

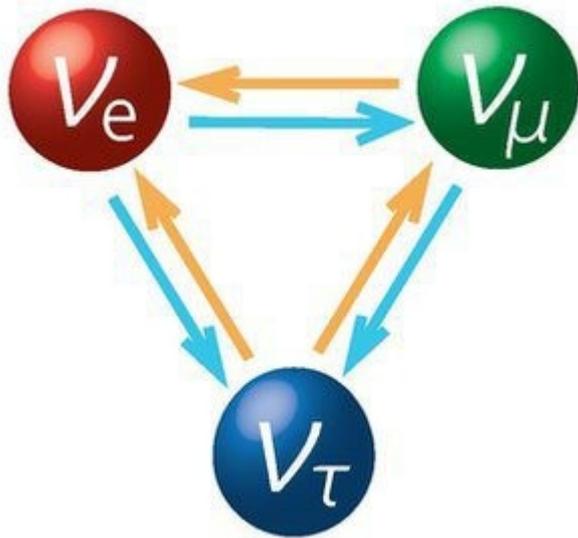
Global analysis of neutrino oscillation experiments

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NuFACT 2018

Blacksburg, August 16th 2018

Neutrino oscillations



Parametrization of the mixing matrix

- Neutrino oscillation probability is given by

$$P(\alpha \rightarrow \beta; E, L) = \sum_{k,j} U_{\alpha k}^* U_{\beta k} U_{\alpha j} U_{\beta j}^* e^{i \frac{\Delta m_{kj}^2}{2E} L}$$

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- For a given energy E and distance L the probability depends on:
 - Two mass splittings Δm_{21}^2 , Δm_{31}^2
 - The entries of the matrix U

Parametrization of the mixing matrix

- The mixing matrix can be parametrized as

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

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- There are also two more majorana phases, but oscillation experiments are blind to them
- Different types of experiments are sensitive to different parameters

Experiment	Dominant parameters	Sub-dominant parameters
Solar Experiments + LBL reactors	$\theta_{12}, \Delta m_{21}^2$	θ_{13}
Short baseline Reactors	$\theta_{13}, \Delta m_{31}^2$	$\theta_{12}, \Delta m_{21}^2$
Atmospheric experiments	$\theta_{23}, \Delta m_{31}^2$	θ_{13}, δ
LBL accelerator disappearance	$\theta_{23}, \Delta m_{31}^2$	θ_{13}
LBL accelerator appearance	θ_{13}, δ	θ_{23}

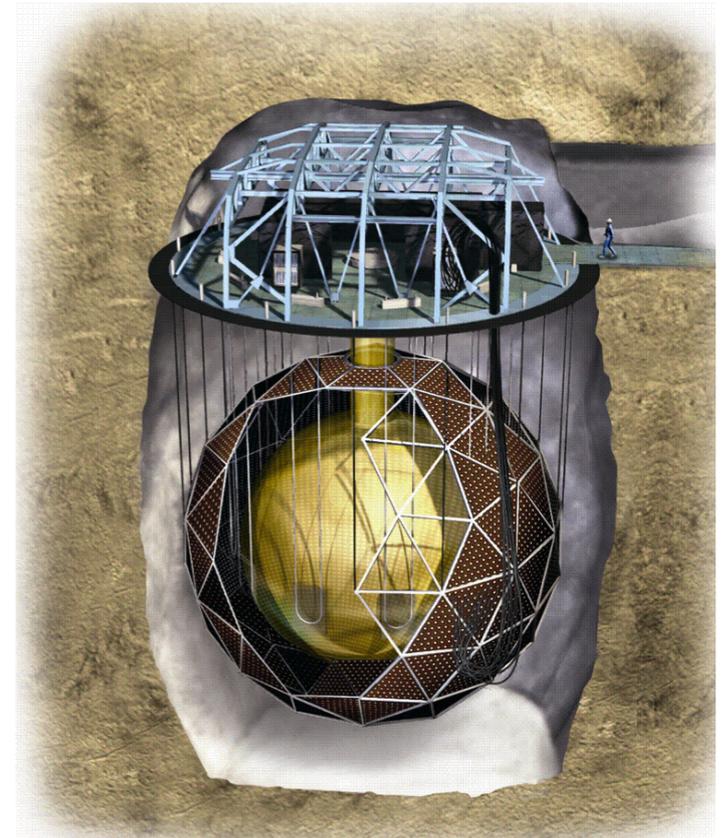
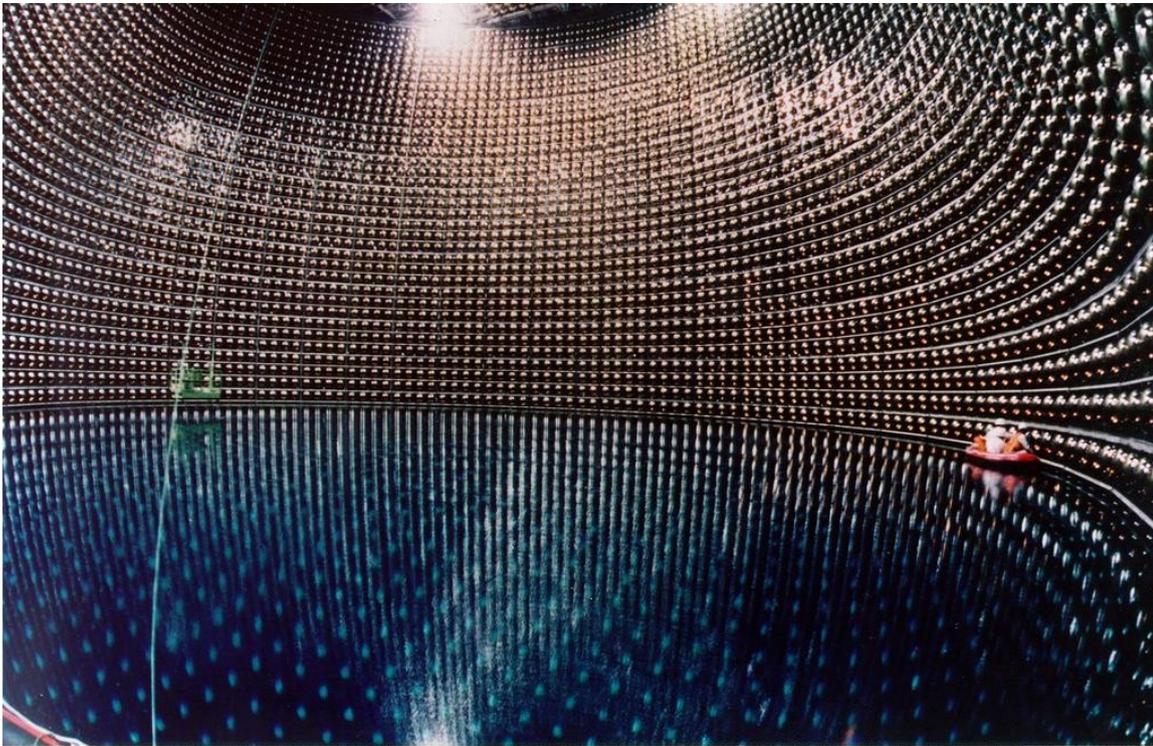
Global fit to neutrino oscillations

Phys.Lett. B782 (2018) 633-640, P.F. de Salas, D.V. Forero, CAT, M. Tórtola, J.W.F. Valle

<https://globalfit.astroparticles.es/>

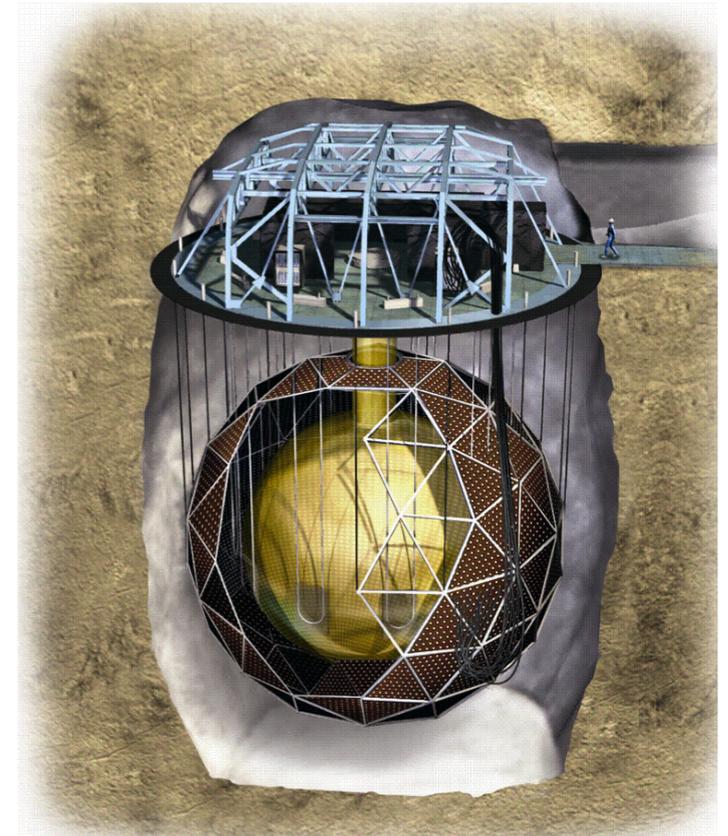
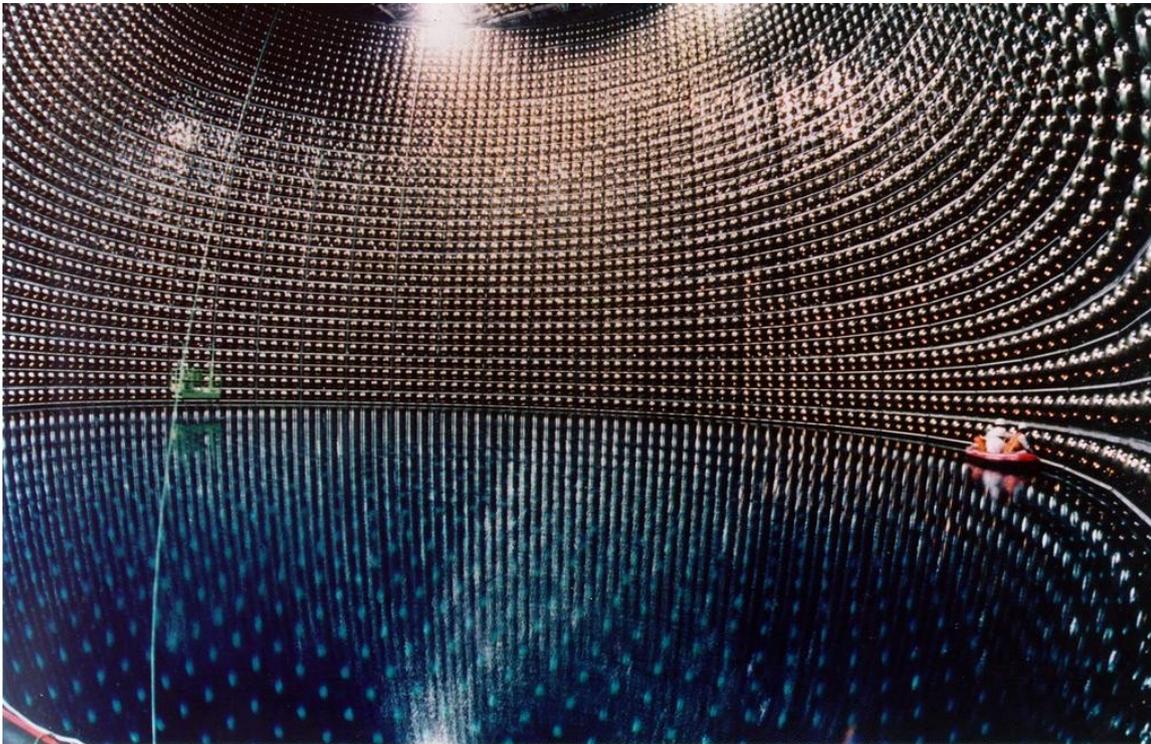
Global fit to neutrino oscillations

- Solar experiments measure disappearance (P_{ee}) and conversion (P_{ex}) of electron neutrinos created in the sun



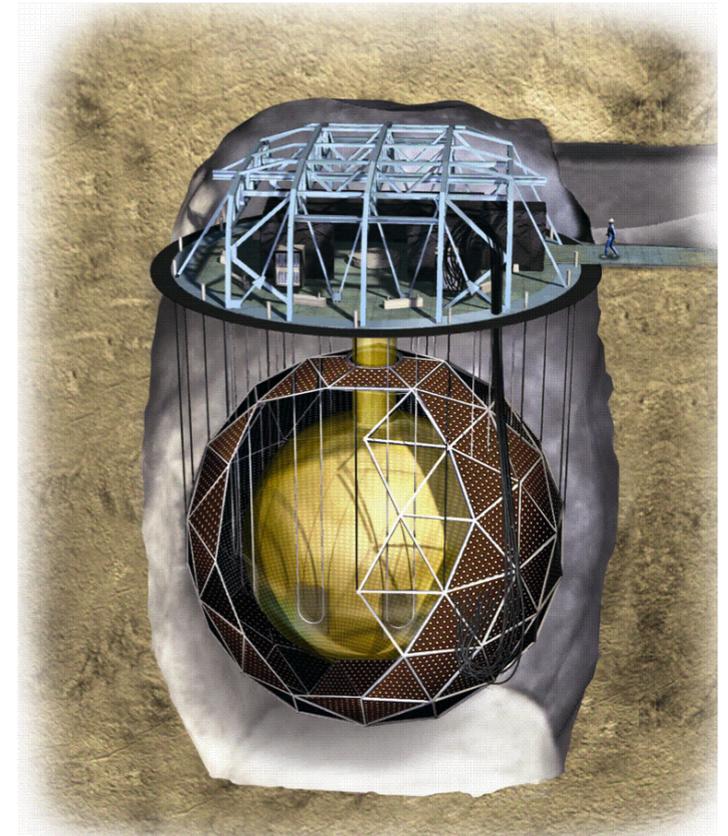
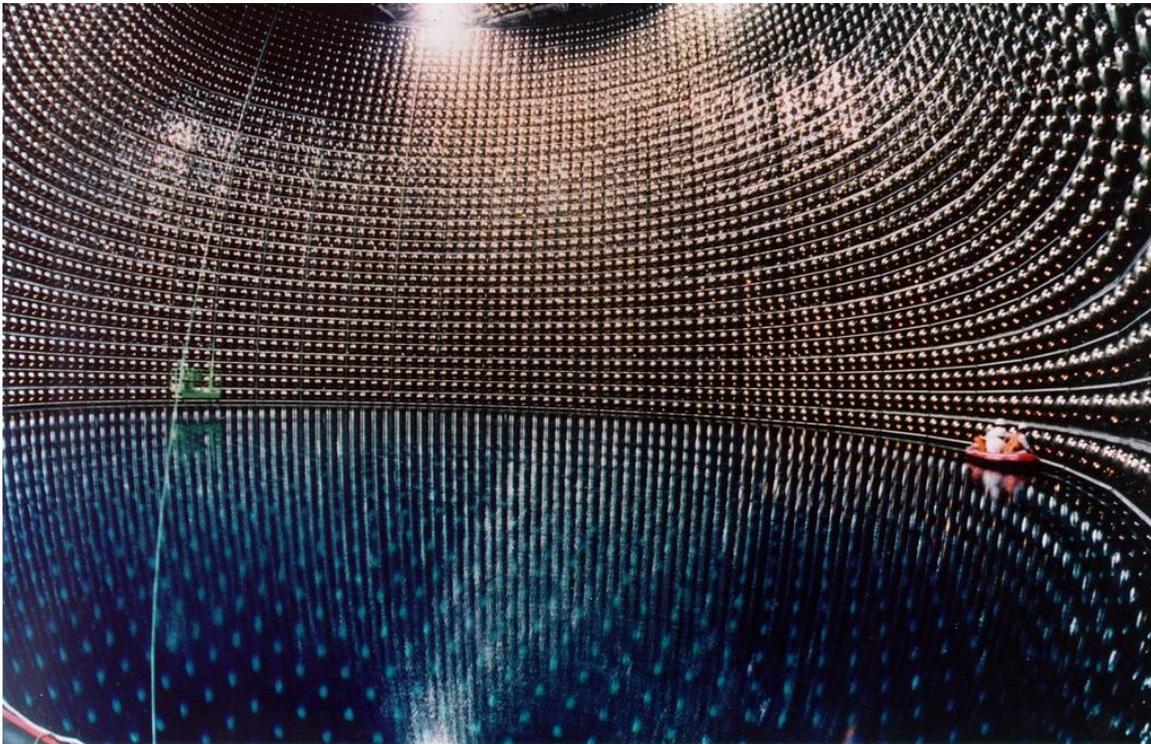
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Global fit to neutrino oscillations

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- The solar parameters are measured also by the long baseline reactor experiment KamLAND

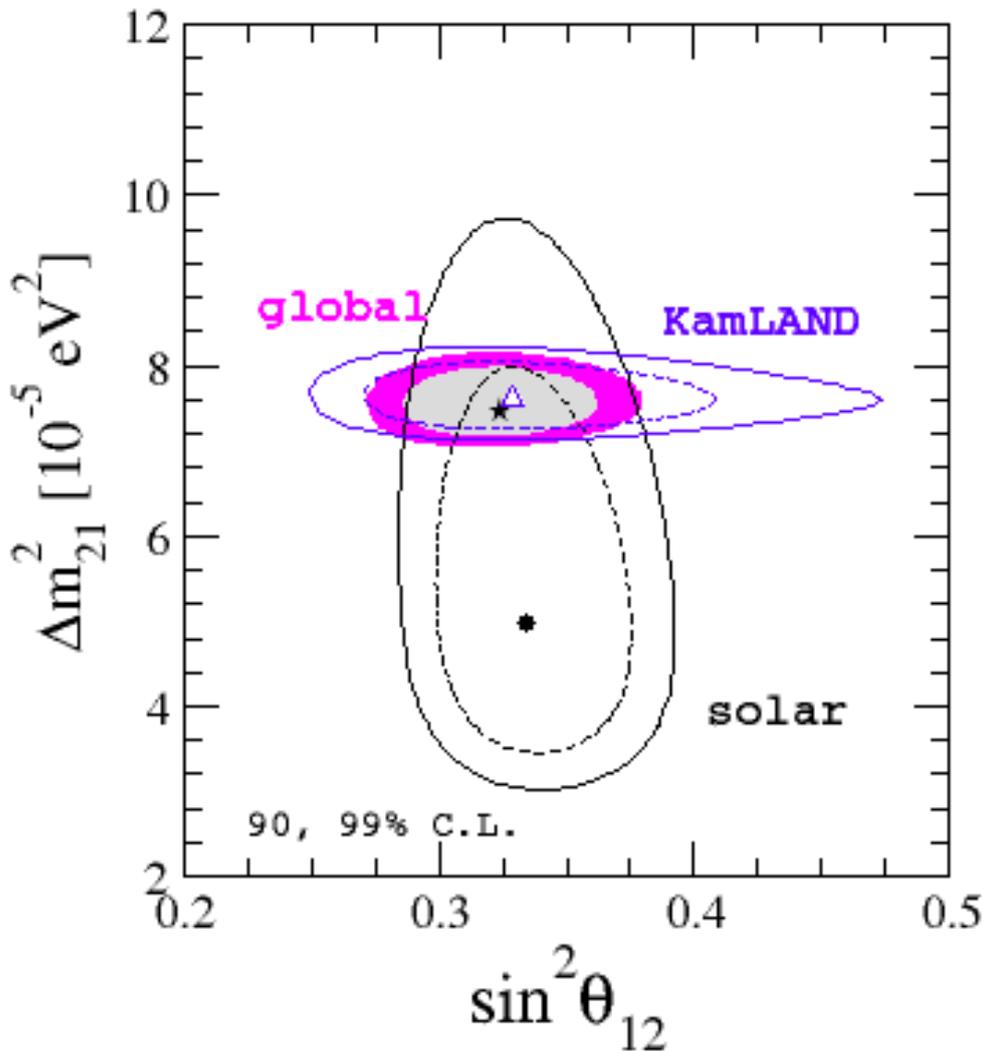


Global fit to neutrino oscillations

- Data included:
 - SK I-IV
 - Borexino: Beryllium data
 - SNO I-III
 - Sage
 - Gallex+GNO
 - Chlorine
 - KamLAND

