A v Leaf: How to Search for Majorana Dynamics at Low-Energy Accelerators

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Based on work in collaboration with Xinshuai Yan (U. Kentucky)



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Fundamental Majorana Dynamics Can exist for electrically neutral massive fermions: either leptons (v's) or combinations of quarks (n's)

Lorentz invariance allows

$$\mathcal{L} = \bar{\psi} i \partial \!\!\!/ \psi - \frac{1}{2} m (\psi^T C \psi + \bar{\psi} C \bar{\psi}^T)$$

[Majorana, 1937]

where m is the Majorana mass.

N.B. a "Majorana neutron" is an entangled n and \overline{n} state

Bibliography:

S.G. & Xinshuai Yan (U. Kentucky), Phys. Rev. D93, 096008 (2016) [arXiv:1602.00693]; S.G. & Xinshuai Yan, Phys. Rev. D97, 056008 (2018) [arXiv:1710.09292]; S.G. & Xinshuai Yan, Phys. Lett. B790 (2019) 421 [arXiv:1808.05288]; and on ongoing work in collaboration with Xinshuai Yan

Why Search for n-n Oscillations?

The Standard Model (SM) cannot explain the origin of the cosmic BAU, dark matter, or dark energy. B violation plays a role in at least one of these puzzles. Although B violation appears in the SM (sphalerons), [Kuzmin, Rubakov, & Shaposhnikov, 1985] we know nothing of its pattern at accessible energies. Do processes occur with $|\Delta B| = 1$ or $|\Delta B| = 2$ or both? The SM conserves B-L, but does Nature? Despite severe limits on $|\Delta B| = 1$ processes, the origin of $|\Delta B|=2$ processes can be completely distinct [Marshak and Mohapatra, 1980; Babu & Mohapatra, 2001 & 2012; Arnold, Fornal, & Wise, 2013] If neutron-antineutron oscillations, e.g., are observed,

then B-L is broken, and we have found physics BSM!



$0\nu \beta\beta$ Decay in Nuclei

Can be mediated by "short-" or "long"-range mechanisms The "short-range" mechanism involves new B-L violating dynamics; e.g.,



S or V that carries B or L

For choices of fermions f_i this decay topology can yield $n-\overline{n}$ or 0ν $\beta\beta$ decay

[Bonnet, Hirsch, Ota, & Winter, 2013]

Can we relate the possibilities in a data-driven way?

[Yes!] [S.G. & Xinshuai Yan, 2019]

Cf. connection via I∆BI=1 process [Babu & Mohapatra, 2015]

Nucleon-Antinucleon Transitions Can be realized in different ways

Enter searches for

• neutron-antineutron oscillations (free n's & in nuclei)

"spontaneous" & thus sensitive to environment

$$\mathcal{M} = \begin{pmatrix} M_n - \mu_n B & \delta \\ \delta & M_n + \mu_n B \end{pmatrix}$$

$$P_{n \to \bar{n}}(t) \simeq \frac{\delta^2}{2(\mu_n B)^2} \left[1 - \cos(2\mu_n B t)\right]$$

- dinucleon decay (in nuclei) (limited by finite nuclear density)
- nucleon-antinucleon conversion (NEW!)
 (mediated by external interactions) [SG & Xinshuai Yan]



Neutron-Antineutron Conversion Different mechanisms are possible

- n-n conversion and oscillation could share
 the same "TeV" scale BSM sources
 - Then the quark-level conversion operators can be derived noting the quarks carry electric charge
- * n-n conversion and oscillation could come from different BSM sources
 - → Indeed different $|\Delta B|=2$ processes could appear (e.g., e⁻ p → e⁺ \overline{p})

NN conversion

Neutron-Antineutron Oscillation
[Rao & Shrock, 1982]

$$(\mathcal{O}_1)_{\chi_1\chi_2\chi_3} = [u_{\chi_1}^{T\alpha}Cu_{\chi_1}^{\beta}][d_{\chi_2}^{T\gamma}Cd_{\chi_2}^{\delta}][d_{\chi_3}^{T\rho}Cd_{\chi_3}^{\sigma}](T_s)_{\alpha\beta\gamma\delta\rho\sigma},$$

