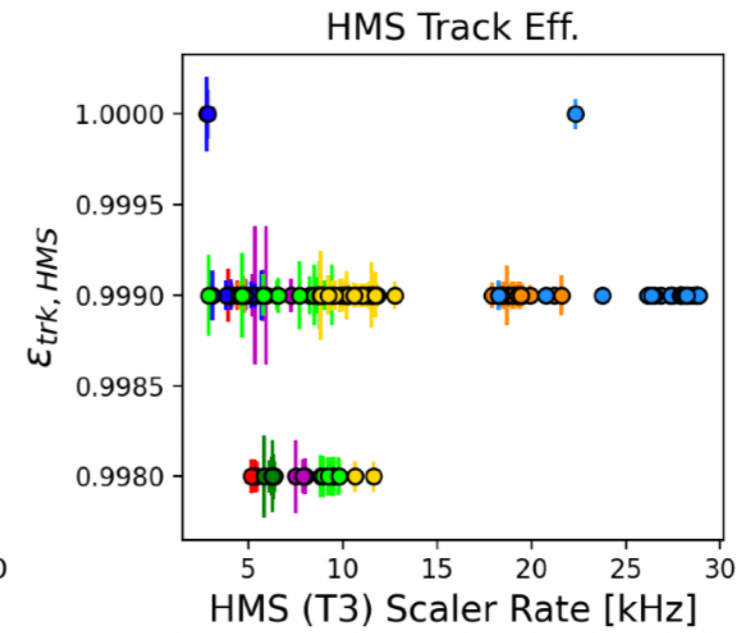
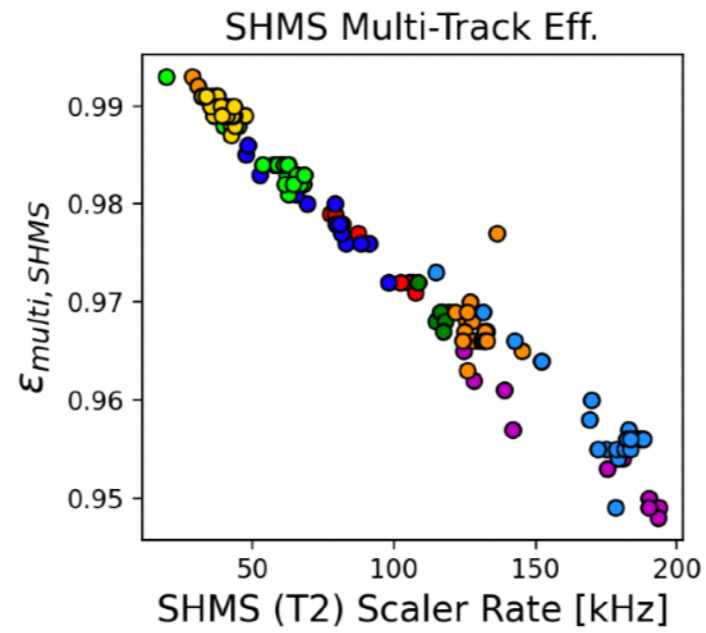
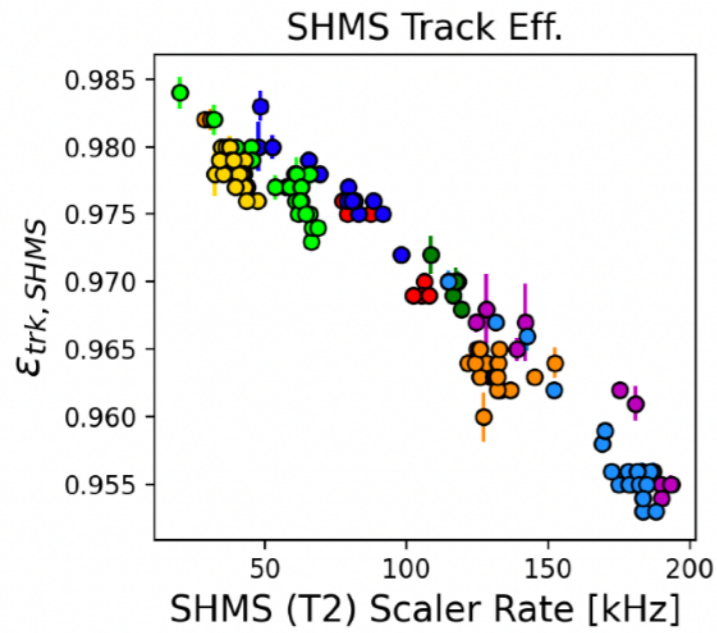
*data: radiative corrections*  
*simc: no radiative effects*