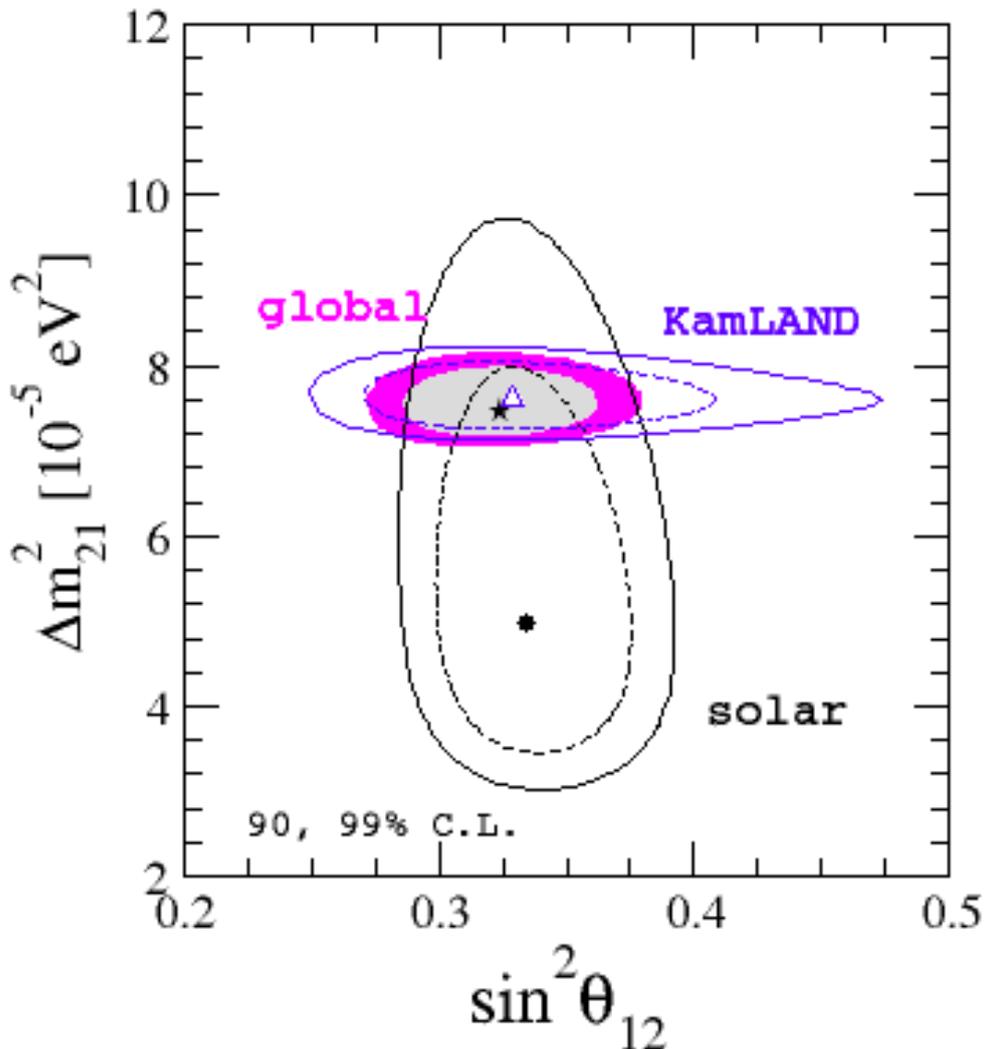
Global fit to neutrino oscillations

- Result of solar experiments and KamLAND



Global fit to neutrino oscillations

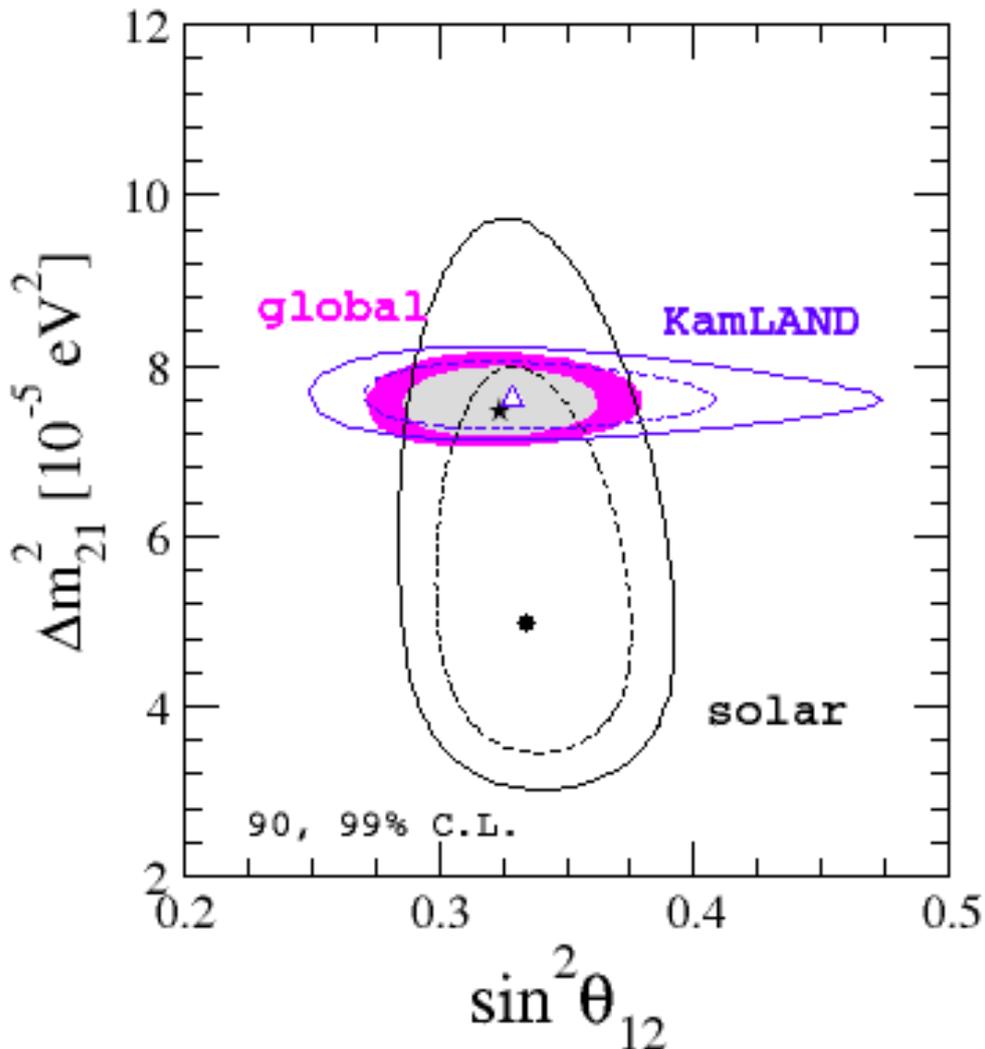
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- θ_{12} better measured by solar data

Global fit to neutrino oscillations

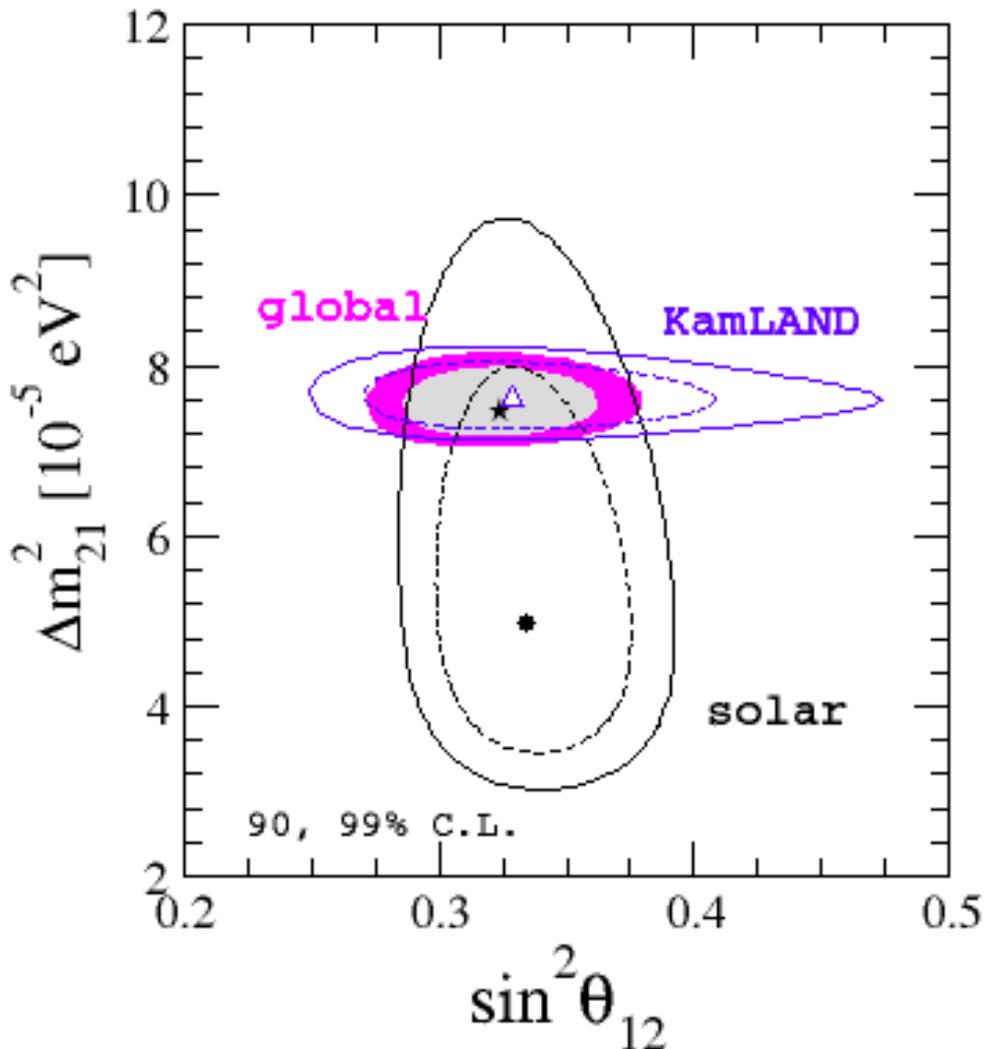
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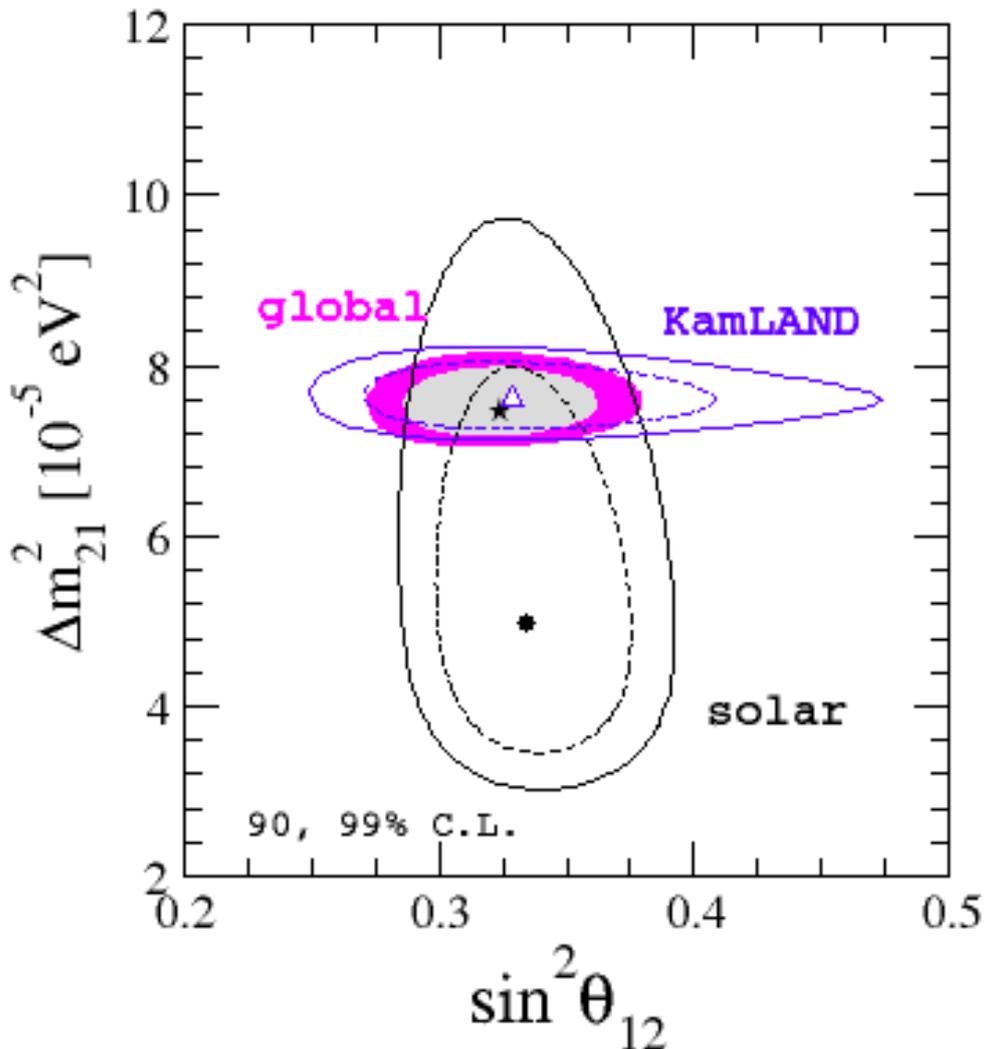
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Global fit to neutrino oscillations

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- θ_{12} better measured by solar data
- Δm_{21}^2 better measured by KamLAND
- Maximal mixing is highly disfavored
- Mismatch between solar and KamLAND data for mass splitting

Global fit to neutrino oscillations

- Reactor experiments measure disappearance of electron antineutrinos ($P_{\bar{e}e}$) created at reactors



Global fit to neutrino oscillations

- Reactor experiments measure disappearance of electron antineutrinos ($P_{\bar{e}\bar{e}}$) created at reactors
- The main dependence of short baseline reactors is on θ_{13} and Δm_{31}^2



Global fit to neutrino oscillations

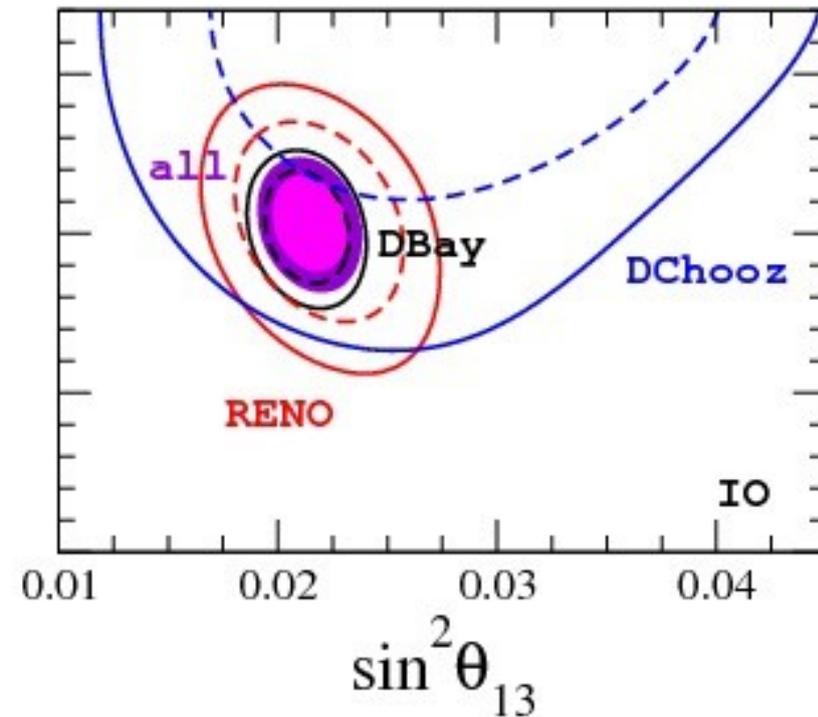
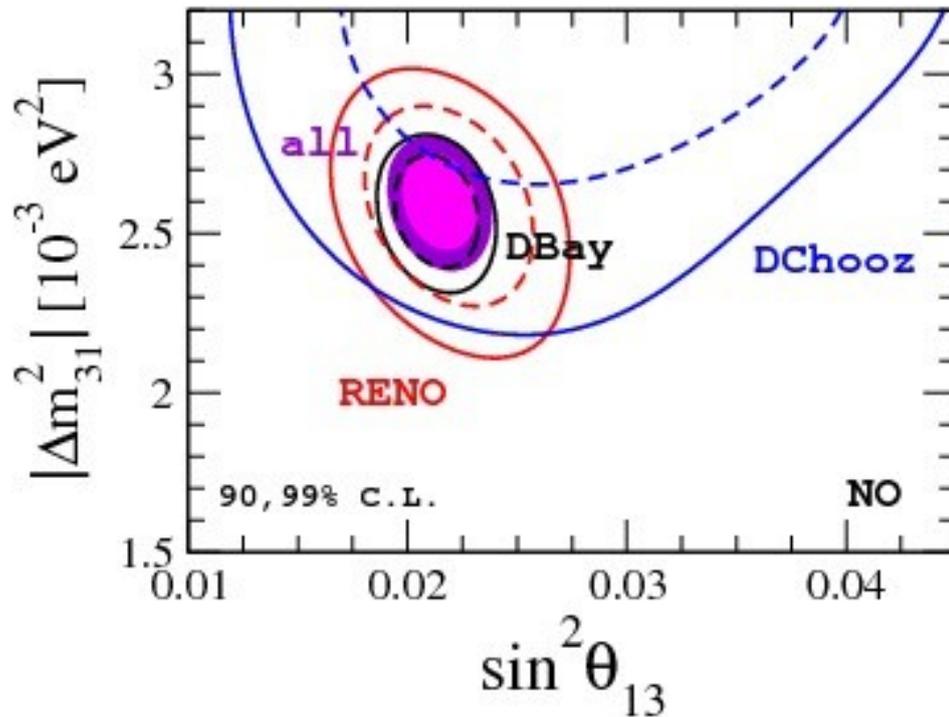
- Data included:
 - 1230 day Daya Bay spectrum
 - 1500 day RENO spectrum
 - 461 day (FI) and 212 day (FII) Double Chooz spectrum

Global fit to neutrino oscillations

- Data included:
 - 1230 day Daya Bay spectrum
 - 1500 day RENO spectrum
 - 461 day (FI) and 212 day (FII) Double Chooz spectrum
- Older reactors are not included, because they only provide upper limits on θ_{13}