 $(\mathcal{O}_2)_{\chi_1\chi_2\chi_3} = [u_{\chi_1}^{T\alpha}Cd_{\chi_1}^{\beta}][u_{\chi_2}^{T\gamma}Cd_{\chi_2}^{\delta}][d_{\chi_3}^{T\rho}Cd_{\chi_3}^{\sigma}](T_s)_{\alpha\beta\gamma\delta\rho\sigma},$
 $(T_s)_{\alpha\beta\gamma\delta\rho\sigma} = \epsilon_{\rho\alpha\gamma}\epsilon_{\sigma\beta\delta} + \epsilon_{\sigma\beta\gamma}\epsilon_{\sigma\alpha\delta} + \epsilon_{\sigma\beta\gamma}\epsilon_{\rho\alpha\delta},$
 $(T_a)_{\alpha\beta\gamma\delta\rho\sigma} = \epsilon_{\rho\alpha\beta}\epsilon_{\sigma\gamma\delta} + \epsilon_{\sigma\alpha\beta}\epsilon_{\rho\gamma\delta}$
Note
 $(T_a)_{\alpha\beta\gamma\delta\rho\sigma} = \epsilon_{\rho\alpha\beta}\epsilon_{\sigma\gamma\delta} + \epsilon_{\sigma\alpha\beta}\epsilon_{\rho\gamma\delta},$
Note
 $(\mathcal{O}_1)_{\chi_1LR} = (\mathcal{O}_1)_{\chi_1RL}, \quad (\mathcal{O}_{2,3})_{LR\chi_3} = (\mathcal{O}_{2,3})_{RL\chi_3},$
 $(\mathcal{O}_2)_{mnn} - (\mathcal{O}_1)_{mnnn} = 3(\mathcal{O}_3)_{mnn}$ [Caswell, Milutinovic, & Senjanovic, 1983]
Only 4 appear in SM effective theory

[Rao & Shrock, 1982]

From Oscillation to Conversion Quark-level operators: compute $q^{\rho}(p) + \gamma(k) \rightarrow \overline{q}^{\delta}(p')$ $\mathcal{H}_{I} \supset \frac{\delta_{q}}{2} \sum_{\mathcal{X}} (\psi_{\chi_{1}}^{\rho T} C \psi_{\chi_{1}}^{\delta} + \bar{\psi}_{\chi_{1}}^{\delta} C \bar{\psi}_{\chi_{1}}^{\rho T}) + Q_{\rho} e \sum_{\chi_{2}} \bar{\psi}_{\chi_{2}}^{\rho} \mathcal{A} \psi_{\chi_{2}}^{\rho}$ matrix element: $\langle \bar{q}^{\delta}(p') | \mathcal{T}\left(\sum_{\alpha} \left(-i\frac{\delta_q}{2}\int d^4x \psi_{\chi_1}^{\rho T} C \psi_{\chi_1}^{\delta}\right)\right)$ $\times \left(-iQ_{\rho}e\int d^{4}y\bar{\psi}^{\rho}_{\chi_{2}}A\psi^{\rho}_{\chi_{2}}-iQ_{\delta}e\int d^{4}y\bar{\psi}^{\delta}_{\chi_{2}}A\psi^{\delta}_{\chi_{2}}\right)\right)$ 🔹 if δ=ρ $\times |q^{\rho}(p)\gamma(k)\rangle,$ **Effective vertex**

B-L Violation via e-n scattering Linking neutron-antineutron oscillation to conversion



B-L Violation via e-n scattering Linking neutron-antineutron oscillation to conversion Moreover...

$$\begin{split} (\tilde{\mathcal{O}}_{1})_{\chi_{1}\chi_{2}\chi_{3}}^{\chi\mu} &= \left[-2[u_{-\chi}^{\alpha\,T}C\gamma^{\mu}\gamma_{5}u_{\chi}^{\beta} + u_{\chi}^{\alpha\,T}C\gamma^{\mu}\gamma_{5}u_{-\chi}^{\beta}][d_{\chi_{2}}^{\gamma\,T}Cd_{\chi_{2}}^{\delta}][d_{\chi_{3}}^{\rho\,T}Cd_{\chi_{3}}^{\sigma}] \\ &+ \left[u_{\chi_{1}}^{\alpha\,T}Cu_{\chi_{1}}^{\beta}][d_{-\chi}^{\gamma\,T}C\gamma^{\mu}\gamma_{5}d_{\chi}^{\delta} + d_{\chi}^{\gamma\,T}C\gamma^{\mu}\gamma_{5}d_{-\chi}^{\delta}][d_{\chi_{3}}^{\rho\,T}Cd_{\chi_{3}}^{\sigma}] \\ &+ \left[u_{\chi_{1}}^{\alpha\,T}Cu_{\chi_{1}}^{\beta}][d_{\chi_{2}}^{\gamma\,T}Cd_{\chi_{2}}^{\delta}][d_{-\chi}^{\rho\,T}C\gamma^{\mu}\gamma_{5}d_{\chi}^{\sigma} + d_{\chi}^{\rho\,T}C\gamma^{\mu}\gamma_{5}d_{-\chi}^{\sigma}] \right] (T_{s})_{\alpha\beta\gamma\delta\rho\sigma} \end{split}$$