# Corrections and Inefficiencies

# MF Kinematics



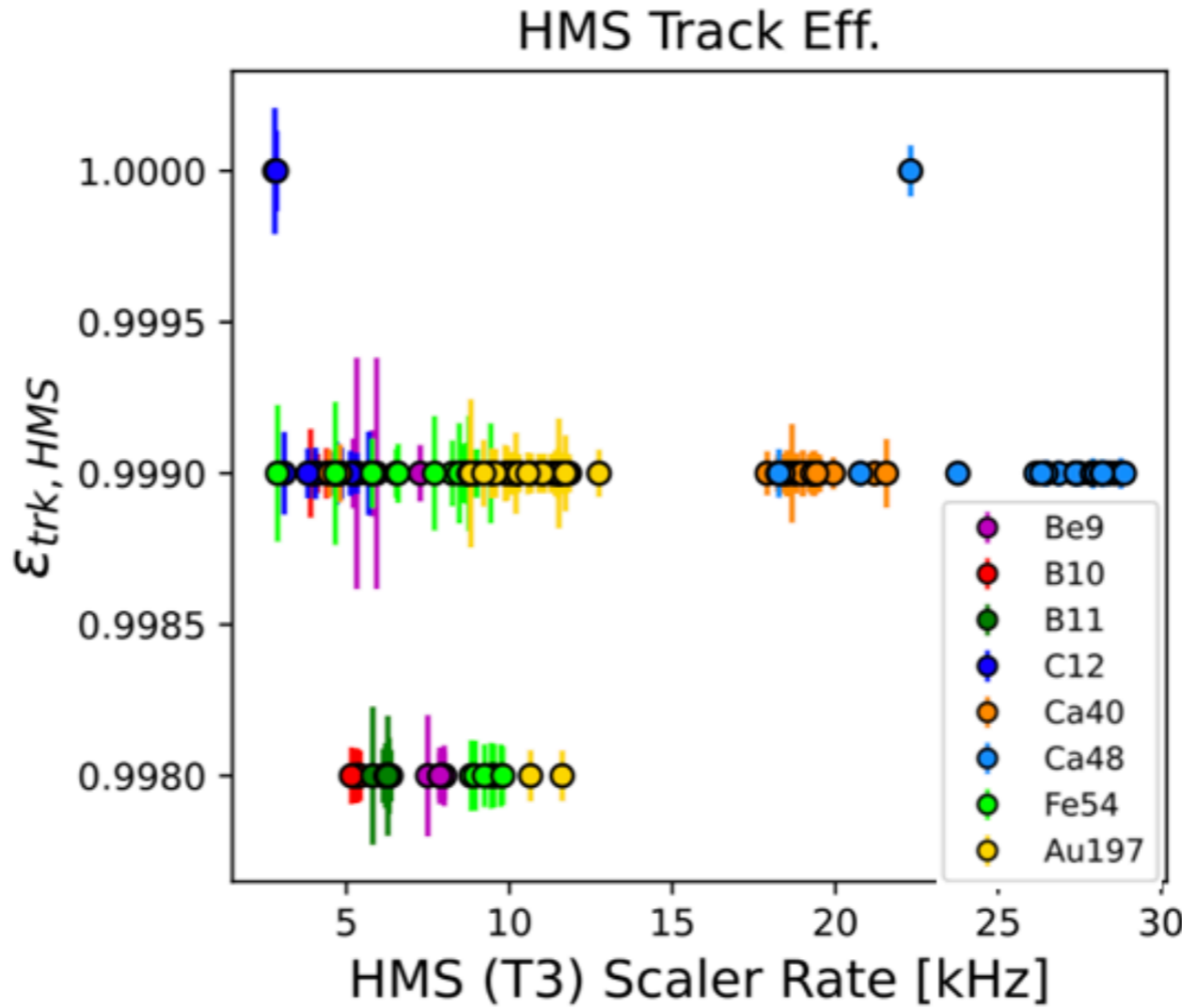
## SRC Kinematics





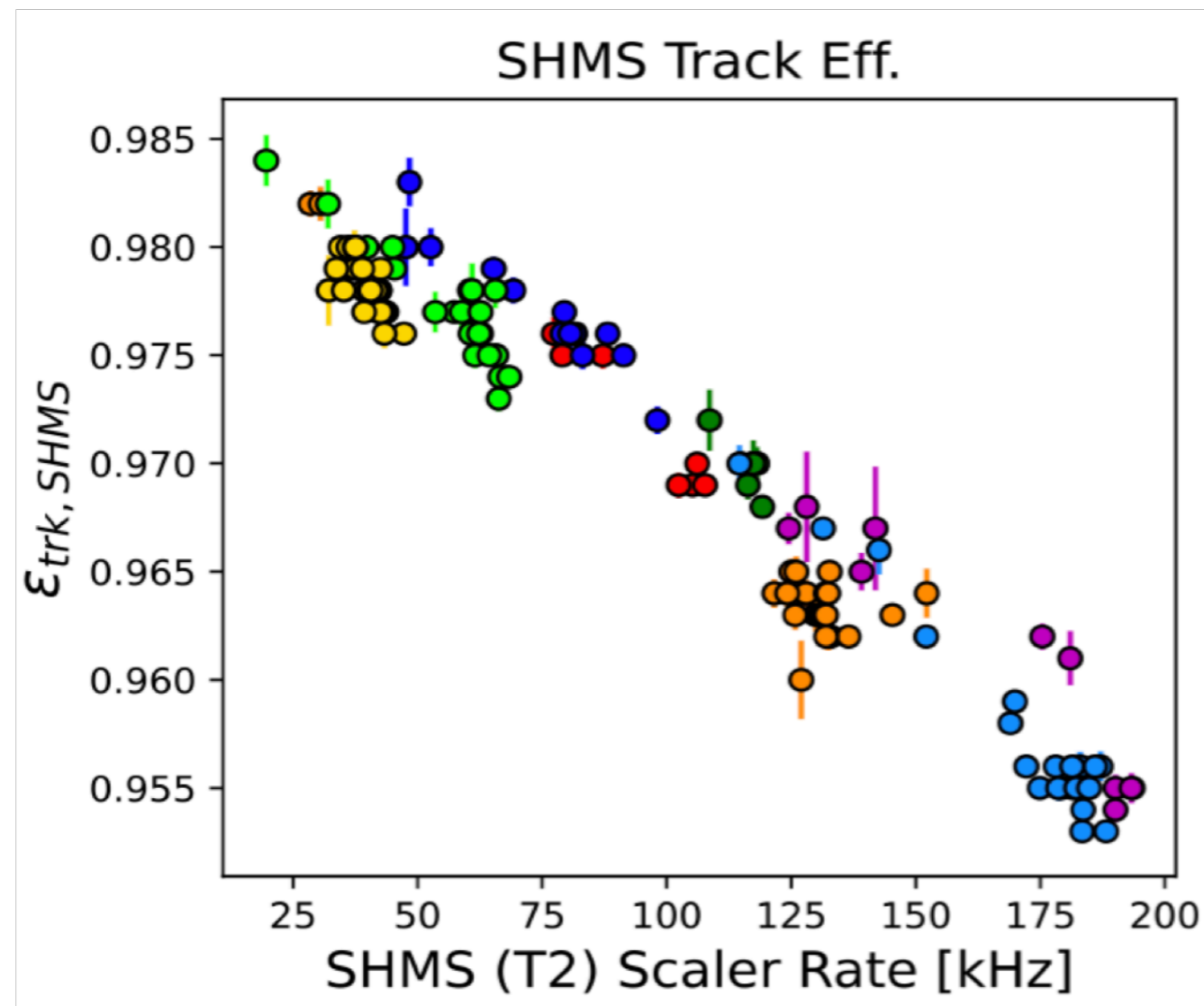
# Yield Extraction

$$Y = \frac{N_{(e,e'p)}}{Q \cdot \epsilon_{htrk} \cdot \epsilon_{etrk} \cdot \epsilon_{mult.trk} \cdot \epsilon_{LT} \cdot T_N \cdot \sigma_{thick}}$$