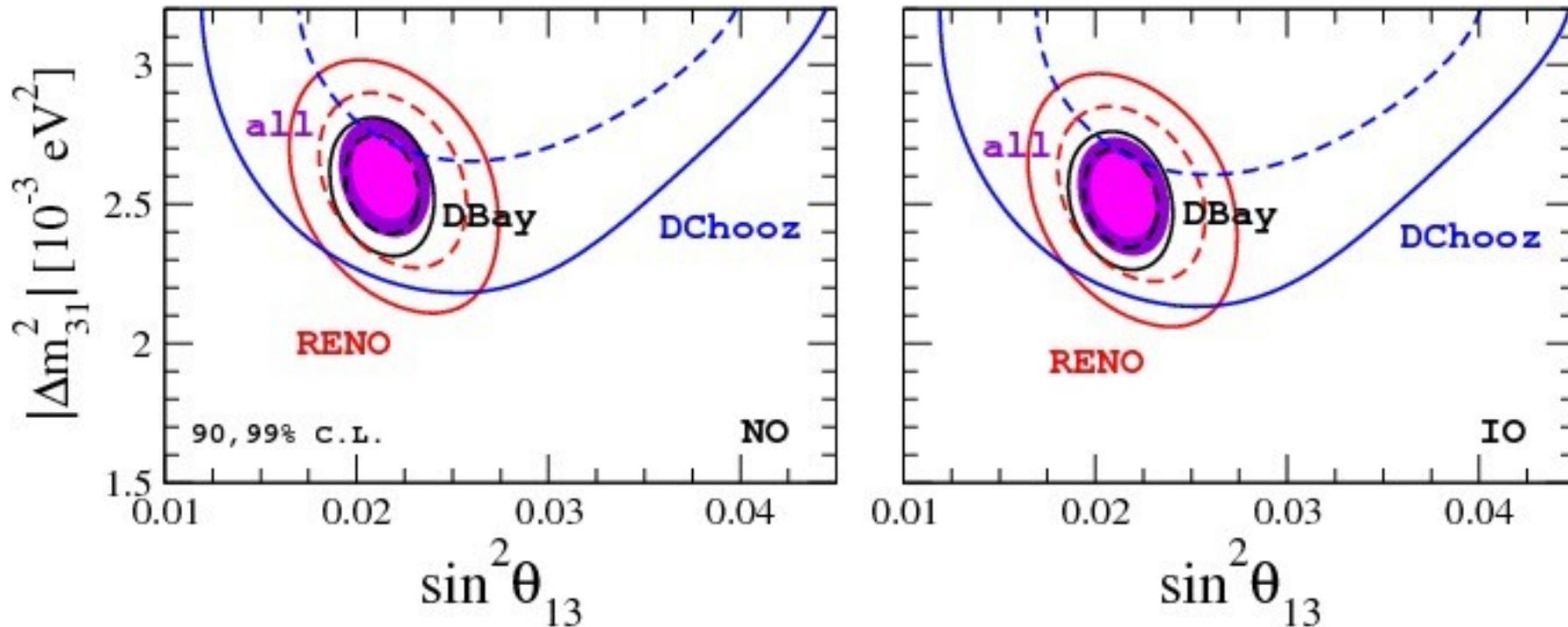
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Global fit to neutrino oscillations

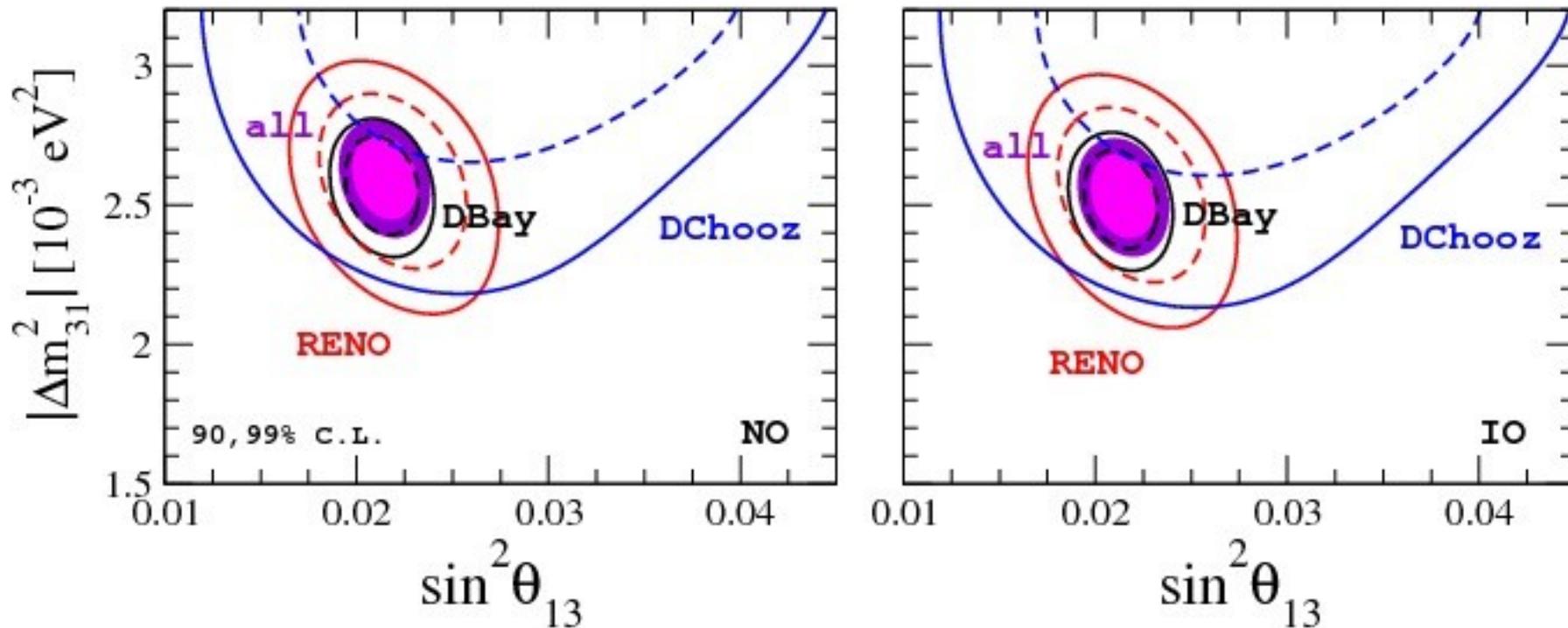
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- Reactor analysis is dominated by Daya Bay

Global fit to neutrino oscillations

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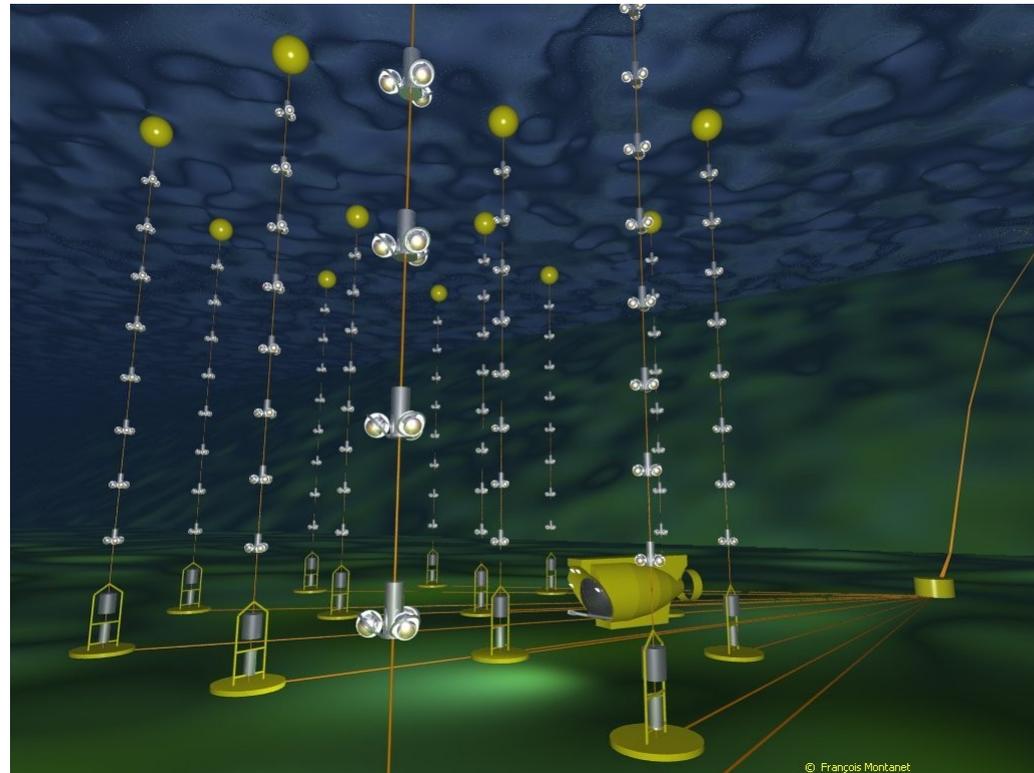
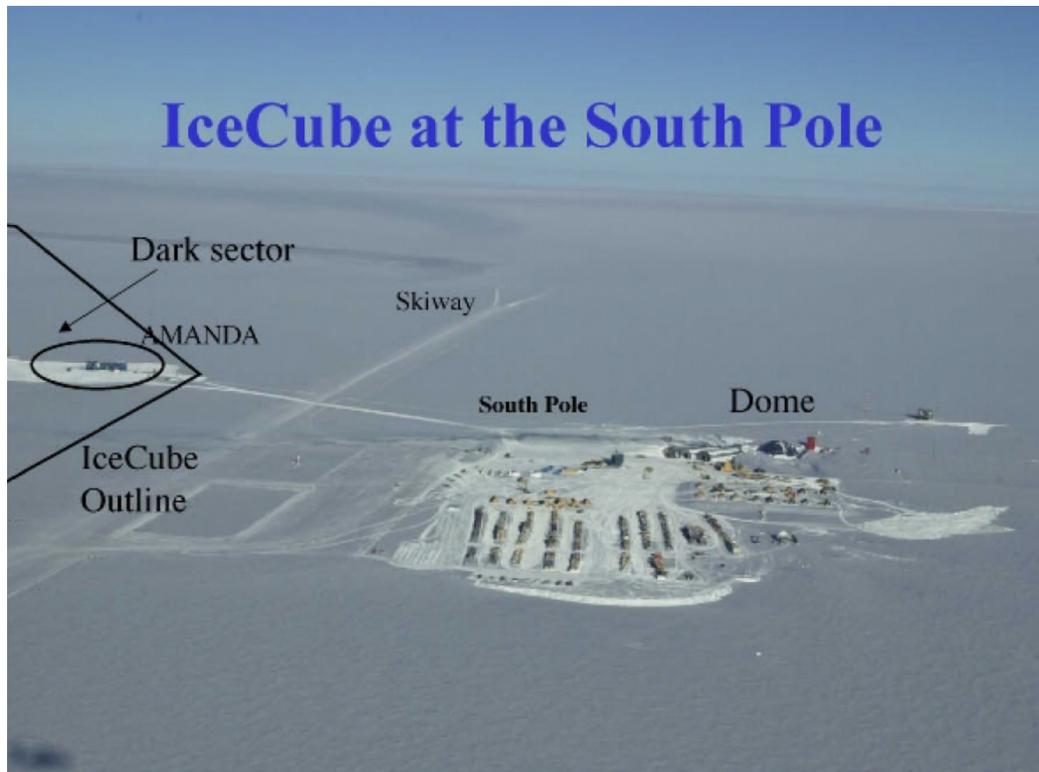


- Reactor analysis is dominated by Daya Bay
- RENO starts being competitive

Global fit to neutrino oscillations

- Atmospheric neutrino experiments are mostly focused on the disappearance of muon neutrinos ($P_{\mu\mu}$) and antineutrinos ($P_{\bar{\mu}\bar{\mu}}$) created in the atmosphere

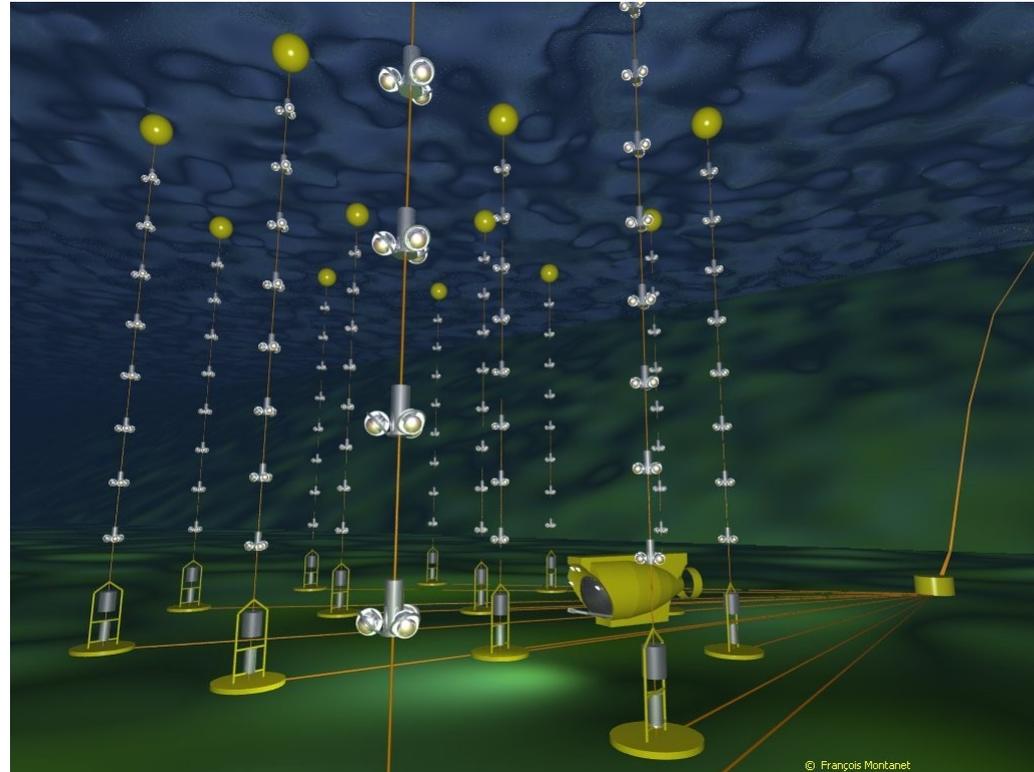
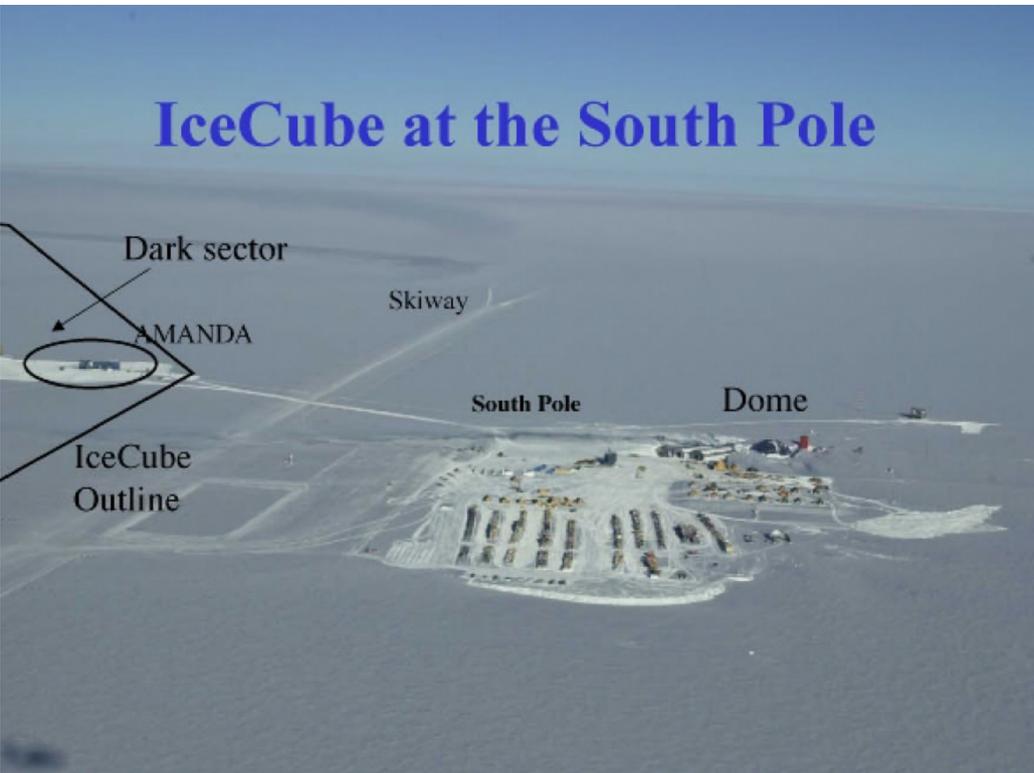
IceCube at the South Pole



Global fit to neutrino oscillations

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- They measure the atmospheric parameters Δm_{31}^2 and θ_{23}

IceCube at the South Pole



Global fit to neutrino oscillations

- Data included:
 - 863 days of ANTARES data
 - 953 days of IceCube DeepCore data
 - SK I-IV

Global fit to neutrino oscillations

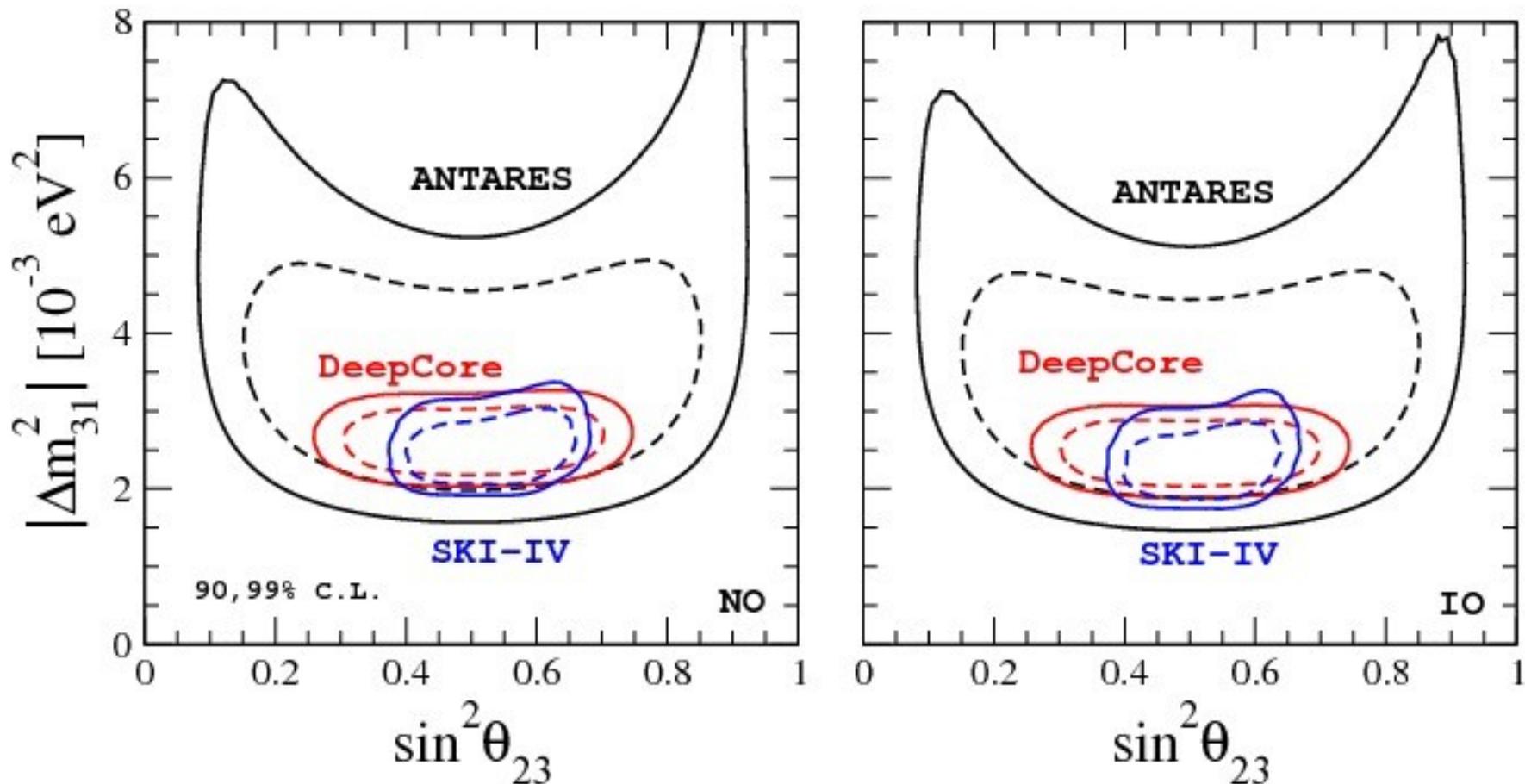
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- In the case of SK we add the grid provided by the collaboration