yielding [Here χ =R - χ =L for em scattering] $(\tilde{\mathcal{O}}_1)_{\chi_1\chi_2\chi_3}^{\chi} = (\delta_1)_{\chi_1\chi_2\chi_3} \frac{em}{3(p_{\text{eff}}^2 - m^2)} \frac{Qej_{\mu}}{q^2} (\tilde{\mathcal{O}}_1)_{\chi_1\chi_2\chi_3}^{\chi\mu},$

(best connection to oscillation as $q^2 \rightarrow 0$)

with similar relationships for i=2,3 [only these in em case] The hadronic matrix elements are computed in the MIT bag model.

B-L Violation via e-n scattering Linking neutron-antineutron oscillation to conversion

[SG & Xinshuai Yan, arXiv:1710.09292, PRD 2018]

TABLE I. Dimensionless matrix elements $(I_i)_{\chi_1\chi_2\chi_3}^{\chi_3}$ of $n - \bar{n}$ conversion operators. The column "EM" denotes the matrixelement combination of $(\chi = R) - (\chi = L)$.

	I_1				I_2					I_3	
$\chi_1\chi_2\chi_3$	$\chi = R$	$\chi = L$	EM	$\chi_1\chi_2\chi_3$	$\chi = R$	$\chi = L$	EM	$\chi_1\chi_2\chi_3$	$\chi = R$	$\chi = L$	EM
RRR	19.8	19.8	0	RRR	-4.95	-4.95	0	RRR	1.80	-8.28	10.1
RRL	17.3	17.3	0	RRL	-2.00	-9.02	7.02	RRL	-1.07	-8.81	7.74
RLR	17.3	17.3	0	RLR	-4.09	-0.586	-3.50	RLR	7.20	6.03	1.17
RLL	6.02	6.02	0	RLL	-0.586	-4.09	3.50	RLL	6.03	7.20	-1.17
LRR	6.02	6.02	0	LRR	-4.09	-0.586	-3.50	LRR	7.20	6.03	1.17
LRL	17.3	17.3	0	LRL	-0.586	-4.09	3.50	LRL	6.03	7.20	-1.17
LLR	17.3	17.3	0	LLR	-9.02	-2.00	-7.02	LLR	-8.81	-1.07	-7.74
LLL	19.8	19.8	0	LLL	-4.95	-4.95	0	LLL	-8.28	1.80	-10.1

Electromagnetic scattering yields n- \overline{n} conversion from O₂ and O₃ operators only! Interactions impact view on n- \overline{n} osc. even in q² \rightarrow 0 limit; (cf. K_S regeneration in matter); cf. Nesvizhevsky et al 2018.... Neutron-Antineutron Conversion Different mechanisms are possible

- n-n conversion and oscillation could share the same "TeV" scale BSM sources
 Then the quark-level conversion operators can be derived noting the quarks carry electric charge
- n-n conversion and oscillation could come from different BSM sources
 - Here we consider nucleon-antinucleon conversion

Now we turn to minimal scalar models.

Models with $|\Delta B|=2$ Processes Enter minimal scalar models without proton decay [Arnold, Fornal, and Wise, 2013; Dev & Mohapatra, 2015] Already used for $n \rightarrow \bar{n}$ oscillation without p decay [Arnold, Fornal, Wise, PRD, 2013] Note limits on $|\Delta B|=1$ processes are severe! E.g., $\tau(N \rightarrow e^+\pi) = 8.2 \times 10^{33}$ yr [p] @ 90% CL

Add new scalars X_i that do not give N decay at tree level

Also choose X_i that respect SM gauge symmetry and also under interactions $X_iX_jX_k$ or $X_iX_jX_kX_l$ — cf. "hidden sector" searches: possible masses are limited by experiment

Scalars without Proton Decay That also carry B or L charge

TABLE I. Scalar particle representations in the $SU(3)_c \times SU(2)_L \times U(1)_Y$ SM that carry nonzero B and/or L but permit no proton decay at tree level, after Ref. [4]. We indicate the possible interactions between the scalar X and SM fermions schematically. Note that the indices a, b run over three generations, that the symmetry of the associated coupling g_i^{ab} under $a \leftrightarrow b$ exchange is noted in brackets, and finally that our convention for Y is $Q_{em} = T_3 + Y$. Please refer to the text for further discussion.