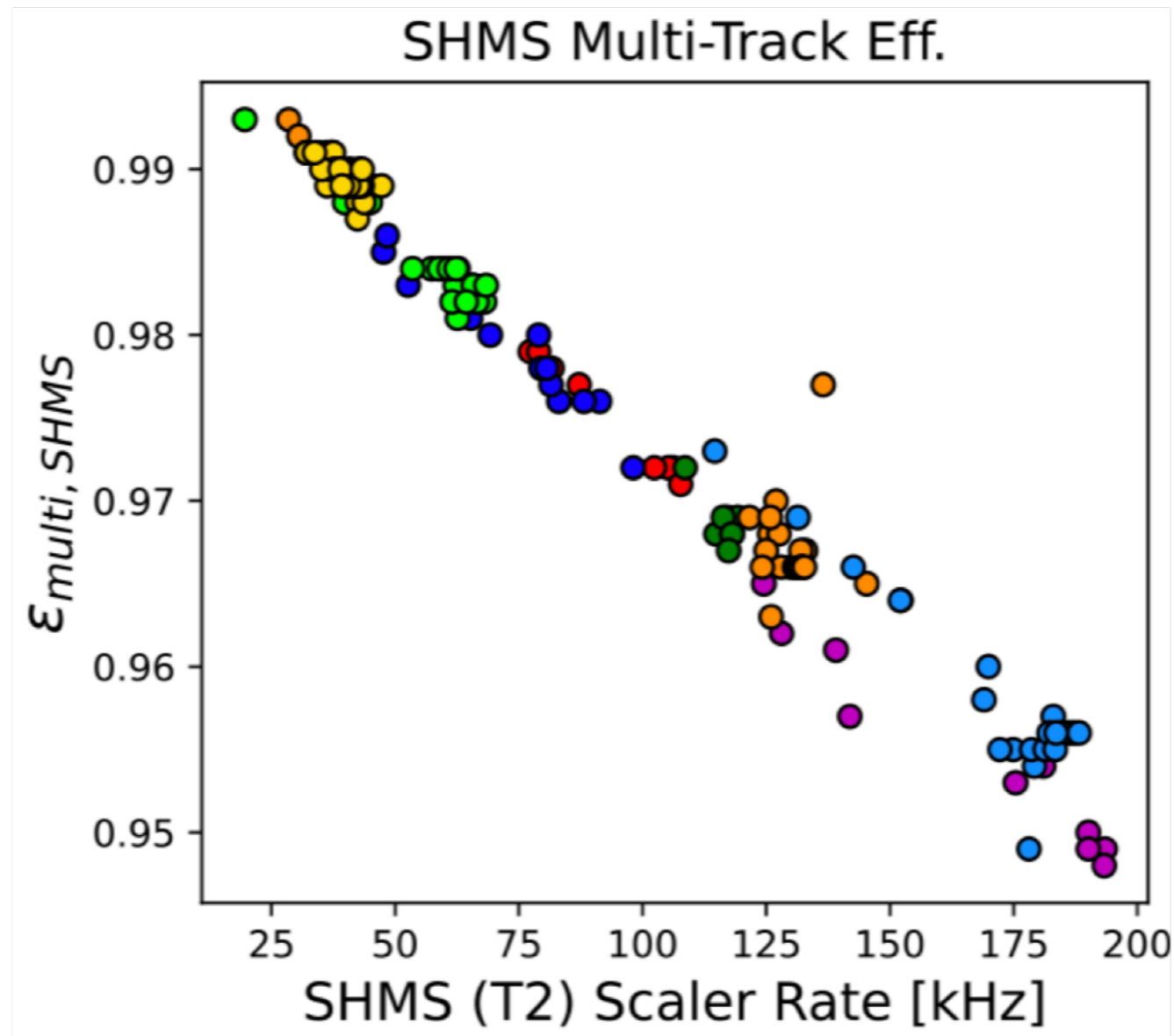
# Yield Extraction

$$Y = \frac{N_{(e,e'p)}}{Q \cdot \epsilon_{htrk} \cdot \epsilon_{etrk} \cdot \epsilon_{mult.trk} \cdot \epsilon_{LT} \cdot T_N \cdot \sigma_{thick}}$$