Global fit to neutrino oscillations

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 - 863 days of ANTARES data
 - 953 days of IceCube DeepCore data
 - SK I-IV
- In the case of SK we add the grid provided by the collaboration
 - 14 datasets, 4 times 520 bins and 155 systematic errors with possible correlations among them, make it impossible to reproduce the results outside the collaboration

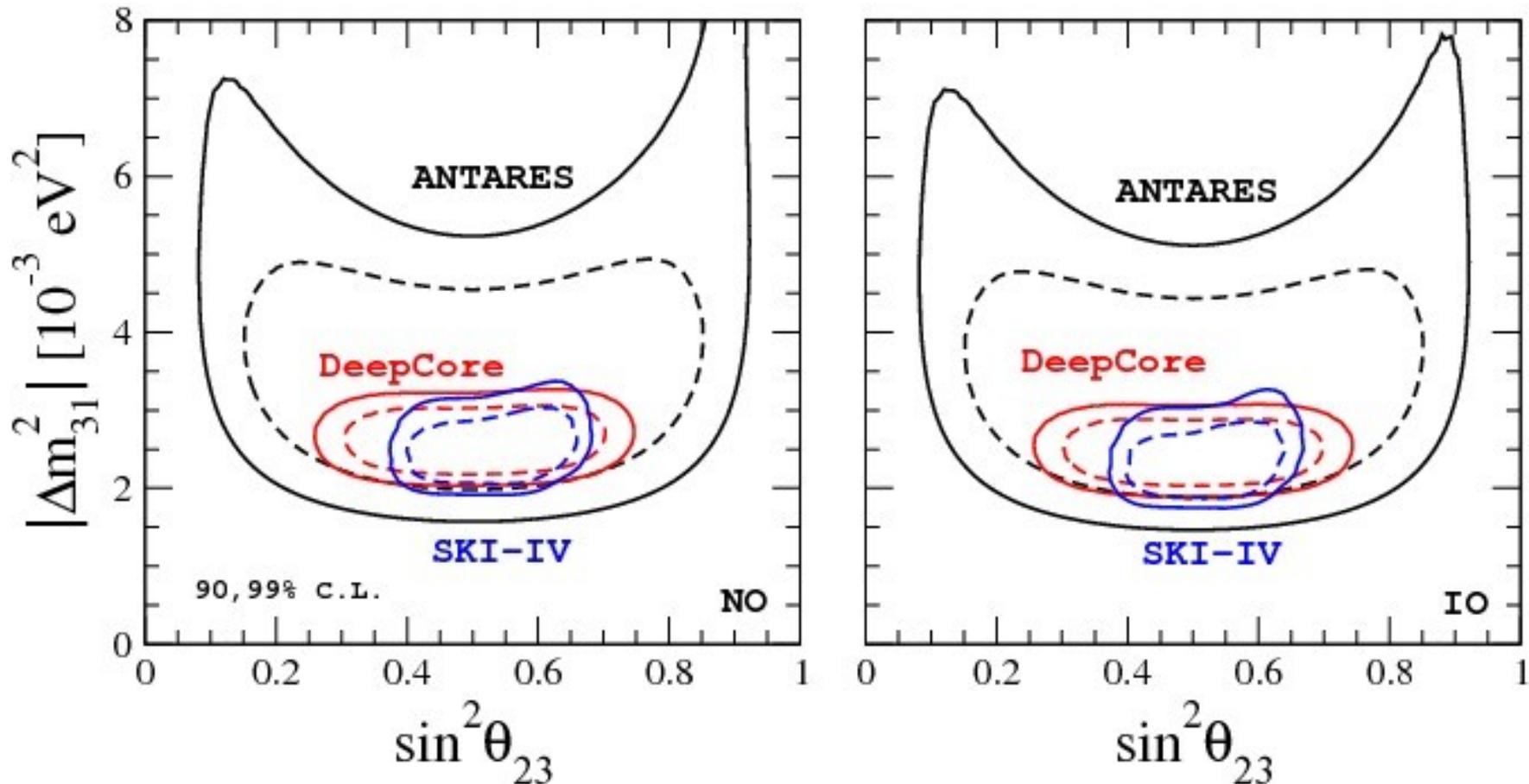
Global fit to neutrino oscillations

- Result of atmospheric experiments



Global fit to neutrino oscillations

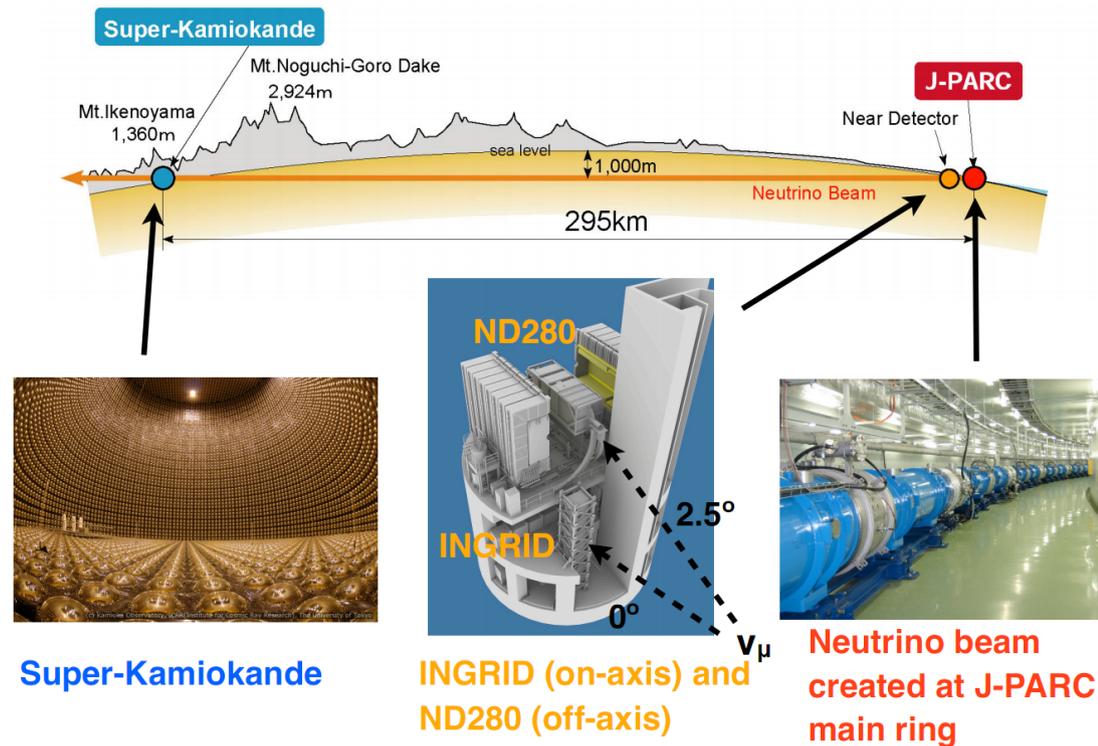
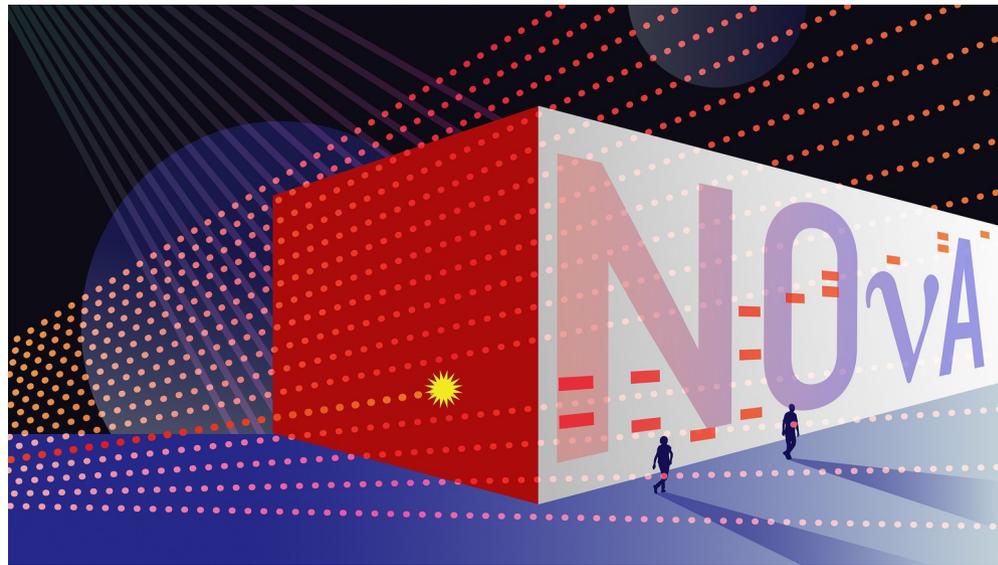
- Result of atmospheric experiments



- Atmospheric experiments start to be competitive with long baseline experiments as we will see now

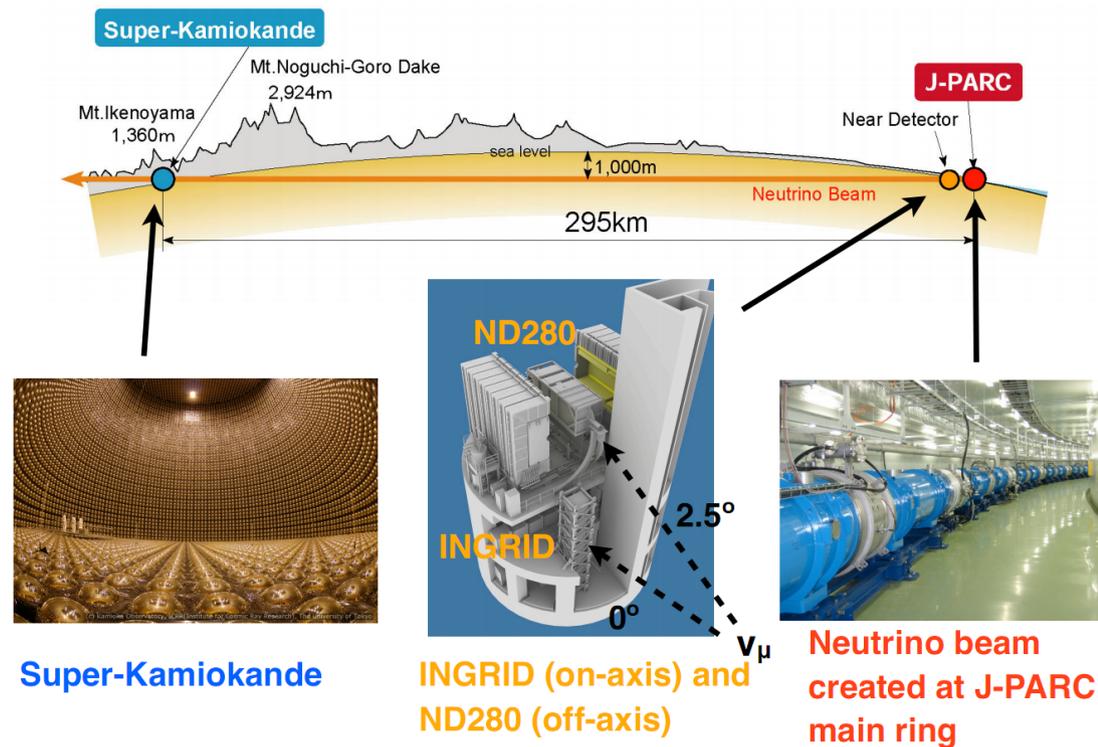
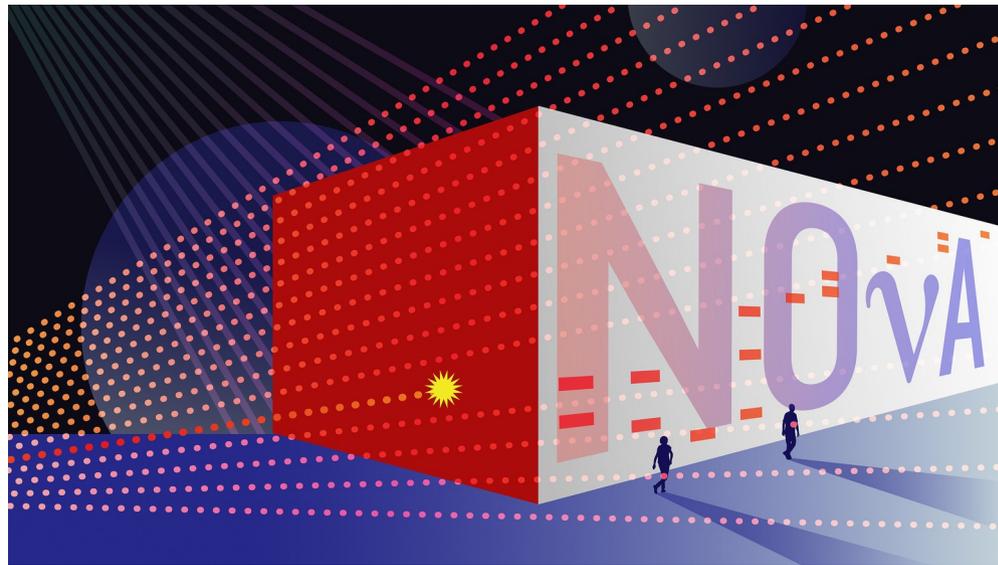
Global fit to neutrino oscillations

- Long baseline experiments measure disappearance of muon neutrinos ($P_{\mu\mu}$) and antineutrinos ($P_{\bar{\mu}\bar{\mu}}$) and appearance of electron neutrinos ($P_{\mu e}$) and antineutrinos ($P_{\bar{\mu}\bar{e}}$) created at accelerator experiments



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- They measure the parameters $\Delta m_{31}^2, \theta_{23}, \theta_{13}$ and δ



Super-Kamiokande

INGRID (on-axis) and ND280 (off-axis)

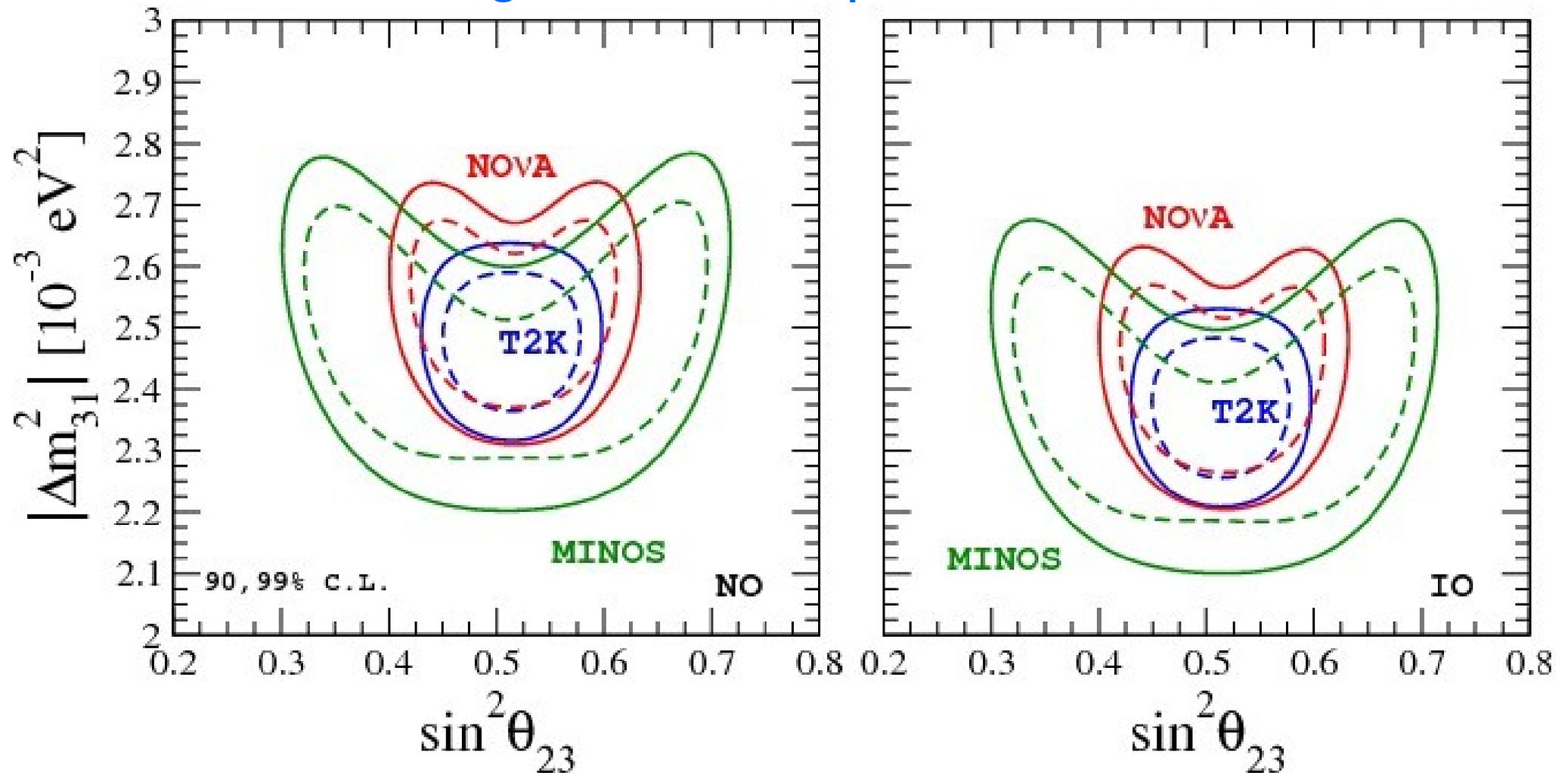
Neutrino beam created at J-PARC main ring

Global fit to neutrino oscillations

- Data included:
 - 14.7×10^{20} POT in neutrino mode at T2K
 - 7.6×10^{20} POT in antineutrino mode at T2K
 - 8.85×10^{20} POT in neutrino mode at NOvA
 - MINOS: full accelerator data set
 - K2K: full data set