Scala	ar SM Representation	В	L	Operator(s)	$[g_i^{ab}?]$
X_1	(1, 1, 2)	0	-2	$Xe^{a}e^{b}$	[S]
X_2	(1, 1, 1)	0	-2	$XL^{a}L^{b}$	[A]
X_3	(1,3,1)	0	-2	$XL^{a}L^{b}$	[S]
X_4	$(\bar{6}, 3, -1/3)$	-2/3	0	XQ^aQ^b	[S]
X_5	$(\bar{6}, 1, -1/3)$	-2/3	0	XQ^aQ^b, Xu^ad^b	[A,-]
X_6	(3, 1, 2/3)	-2/3	0	Xd^ad^b	$[\mathbf{A}]$
X_7	$(\overline{6},1,2/3)$	-2/3	0	$X d^a d^b$	[S]
X_8	$(\bar{6}, 1, -4/3)$	-2/3	0	Xu^au^b	[S]
X_9	(3, 2, 7/6)	1/3	-1	$X\bar{Q}^a e^b, XL^a \bar{u}^b$	[,]

Note SU(3) rep'ns

Scalar-fermion couplings

Patterns of $|\Delta B|=2$ Violation? Note possible SM gauge invariant scalar models

[SG & Xinshuai Yan, arXiv: 1808.05288]

TABLE II. Minimal interactions that break B and/or L from scalars X_i that do not permit $|\Delta B| = 1$ interactions at tree level, indicated schematically, with the Hermitian conjugate implied. Interactions labelled M1-M9 appear in models 1-9 of Ref. [4]. Interactions A-G possess $|\Delta L| = 2$, $|\Delta B| = 0$. M19, M20, and M21 follow from M8, M17, and M18 under $X_7 \rightarrow X_6$, respectively, but they do not involve firstgeneration fermions only.

	Model		Model	Mo	del	-"4 X"	models
$\overline{\mathbf{N}}$	M1	$X_5 X_5 X_7$	А	$X_1 X_8 X_7^{\dagger}$ M10	$X_7 X_8 X_8 X_1$		
0-0	M2	$X_4 X_4 X_7$	В	$X_3 X_4 X_7^{\dagger}$ M1	$1 X_5 X_5 X_4 X_3$	^s can	yield
	M3	$X_7 X_7 X_8$	C	$X_3 X_8 X_4^{\dagger}$ M12	$2 X_5 X_5 X_8 X_1$	L	
	M4	$X_6 X_6 X_8$	D	$X_5 X_2 X_7^{\dagger}$ M13	$3 X_4 X_4 X_5 X_2$	• e p	→e⁻p
	M5	$X_5 X_5 X_5 X_2$	Ε	$X_8 X_2 X_5^{\dagger}$ M1	$4 X_4 X_4 X_5 X_3$	∎ }	•
	M6	$X_4 X_4 X_4 X_2$	\mathbf{F}	$X_2 X_2 X_1^{\dagger}$ M1	$5 X_4 X_4 X_8 X_1$		
	M7	$X_4 X_4 X_4 X_3$	G	$X_3 X_3 X_1^{\dagger}$ M1	$5 X_4 X_7 X_8 X_3$, e p	
	M8	$X_7 X_7 X_7 X_1^{\dagger}$		M1'	$7 X_5 X_7 X_7 X_2^{\dagger}$	2	
	M9	$X_6 X_6 X_6 X_1^{\dagger}$		M18	$X_4 X_7 X_7 X_3$	- 3	

π⁻π⁻→e⁻e⁻

Patterns of IABI=2 Violation? Note possible BNV processes

[SG & Xinshuai Yan, arXiv: 1808.05288]

TABLE III. Suite of $|\Delta B| = 2$ and $|\Delta L| = 2$ processes generated by the models of Table II, focusing on states with first-generation matter. The (*) superscript indicates that a weak isospin triplet of $|\Delta L| = 2$ processes can appear, namely $\pi^0 \pi^0 \to \nu \nu$ and $\pi^- \pi^0 \to e^- \nu$. Models M7, M11, M14, and M16 also support $\nu n \to \bar{n}\bar{\nu}$, revealing that cosmic ray neutrinos could potentially mediate a $|\Delta B| = 2$ effect.