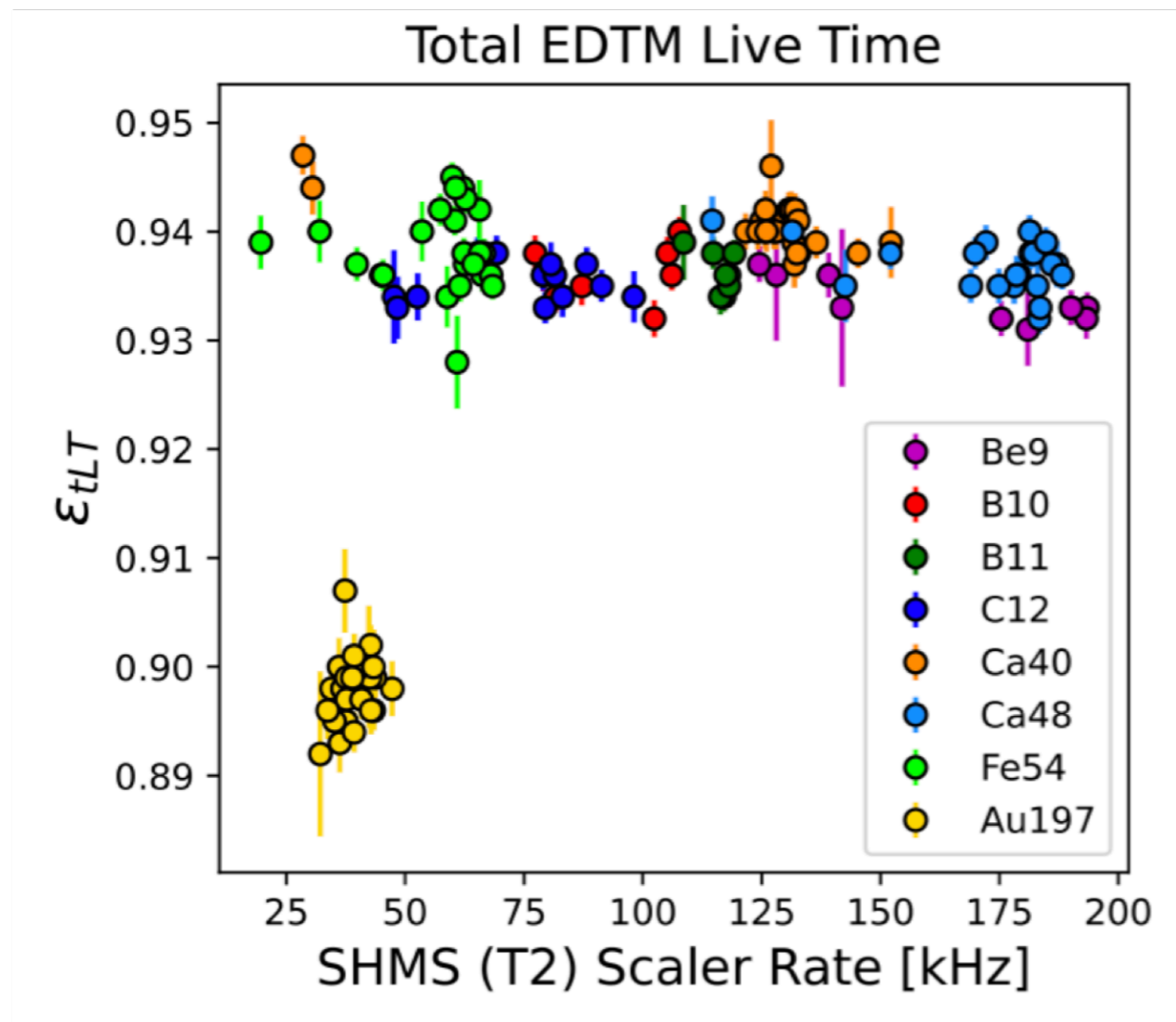
# Yield Extraction

$$Y = \frac{N_{(e,e'p)}}{Q \cdot \epsilon_{htrk} \cdot \epsilon_{etrk} \cdot \epsilon_{mult.trk} \cdot \epsilon_{LT} \cdot T_N \cdot \sigma_{thick}}$$