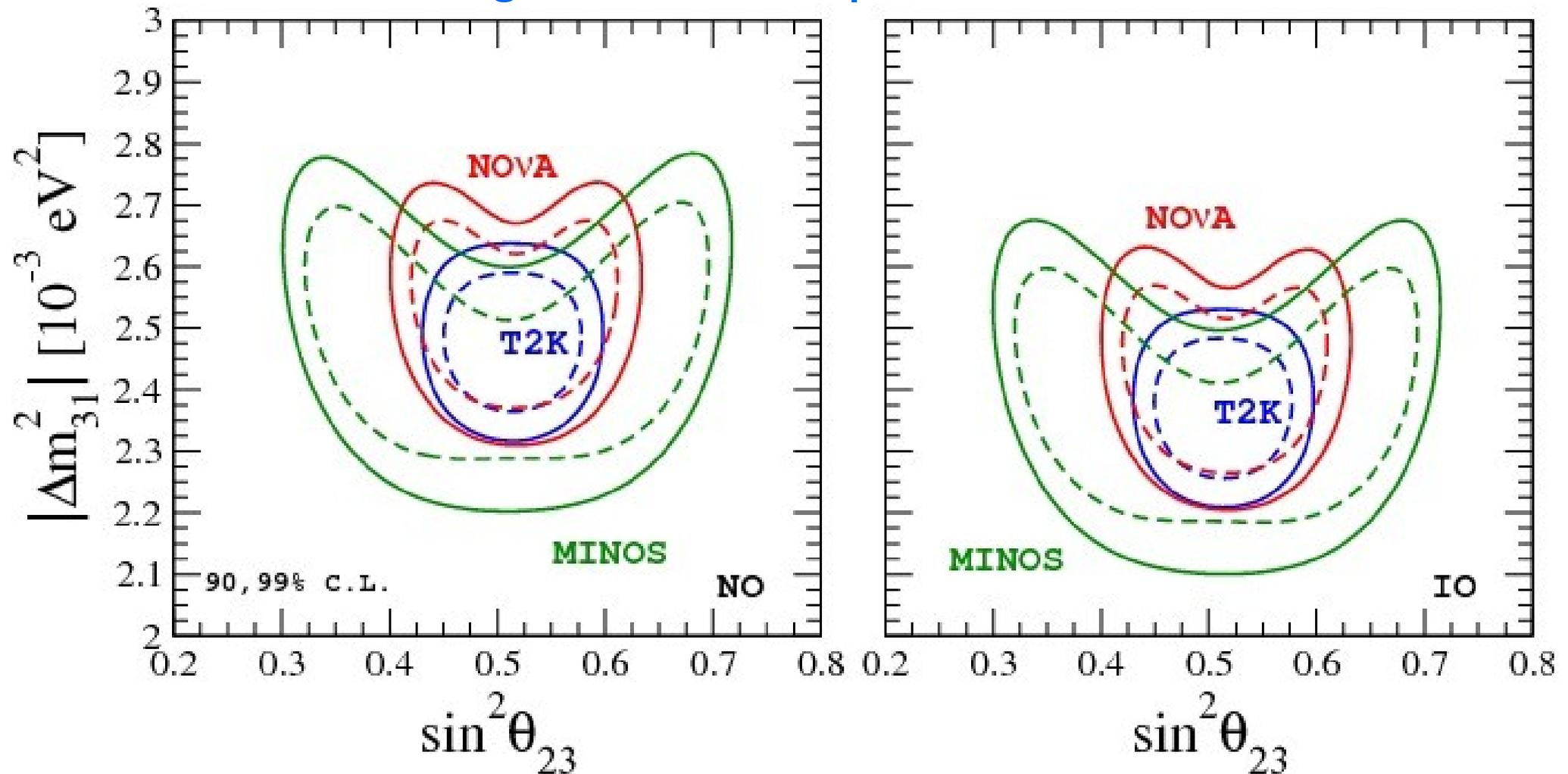
Global fit to neutrino oscillations

- Result of long-baseline experiments



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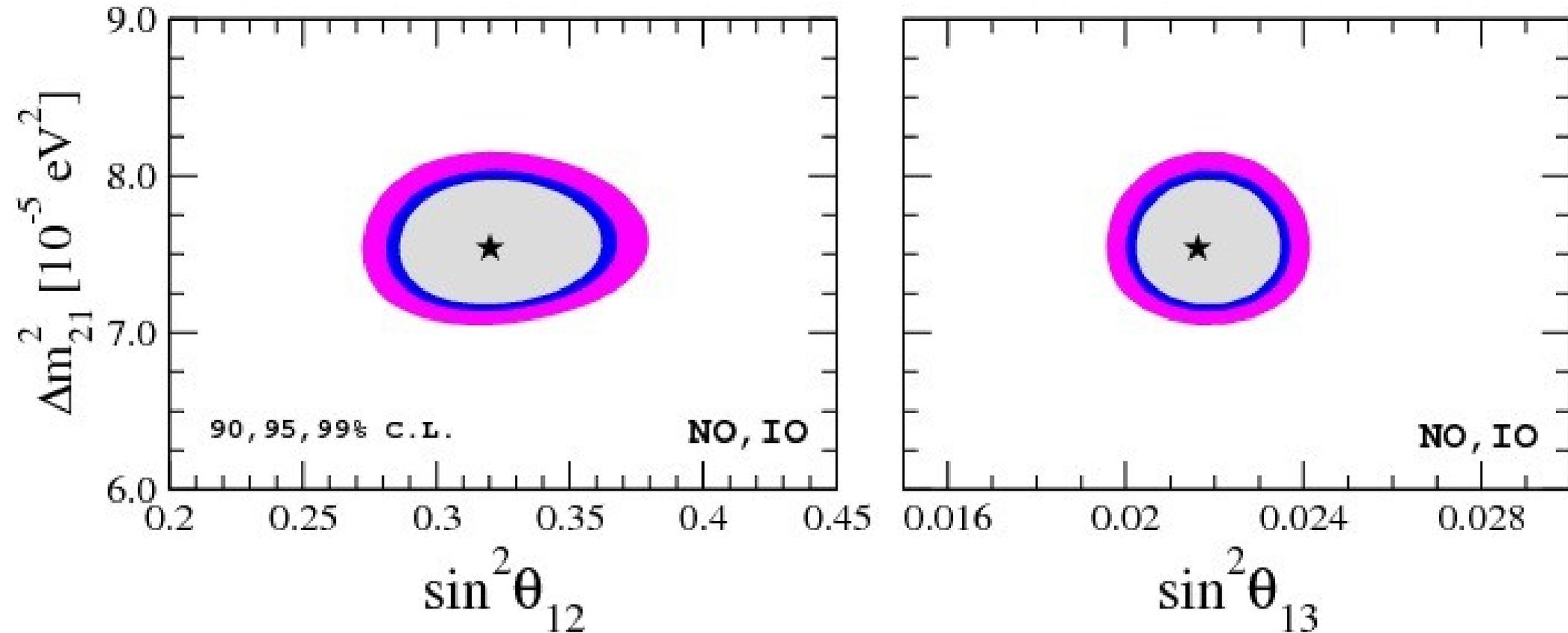


- Analysis dominated by T2K and NOvA

Results of the combined analysis

The solar plane

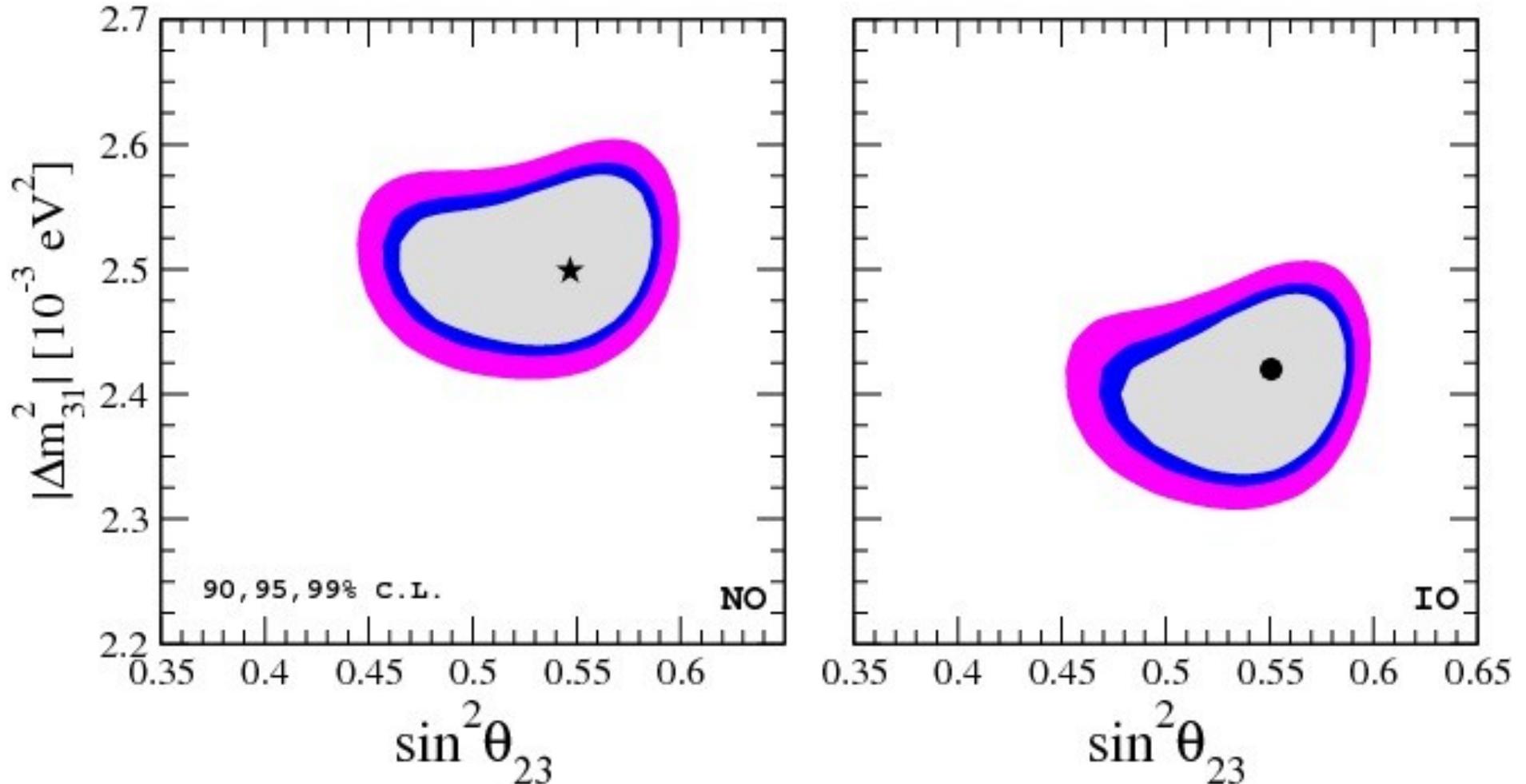
- The solar parameters are measured by solar experiments and KamLAND



- Best fit:** $\sin^2 \theta_{12} = 0.320$, $\Delta m_{21}^2 = 7.55 \times 10^{-5} \text{ eV}^2$

The atmospheric plane

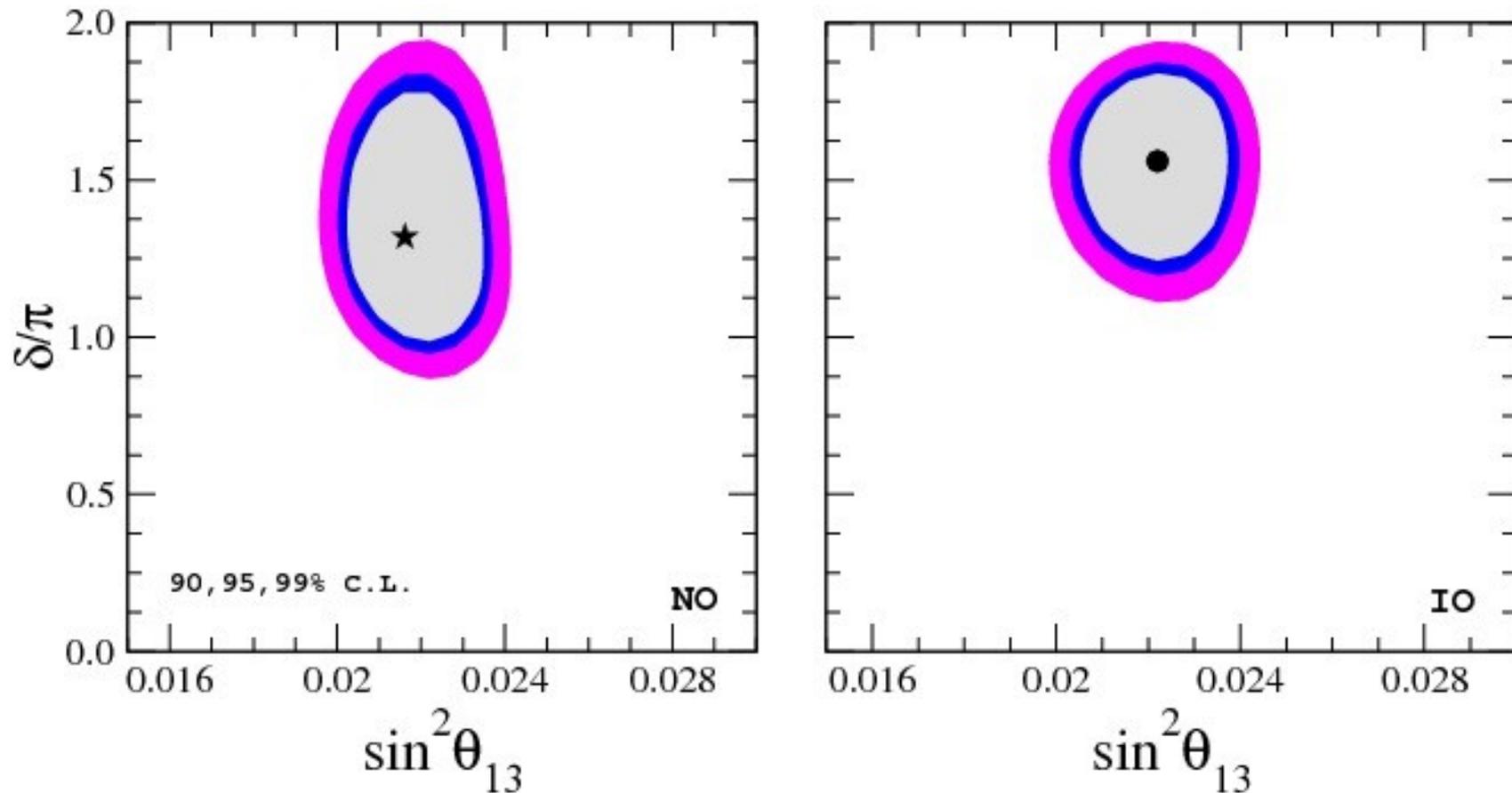
- Measurement of atmospheric parameters dominated by the combination of LBL and reactor experiments



- Best fit:** $\sin^2 \theta_{23} = 0.547, \Delta m_{31}^2 = 2.50 \times 10^{-3} \text{ eV}^2$ (NO)
 $\sin^2 \theta_{23} = 0.551, \Delta m_{31}^2 = -2.42 \times 10^{-3} \text{ eV}^2$ (IO)

The reactor angle and the CP phase

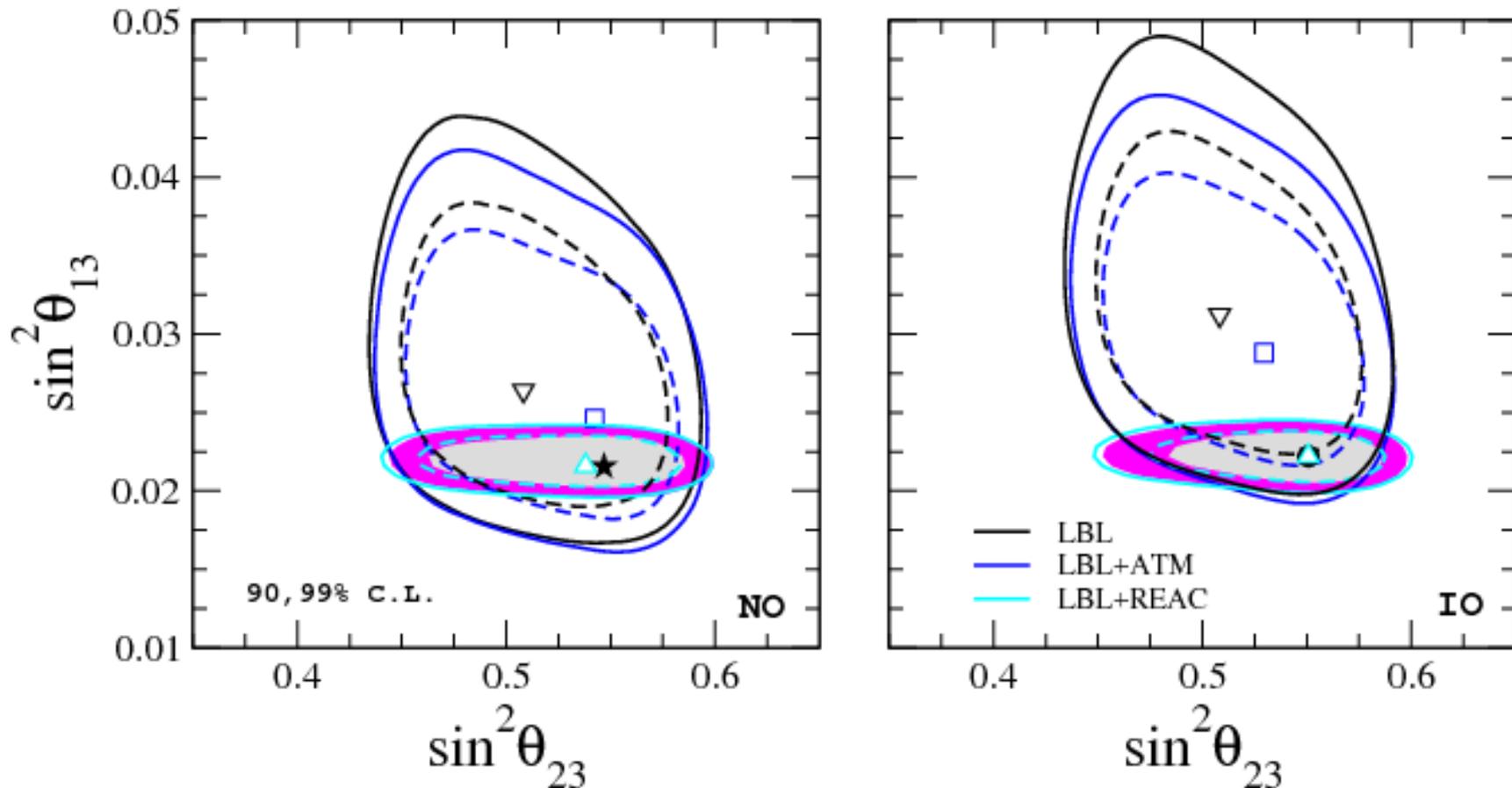
- For the first time we can exclude big part of the parameter space for δ



- Best fit:** $\sin^2 \theta_{13} = 0.02160, \delta = 1.32\pi$ (NO)
 $\sin^2 \theta_{13} = 0.02220, \delta = 1.56\pi$ (IO)