$n\bar{n}$	$\pi^-\pi^- ightarrow e^-e^-$	$e^- p \to \bar{\nu}_{\mu,\tau} \bar{n}$	$e^-p ightarrow \bar{\nu}_e \bar{n}/e^+ \bar{p}$	$e^-p \to e^+ \bar{p}$
M1	А	M5	Μ7	M10
M2	$\mathrm{B}^{(*)}$	M6	M11	M12
M3	$\mathrm{C}^{(*)}$	M13	M14	M15
			M16	

Use observations of $n\bar{n}$ oscillation or NN conversion (e⁻ p \rightarrow e⁺ \bar{p} , ...) to establish new scalars... & w/ both can predict the existence of $\pi^{-}\pi^{-}\rightarrow$ e⁻e⁻!



Connecting $|\Delta B| = 2$ to $|\Delta L| = 2...$



Patterns of $|\Delta B| = 2$ Violation Discovery implications for 0v ßß decay

TABLE IV. Possible patterns of $|\Delta B| = 2$ discovery and their interpretation in minimal scalar-fermion models. Note that only $n - \bar{n}$ oscillations and $e^-n \rightarrow e^-\bar{n}$ break B-L symmetry and that the pertinent conversion processes can be probed through electron-deuteron scattering. The latter are distinguished by the electric charge of the final-state lepton accompanying nucleon-antinucleon annihilation. Note that the $0\nu\beta\beta$ query refers specifically to the existence of $\pi^-\pi^- \rightarrow e^-e^-$ from new, short-distance physics. Note that we can possibly establish model D and $|\Delta L| = 2$ violation, but that model does not give rise to $\pi^-\pi^- \rightarrow e^-e^-$. In contrast we cannot establish X_8 alone and thus cannot establish model C.

Model	$n\bar{n}?$	$e^-n \rightarrow e^-\bar{n}?$	$e^- p \to \bar{\nu}_X \bar{n}?$	$e^- p \rightarrow e^+ \bar{p}?$	0 uetaeta ?
M3	Y	Ν	Ν	Y	Y [A]
M2	Υ	Υ	Y	Y	Y[B]
M1	Υ	Υ	Υ	Ν	? [D]
_	Ν	Ν	Y	Y	? [C?]

Note high-intensity, low-energy e-scattering facilities (P2, e.g.) can be used to broader purpose

[SG & Xinshuai Yan, arXiv: 1808.05288]

Phenomenology of New Scalars Constraints from many sources — Focus on first generation

i) **n-n** (But this does not impact M7) ii) Collider constraints

[Grossman, Ng, & Ray, 2018]

But beware galactic magnetic fields!

CMS: I+I+ search; cannot look at invariant masses below 8 GeV [CMS 2012, 2014, 2016]



Low-Energy Electron Facilities Illustrative parameter choices have been made [Hydrogen]

	Facility	Be	am	Τ	Luminosity	
	raciiity	Energy(MeV)	Current (mA)	Length (cm)	Density (g/cm^3)	(cm^{-2})
}	CBETA $[14]$	150	40	60	0.55×10^{-6}	2.48×10^{36}
2	MESA $[15]$	100	10	60	0.55×10^{-6}	6.21×10^{35}
M	ADIFI [16]	50	10	100	0.09×10^{-3}	1.69×10^{38}
X		50	10	* 0.2	71.3×10^{-3}	2.68×10^{38}
in	FAST [17]	150	28.8	100	0.09×10^{-3}	4.88×10^{38}
		100	20.0	* 0.1	71.3×10^{-3}	3.87×10^{38}

*Liquid

- 💫 = ERL (e.g.)

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- ⅔ = Linac (external target)
- = Linac, ILC test accelerator

Event Rates Select particular scalar masses/couplings for reference Rates in #/yr M'_{1,3} = 3.5 GeV, else 2.5 GeV

M12M14Facility M7M10 M11 M15M16 0.010 0.001 0.001 CBETA [14] 0.076 0 0.053 0.006 MESA [15] 0.001 0.007 0.010 0.0 0.0 0 0.0010.107 0.014 0.007 0 0.558 |0.065|0.800 ARIEL [16] 0.170 0.022 0.011 1.268 0 0.884 0.104 14.908 1.998 0.259 0.124 0 10.398 1.217 FAST [17]11.810 1.583 0.205 0.098 8.238 0.964 0

 $e^- p \rightarrow e^+ p$:

e ⁻	р –	→Ve	n
		• •	; • •

N.B. conversion processes (also pertinent to $0\nu\beta\beta$) are discoverable

[SG & Xinshuai Yan, in preparation]