# Yield Extraction

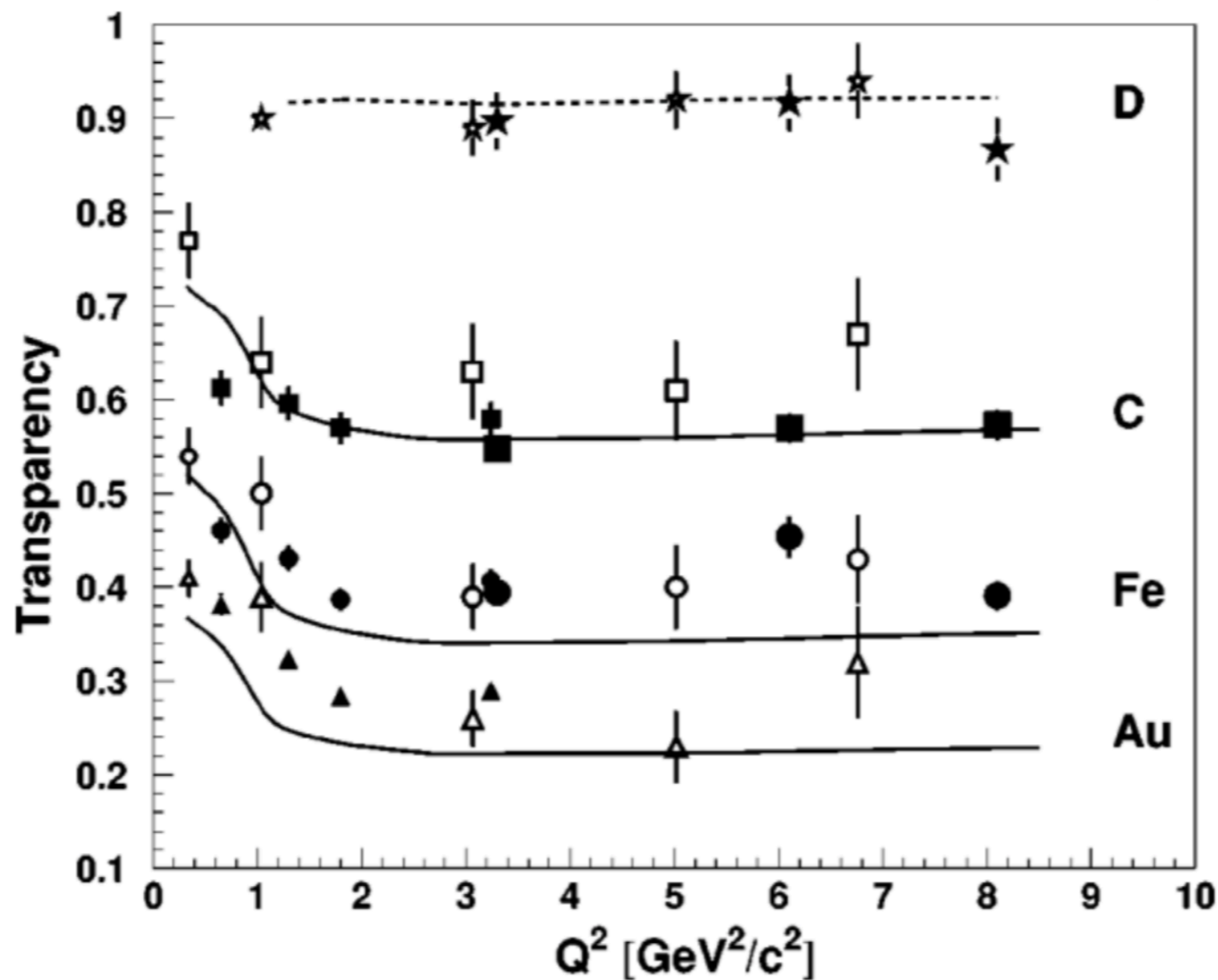
$$Y = \frac{N_{(e,e'p)}}{Q \cdot \epsilon_{htrk} \cdot \epsilon_{etrk} \cdot \epsilon_{mult.trk} \cdot \epsilon_{LT} \cdot T_N \cdot \sigma_{thick}}$$



# Yield Extraction

$$Y = \frac{N_{(e,e'p)}}{Q \cdot \epsilon_{htrk} \cdot \epsilon_{etrk} \cdot \epsilon_{mult.trk} \cdot \epsilon_{LT} \cdot T_N \cdot \sigma_{thick}}$$

K. Garrow *et al.* PHYSICAL REVIEW C **66**, 044613 (2002)



$$T_N = cA^{-\alpha(Q^2)}$$

For  $Q^2 \gtrsim 2\text{GeV}^2$

$$c \rightarrow 1$$

$$\alpha \rightarrow 0.24$$

The IPSM spectral function does not include the effects of short-range nuclear correlations, which move strength to  $|p_m| > p_f$ . The measured  $T$  must be corrected by the ratio of  $\int S d^3 p dE_s$  for the IPSM and correlated spectral functions, integrated over the  $(E_m, p_m)$  range  $\mathcal{R}$ :

$$C_{correl} = \frac{1}{I_{correl}} \int_{\mathcal{R}} dE_s d^3 p S(E_s, \mathbf{p}). \quad (5.7)$$

TABLE 12. Correlation tail correction to the PWIA calculation

$A$	$C_{correl}$
$^1\text{H}, ^2\text{H}$	1.00
$^{12}\text{C}$	$1.11 \pm 0.03$
$^{56}\text{Fe}$	$1.26 \pm 0.08$
$^{197}\text{Au}$	$1.32 \pm 0.08$