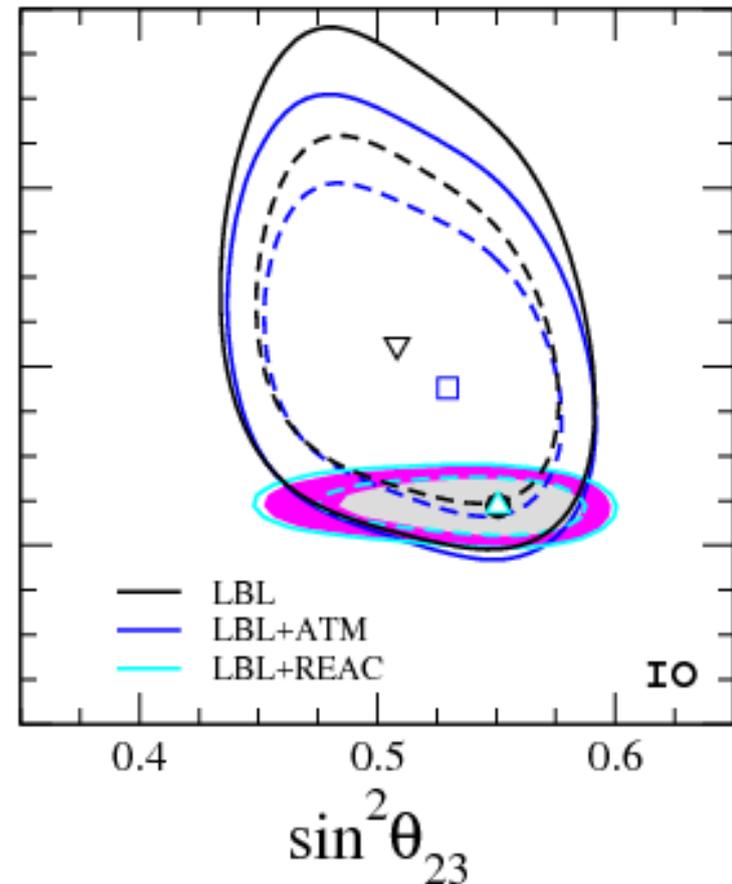
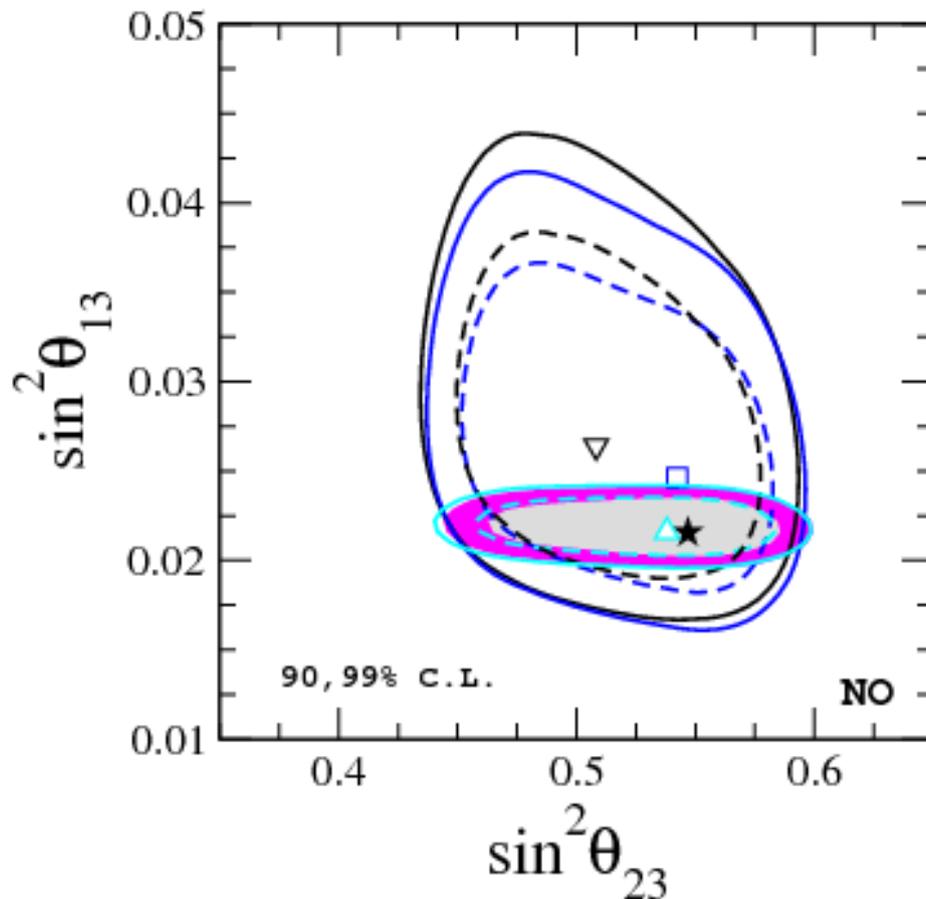
The reactor angle

- The measurement of the reactor angle is dominated by the short baseline reactors

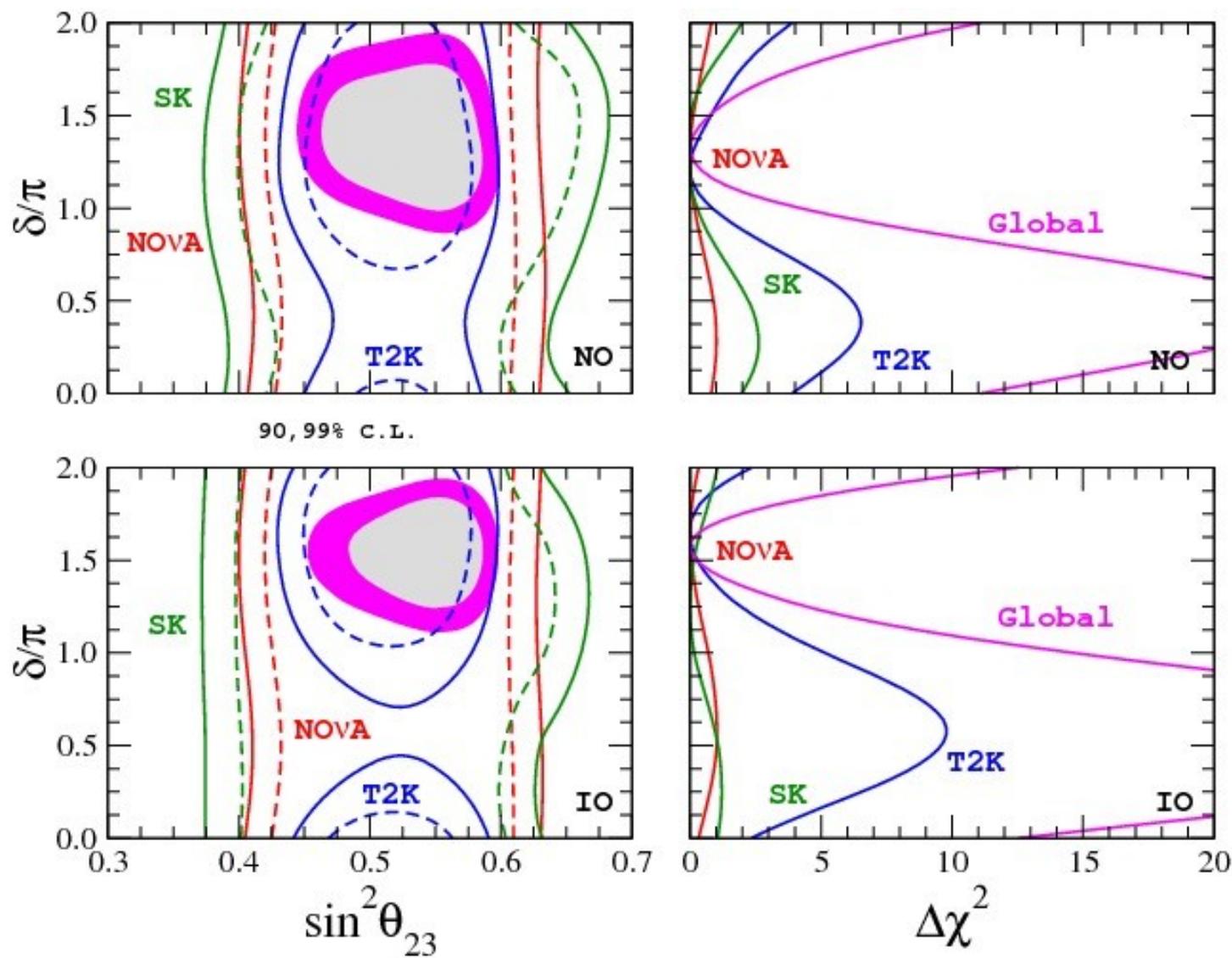


The reactor angle

- The measurement of the reactor angle is dominated by the short baseline reactors
- LBL+ATM might start being competitive in the near future

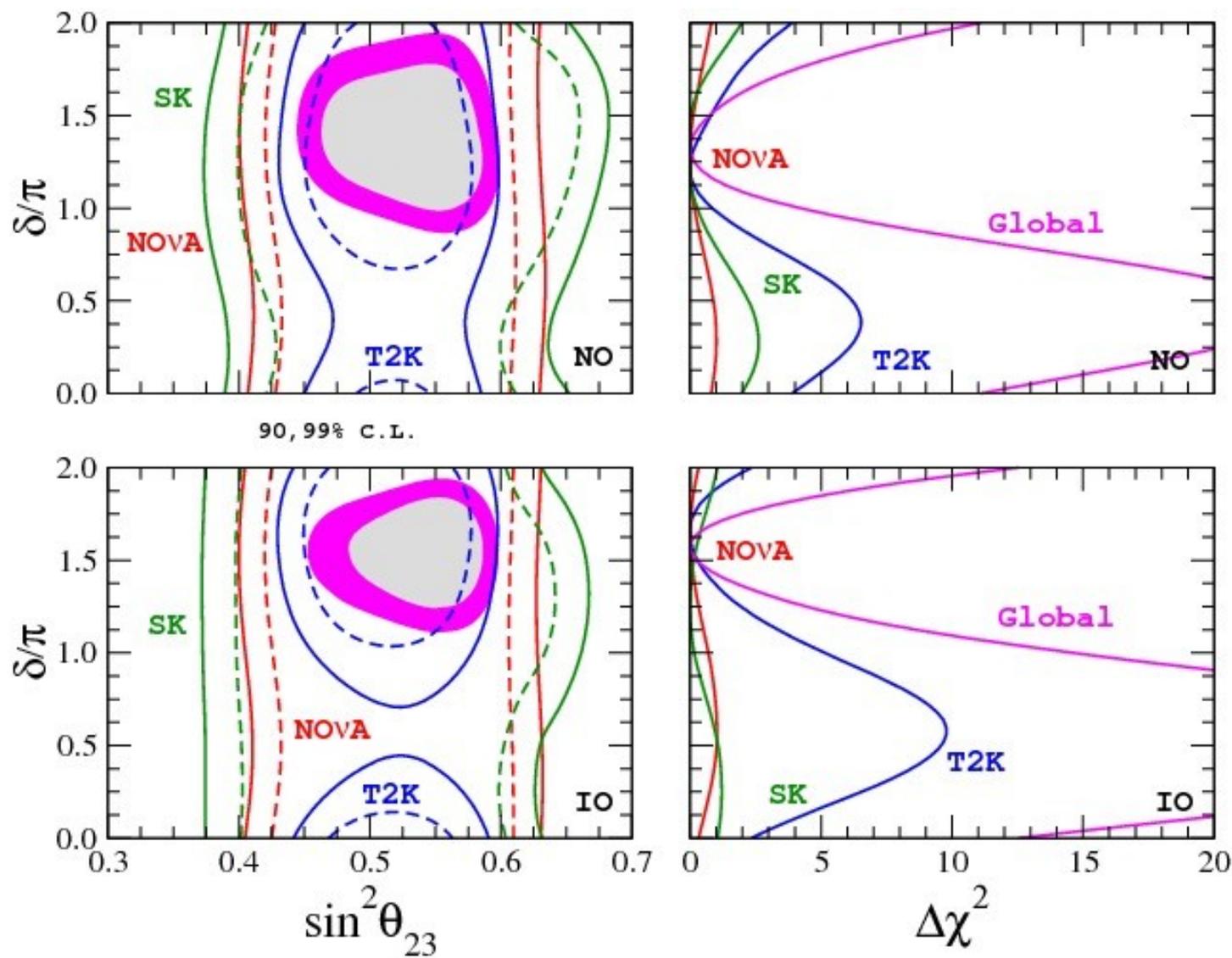


The CP phase



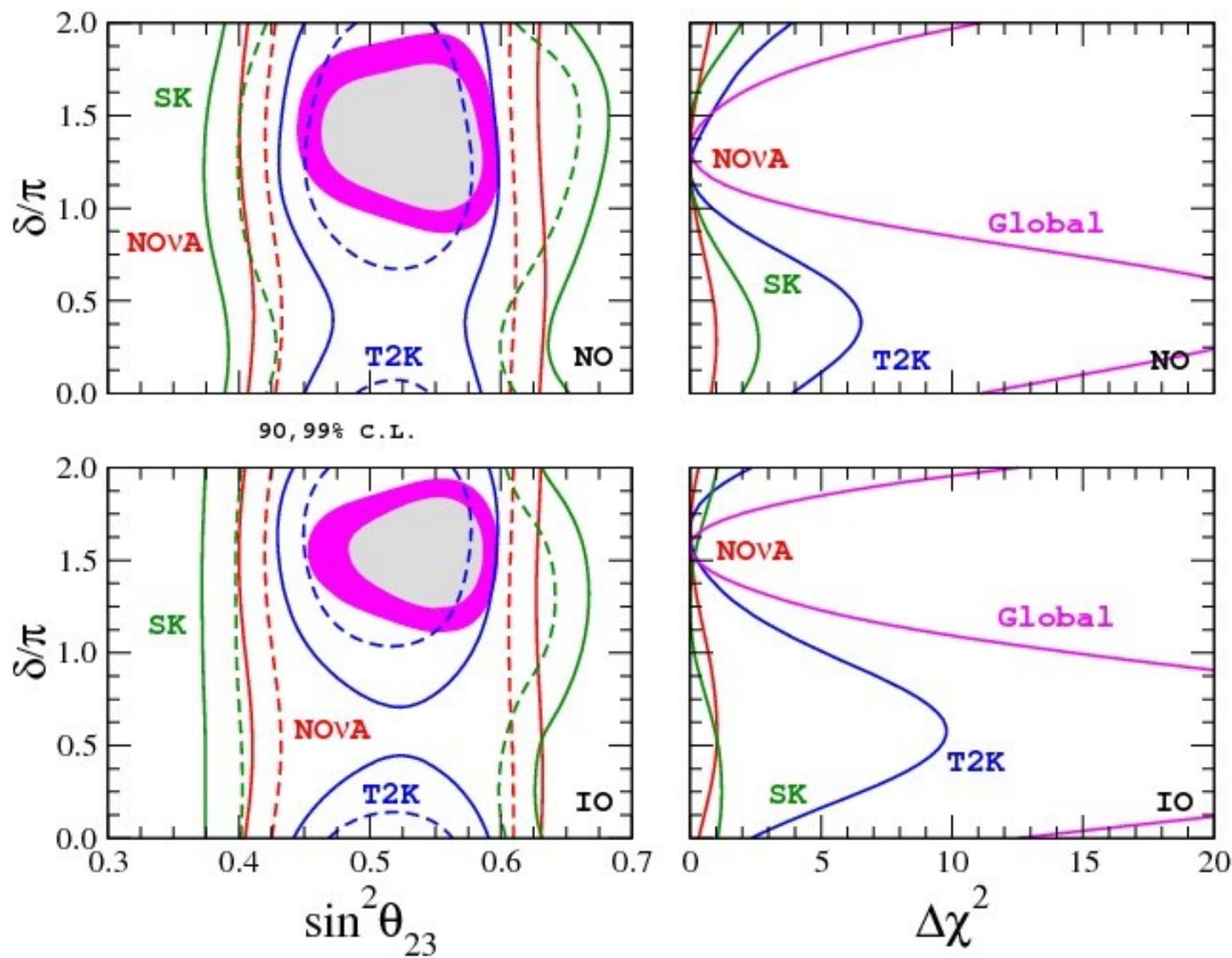
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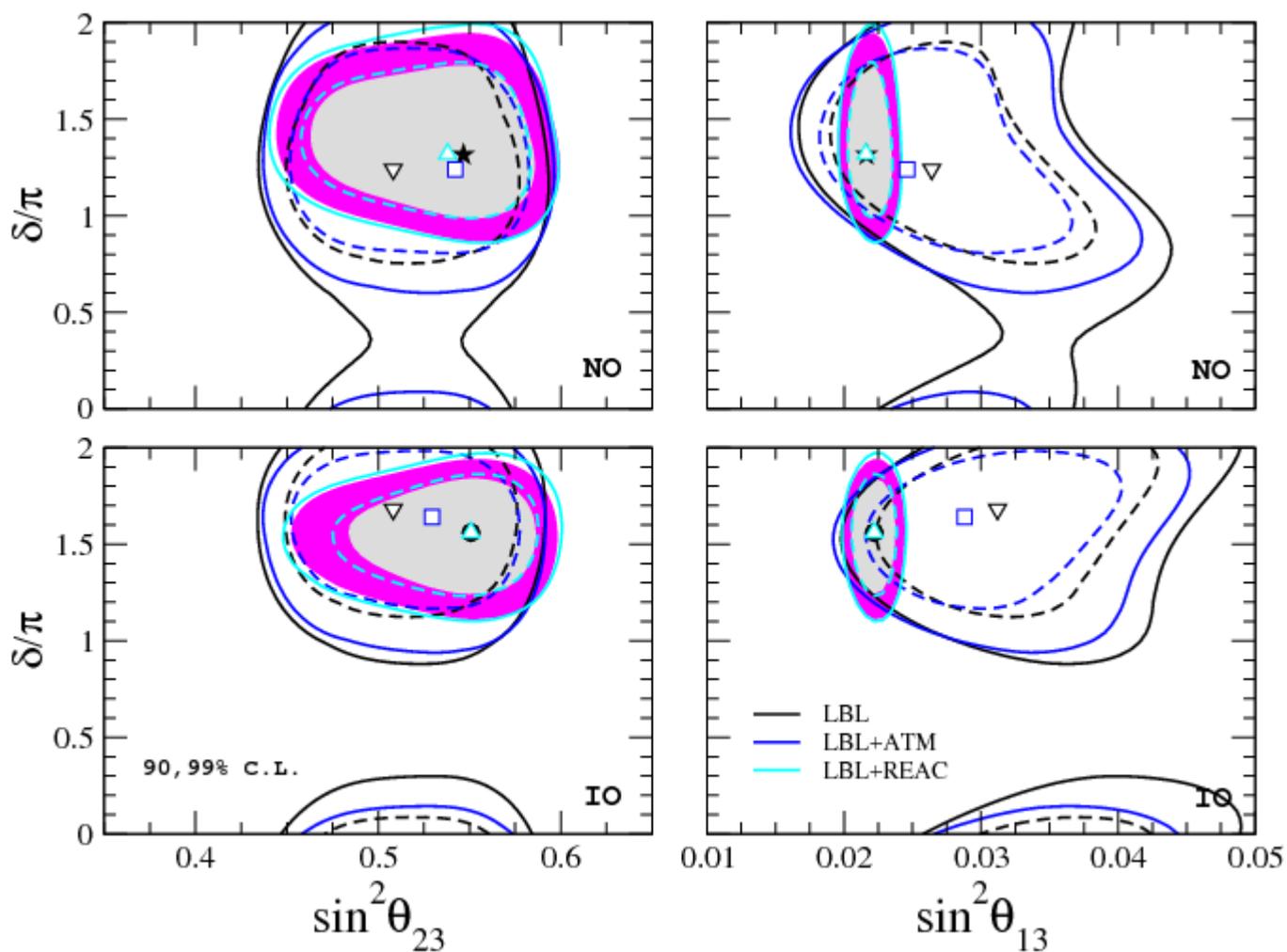
The CP phase



- Best sensitivity to δ comes from T2K
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- This results in exclusion of values around 0.5π at $> 4\sigma$