 $M_i' \equiv M_i / [g_i^{11}]^{1/2}$

Facility	M7	M11	M14	M16
CBETA $[14]$	0.087	0.007	0	0.006
MESA [15]	0.011	0.001	0	0.001
ARIEL [16]	0.801	0.060	0	0.056
	1.270	0.096	0	0.088
FAST [17]	17.045	1.285	0	1.181
	13.503	1.018	0	0.935

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Summary

- The discovery of B-L violation would reveal the existence of dynamics beyond the Standard Model
- The energy scale of B-L violation speaks to different explanations as to why the neutrino is light — a "short range" mechanism could also generate B-L violation in the quark sector
- We have noted neutron-antineutron (& nucleon-antinucleon conversion!) conversion, i.e., neutron-antineutron transitions as mediated by an external current (as via scattering)
- We have used minimal scalar models to relate IΔBI=2 to IΔLI=2 processes
- Experiments with intense low-energy electron beams, e.g., complement essential neutron studies to help solve the v mass puzzle

Backup Slides

B-L Violation via e-d scattering What sorts of limits could be set?

Matching relation: $\eta \bar{v}(\mathbf{p}', s') C \mathbf{j} \gamma_5 u(\mathbf{p}, s) = \frac{em}{3(p_{\text{eff}}^2 - m^2)} \frac{ej_{\mu}}{q^2}$ $\times \langle \bar{n}_q(\mathbf{p}', \mathbf{s}') | \int \mathbf{d}^3 \mathbf{x} \sum_{\mathbf{i}, \chi_1, \chi_2, \chi_3} '(\delta_{\mathbf{i}})_{\chi_1, \chi_2, \chi_3} [(\tilde{\mathcal{O}}_{\mathbf{i}})_{\chi_1, \chi_2, \chi_3}^{\mathrm{R}\,\mu} - (\tilde{\mathcal{O}}_{\mathbf{i}})_{\chi_1, \chi_2, \chi_3}^{\mathrm{L}\,\mu}] |\mathbf{n}_q(\mathbf{p}, \mathbf{s})\rangle$ The best limits come from small-angle scattering

— using the uncertainty principle to estimate θ_{min}

Sensitivity estimate for a beam energy of 20 MeV:

$$|\tilde{\delta}| \lesssim 2 \times 10^{-15} \sqrt{\frac{N \text{ events}}{1 \text{ event}}} \sqrt{\frac{1 \text{ yr}}{t}} \sqrt{\frac{0.6 \times 10^{17} \text{ s}^{-1}}{\phi}} \sqrt{\frac{1 \text{ m}}{L}} \sqrt{\frac{5.1 \times 10^{22} \text{ cm}^{-3}}{\rho}} \text{ GeV}.$$

B-L Violation via n-d scattering What sorts of limits could be set?

For cold neutrons (as at the ILL)

 $|\boldsymbol{p}_n| = 1.94 \text{ keV}$

Sensitivity estimate (set by n-e scattering):

$$|\tilde{\delta}| \lesssim 3 \times 10^{-19} \sqrt{\frac{N \text{ events}}{1 \text{ event}}} \sqrt{\frac{1 \text{ yr}}{t}} \sqrt{\frac{1.7 \times 10^{11} \text{ s}^{-1}}{\phi}} \sqrt{\frac{1 \text{ m}}{L}} \sqrt{\frac{5 \times 10^{22} \text{ cm}^{-3}}{\rho}} \text{ GeV}$$

for the Majorana mass of the neutron

The combination of e and n beam experiments should offer a powerful crosscheck

Cross Section Estimate Experimental limits can be translated to scalar-mass-coupling "sensitivity" plots $\sigma \sim 1.5 \times 10^{-4} |g_4^{11}|^6 |\lambda_7|^2 |g_3^{11}|^2 \left(\frac{5 \text{ GeV}}{M_{X_4}}\right)^{12} \left(\frac{1 \text{ GeV}}{M_{X_3}}\right)^4 \text{ ab}$

[SG & Xinshuai Yan, arXiv: 1808.05288]

Visible with "DarkLight" (FEL JLab) parameters [Babu & Macesanu, 2003; Hanneke, Fogwell, Gabrielse, 2008]

N.B. survives direct limits: (g-2)_e; observed H-atom stability

Constraints from muonium-antimuonium osc.; $|\Delta F|=2$ mixing removed by generation-dependent couplings