The mass ordering and the role of SK

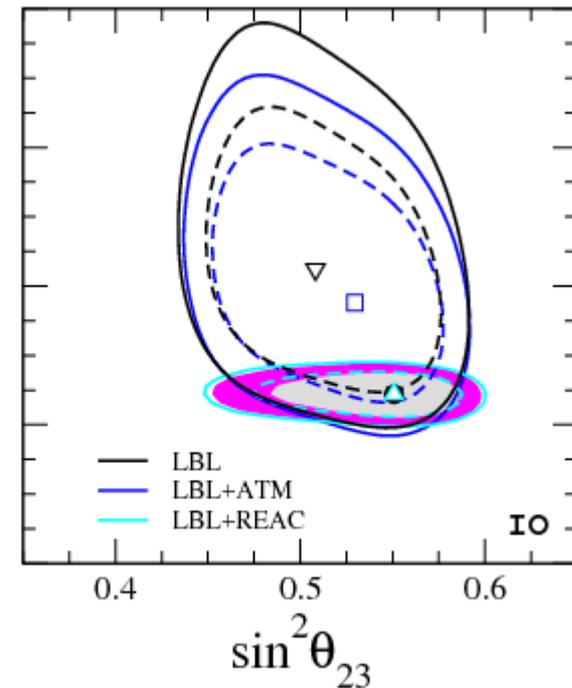
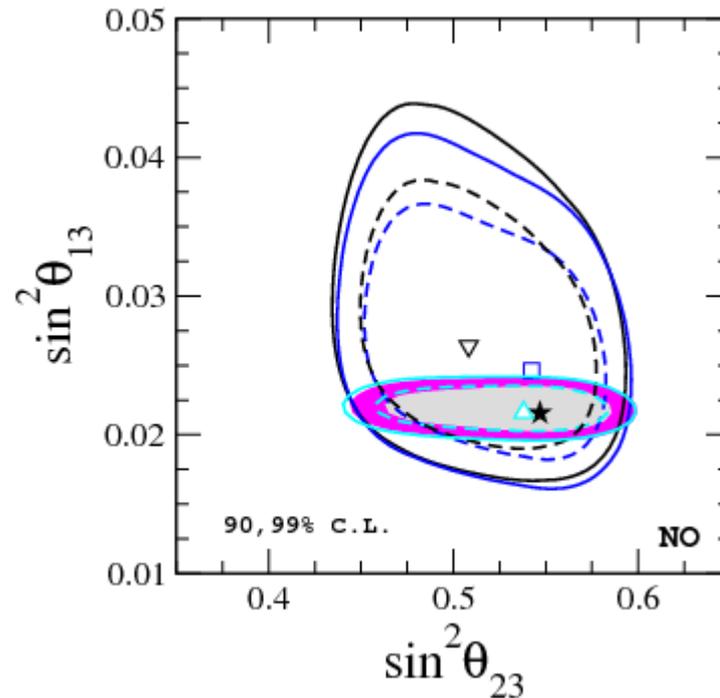
- Inverted mass ordering is now disfavored at more than 3σ , with $\Delta\chi^2 = 11.7$



SK does not
change regions:

The mass ordering and the role of SK

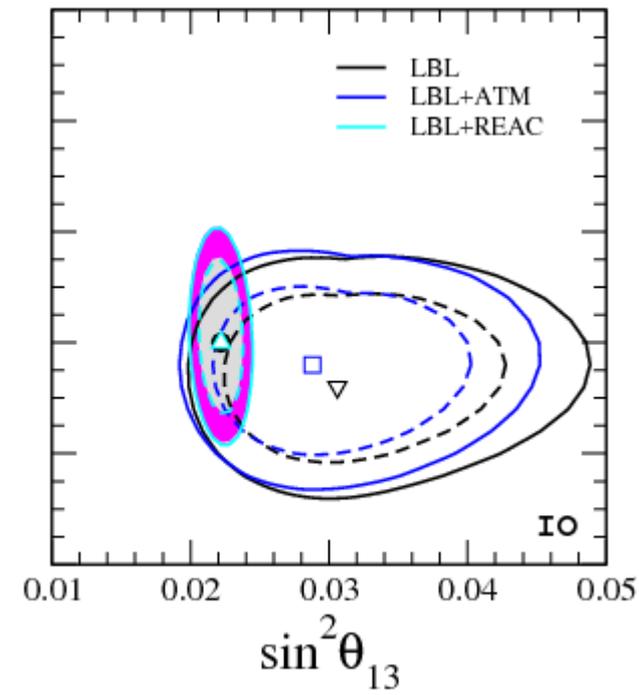
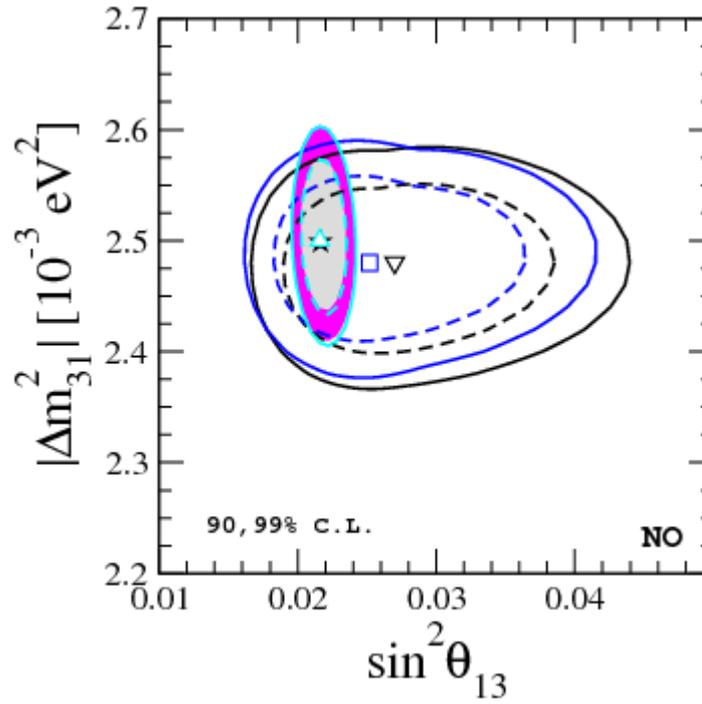
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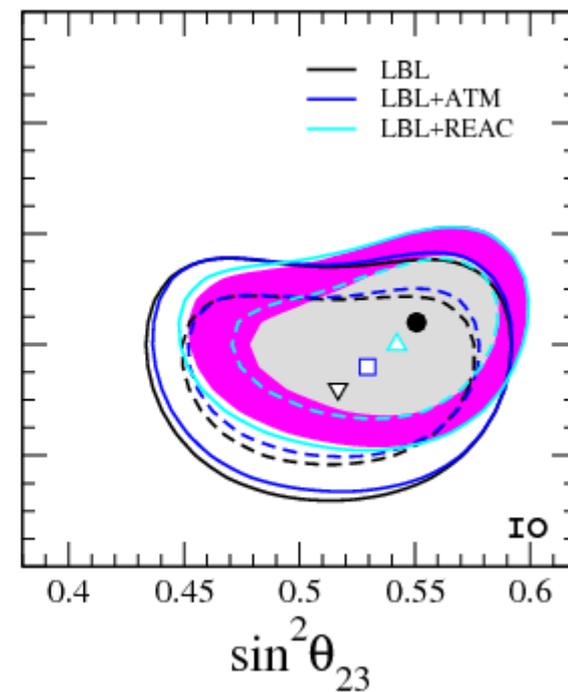
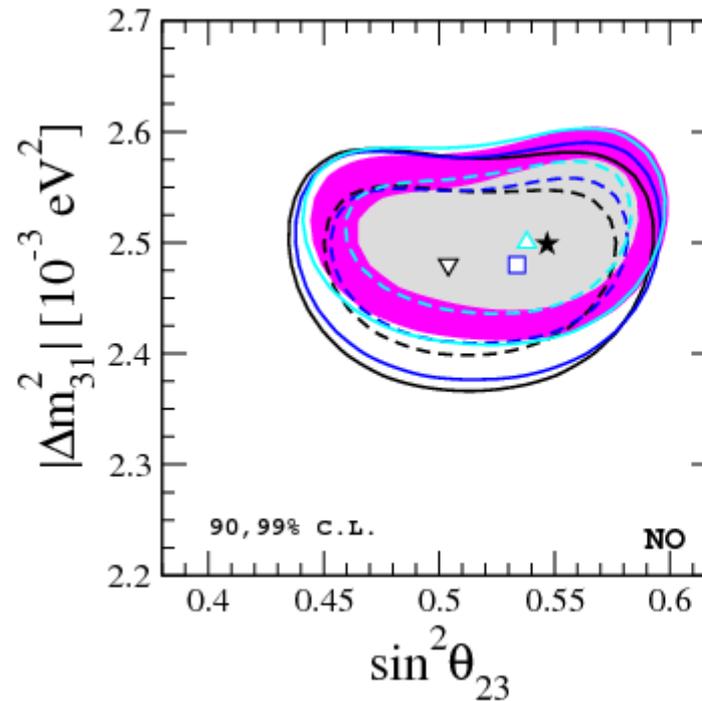


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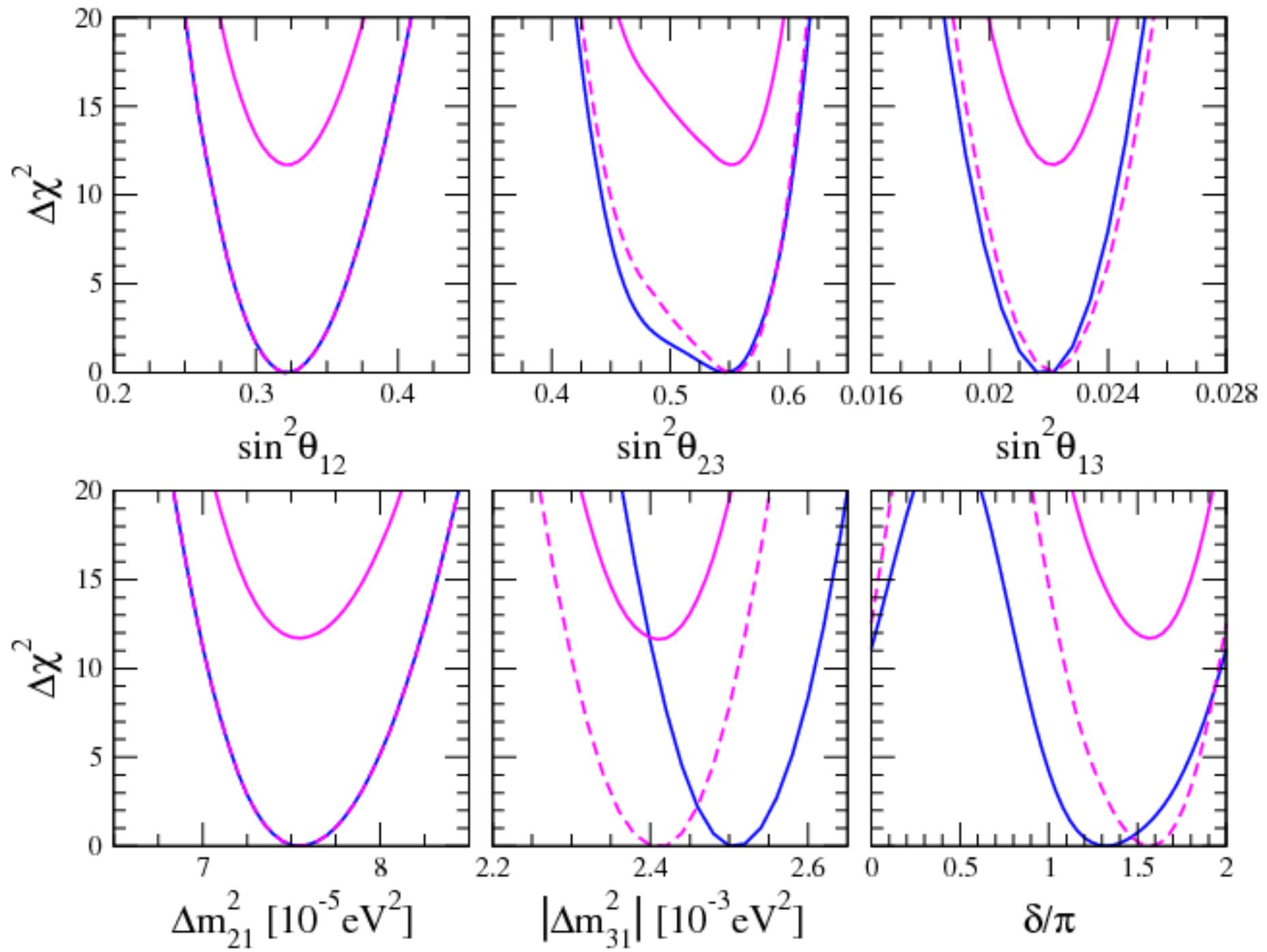
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- If we exclude SK from the fit we obtain $\Delta\chi^2 = 7.7$
- This is due to the combination of LBL+Reactors, since LBL alone gives $\Delta\chi^2 = 2.0$
- SK “only” improves the sensitivity to the mass ordering

SK does not change regions:



Summary of the global fit



Summary of the global fit

parameter	best fit $\pm 1\sigma$	3σ range
Δm_{21}^2 [10^{-5}eV^2]	$7.55^{+0.20}_{-0.16}$	7.05–8.14
$ \Delta m_{31}^2 $ [10^{-3}eV^2] (NO)	2.50 ± 0.03	2.41–2.60
$ \Delta m_{31}^2 $ [10^{-3}eV^2] (IO)	$2.42^{+0.03}_{-0.04}$	2.31–2.51
$\sin^2 \theta_{12}/10^{-1}$	$3.20^{+0.20}_{-0.16}$	2.73–3.79
$\sin^2 \theta_{23}/10^{-1}$ (NO)	$5.47^{+0.20}_{-0.30}$	4.45–5.99
$\sin^2 \theta_{23}/10^{-1}$ (IO)	$5.51^{+0.18}_{-0.30}$	4.53–5.98
$\sin^2 \theta_{13}/10^{-2}$ (NO)	$2.160^{+0.083}_{-0.069}$	1.96–2.41
$\sin^2 \theta_{13}/10^{-2}$ (IO)	$2.220^{+0.074}_{-0.076}$	1.99–2.44
δ/π (NO)	$1.32^{+0.21}_{-0.15}$	0.87–1.94
δ/π (IO)	$1.56^{+0.13}_{-0.15}$	1.12–1.94

More on mass ordering

JCAP 1803 (2018) no.03, 011, S. Gariazzo, M. Archidiacono, P.F. de Salas, O. Mena, CAT, M. Tórtola

arXiv:1806.11051, P.F. de Salas, S. Gariazzo, O. Mena, CAT, M. Tórtola

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- We calculate the Bayesian evidence for both mass orderings

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- We can perform a Bayesian analysis combining several datasets
- In this case we compare NO and IO by means of model selection techniques
- We calculate the Bayesian evidence for both mass orderings

$$Z = p(d|\mathcal{M}) = \int_{\Omega_{\mathcal{M}}} p(d|\theta, \mathcal{M})p(\theta|\mathcal{M})d\theta$$

- Then we compute the Bayes factor

$$B_{\text{NO,IO}} = \frac{Z_{\text{NO}}}{Z_{\text{IO}}} \Rightarrow \ln B_{\text{NO,IO}} = \ln Z_{\text{NO}} - \ln Z_{\text{IO}}$$

More on mass ordering

- The preference for one ordering is then given by the Jeffreys' scale

$ \ln B_{\text{NO},\text{IO}} $	Odds	strength of evidence	$N\sigma$ for the mass ordering
< 1.0	$\lesssim 3 : 1$	inconclusive	$< 1.1\sigma$
$\in [1.0, 2.5]$	$(3 - 12) : 1$	weak	$1.1 - 1.7\sigma$
$\in [2.5, 5.0]$	$(12 - 150) : 1$	moderate	$1.7 - 2.7\sigma$
$\in [5.0, 10]$	$(150 - 2.2 \times 10^4) : 1$	strong	$2.7 - 4.1\sigma$
$\in [10, 15]$	$(2.2 \times 10^4 - 3.3 \times 10^6) : 1$	very strong	$4.1 - 5.1\sigma$
> 15	$> 3.3 \times 10^6 : 1$	decisive	$> 5.1\sigma$

Parameterization and data

Parameterization and data

- Apart from oscillation data we include:
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Temperature and high- l polarization data from Planck (as of 2015) + a prior on the optical depth (2016), BAO, and a prior on H_0
- Also included is data from the decay experiments: KamLAND-ZEN, EXO200 and GERDA

Parameterization and data

- The result can depend drastically on the choice of parametrization and priors

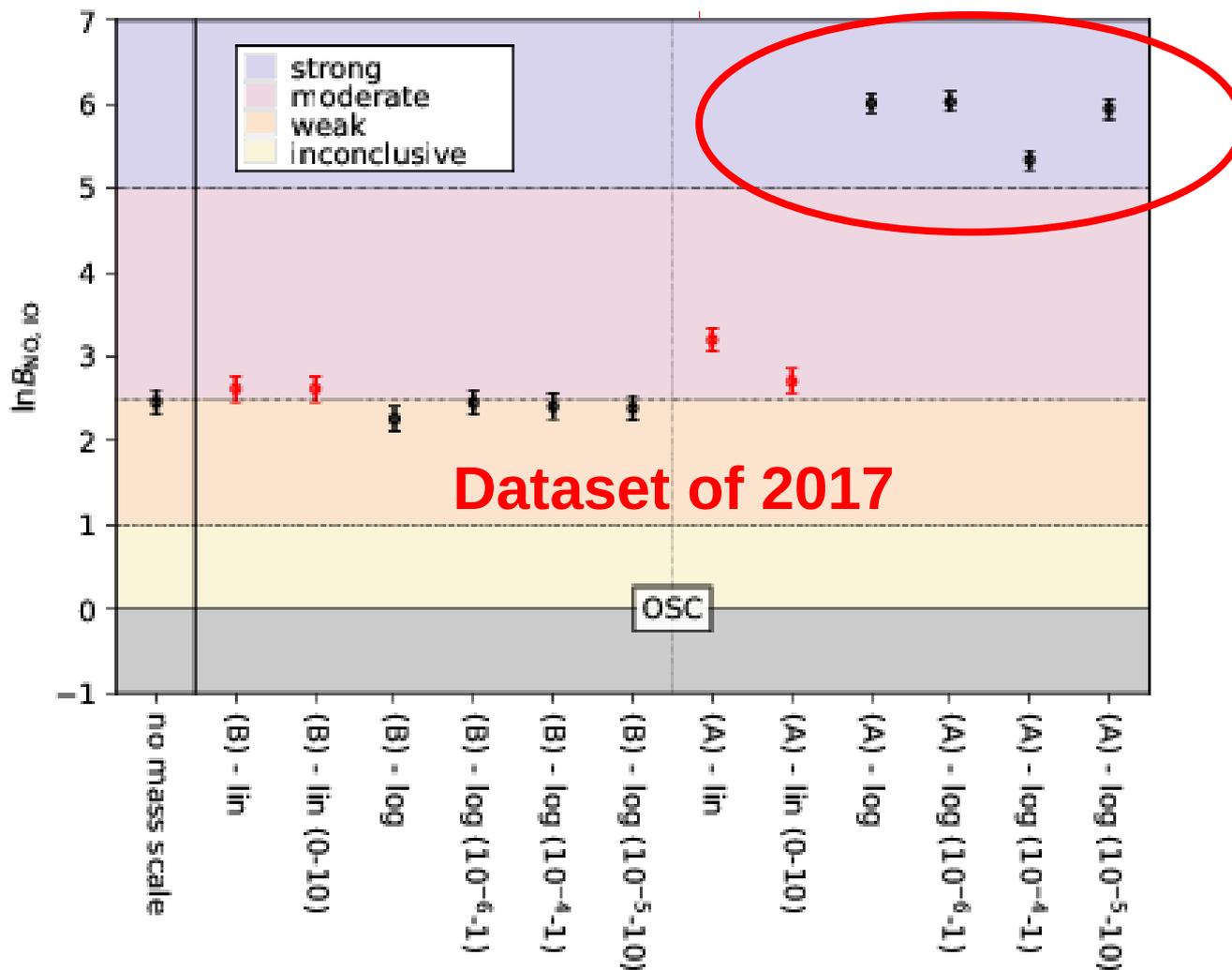
Parameterization and data

- The result can depend drastically on the choice of parametrization and priors
- There are for example several ways to parametrize the neutrino masses

Model A			Model B		
Parameter	Prior	Range	Parameter	Prior	Range
m_1/eV	linear log	0 – 1 $10^{-5} - 1$	m_{lightest}/eV	linear log	0 – 1 $10^{-5} - 1$
m_2/eV	linear log	0 – 1 $10^{-5} - 1$	$\Delta m_{21}^2/eV^2$	linear	$5 \times 10^{-5} - 10^{-4}$
m_3/eV	linear log	0 – 1 $10^{-5} - 1$	$ \Delta m_{31}^2 /eV^2$	linear	$1.5 \times 10^{-3} - 3.5 \times 10^{-3}$

Parameterization and data

- This can give a biased preference for normal ordering



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Neutrino mixing and masses		Cosmological		$0\nu\beta\beta$	
Parameter	Prior	Parameter	Prior	Parameter	Prior
$\sin^2 \theta_{12}$	0.1 – 0.6	$\Omega_b h^2$	0.019 – 0.025	α_2	0 – 2π
$\sin^2 \theta_{13}$	0.00 – 0.06	$\Omega_c h^2$	0.095 – 0.145	α_3	0 – 2π
$\sin^2 \theta_{23}$	0.25 – 0.75	Θ_s	1.03 – 1.05	$\mathcal{M}_{76\text{Ge}}^{0\nu}$	3.3 – 5.7
δ_{CP}/π	0 – 2	τ	0.01 – 0.4	$\mathcal{M}_{136\text{Xe}}^{0\nu}$	1.5 – 3.7
$\Delta m_{21}^2/\text{eV}^2$	$5 \times 10^{-5} - 10^{-4}$	n_s	0.885 – 1.04		
$\Delta m_{31}^2/\text{eV}^2$	$1.5 \times 10^{-3} - 3.5 \times 10^{-3}$	$\log(10^{10} A_s)$	2.5 – 3.7		
$\log_{10}(m_{\text{lightest}}/\text{eV})$	-5 – 0				

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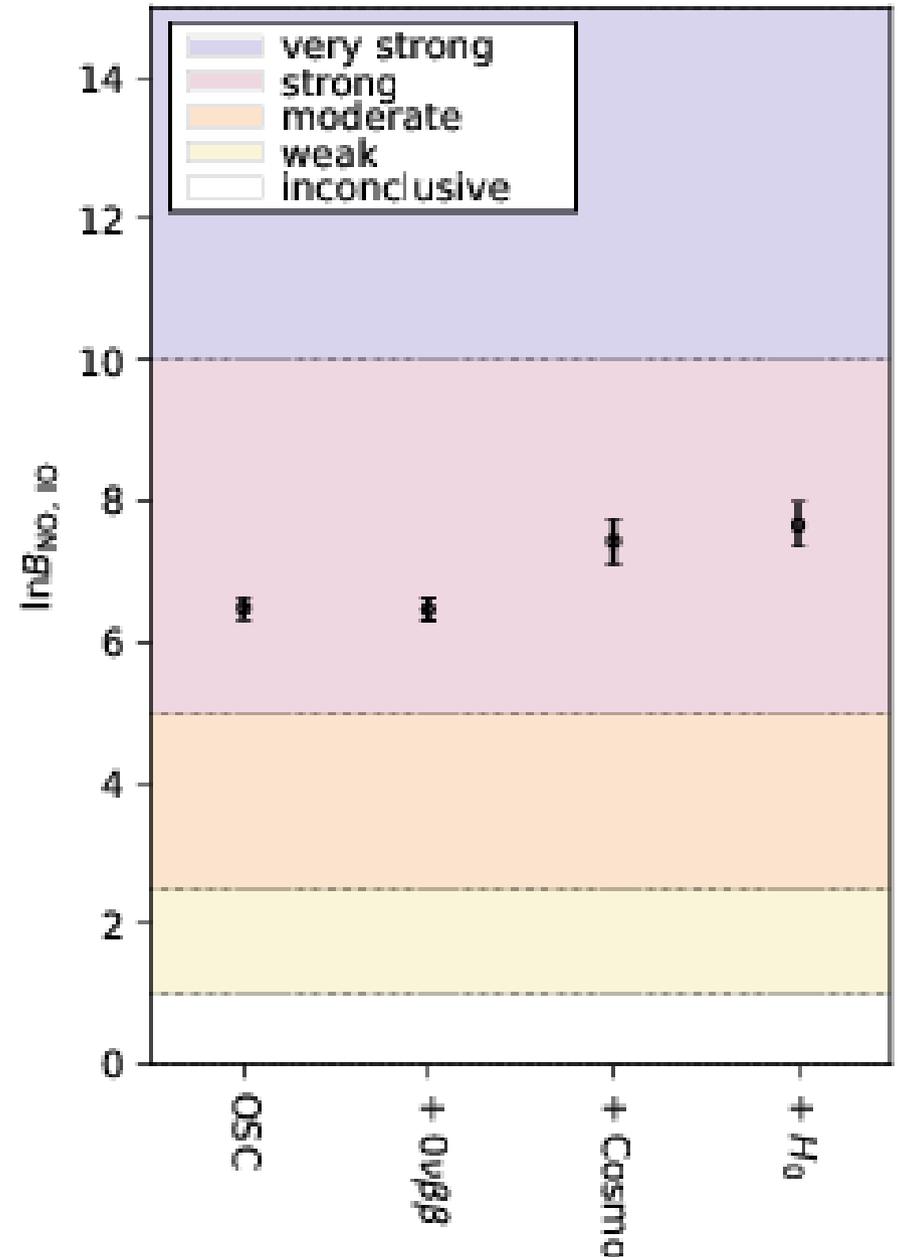
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- with a logarithmic prior on the lightest neutrino mass

Results

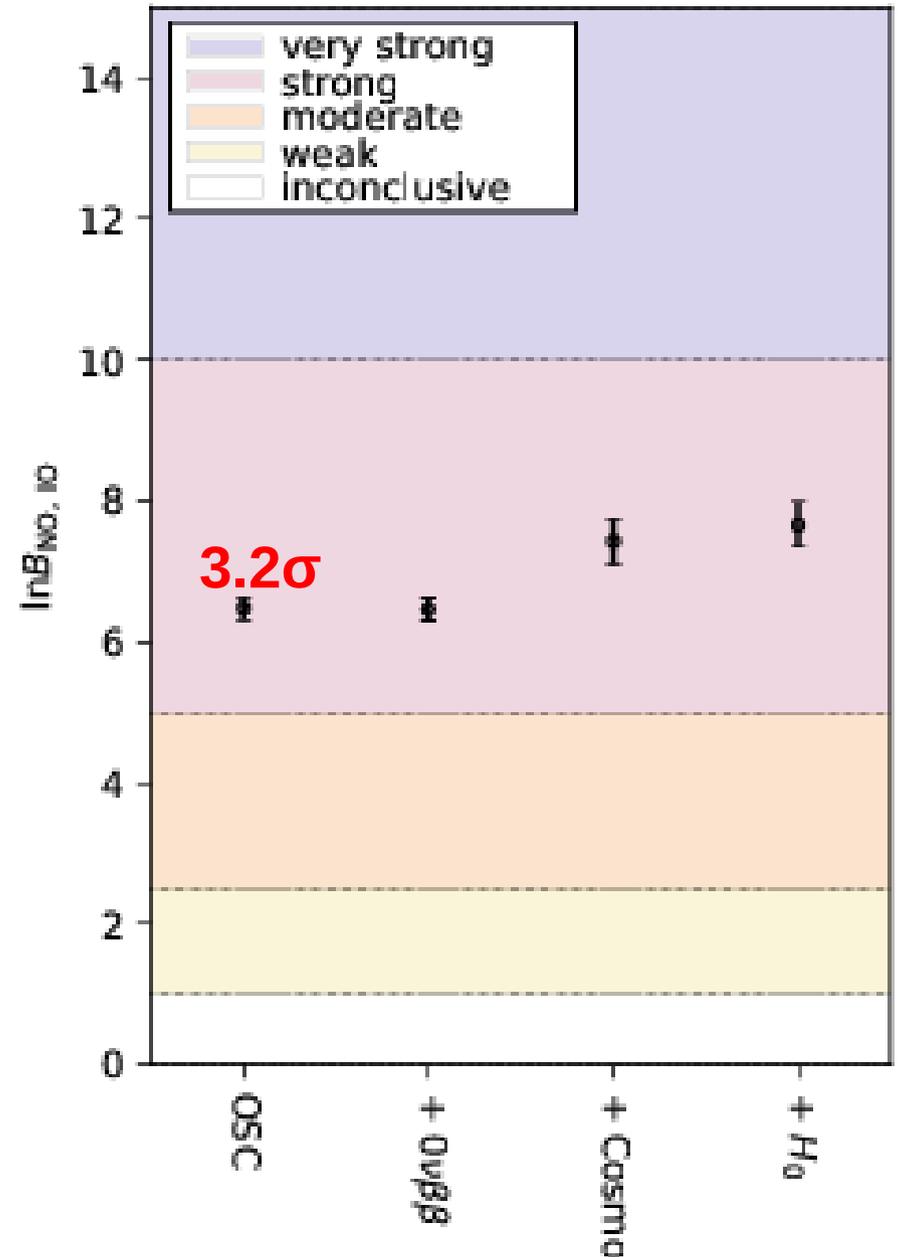
Results

- Different data sets are considered



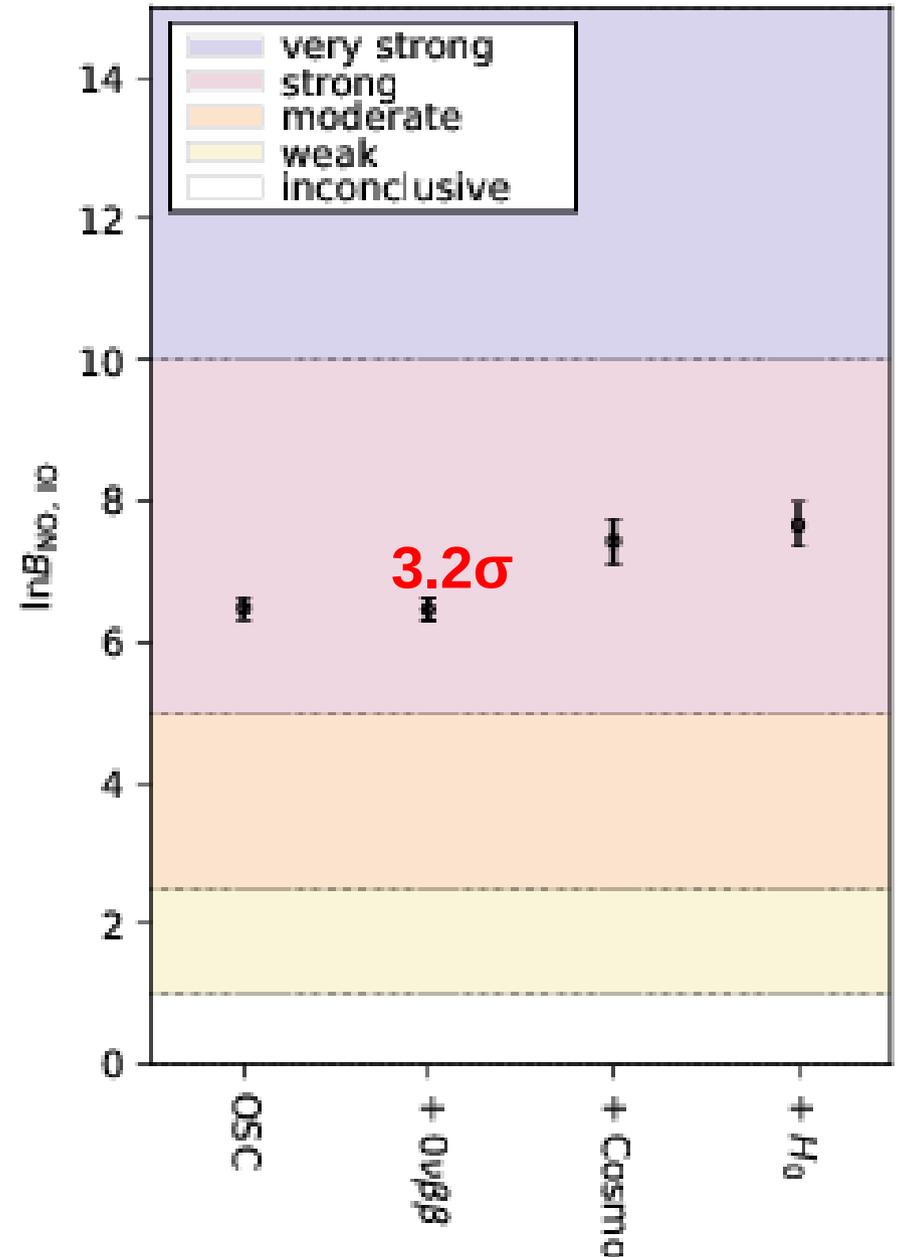
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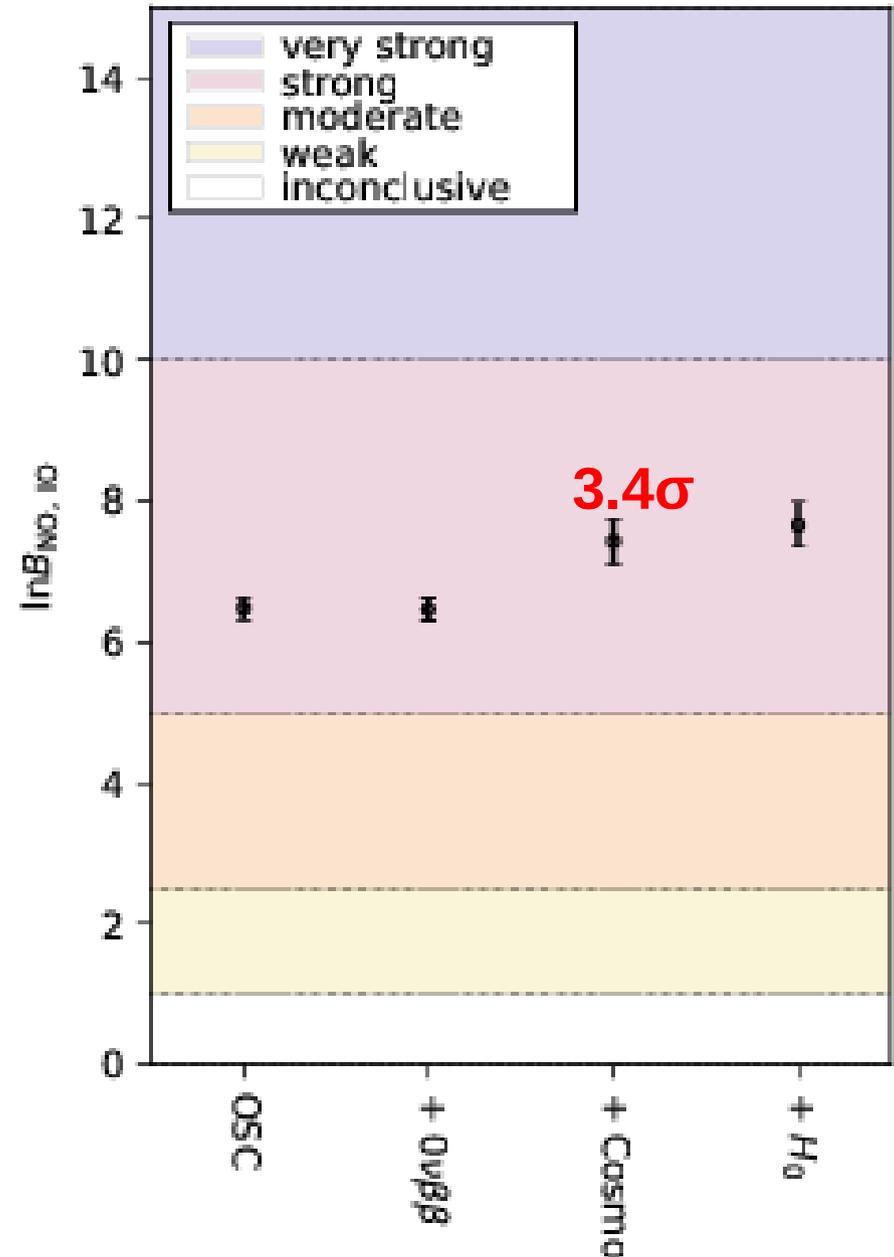
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 - OSC plus decay data



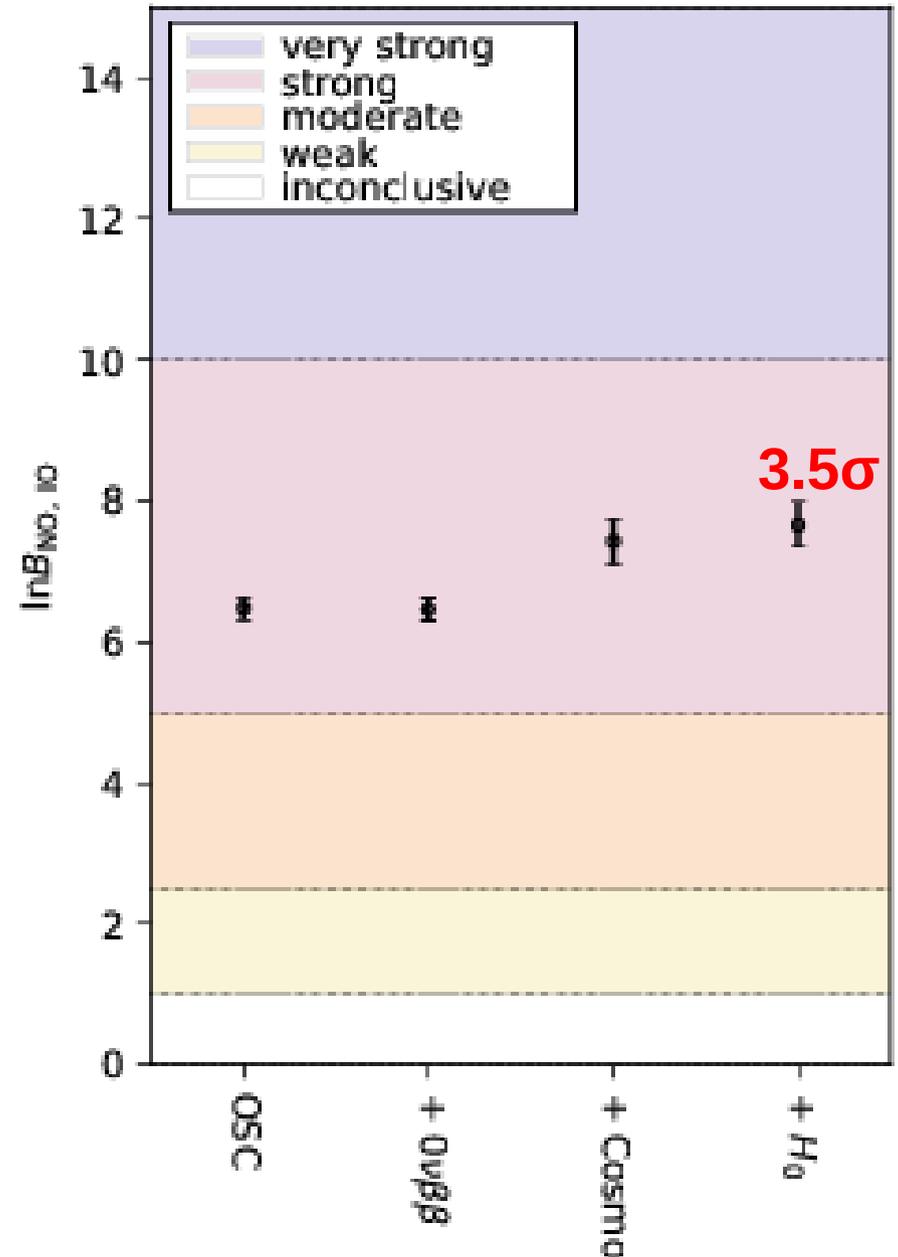
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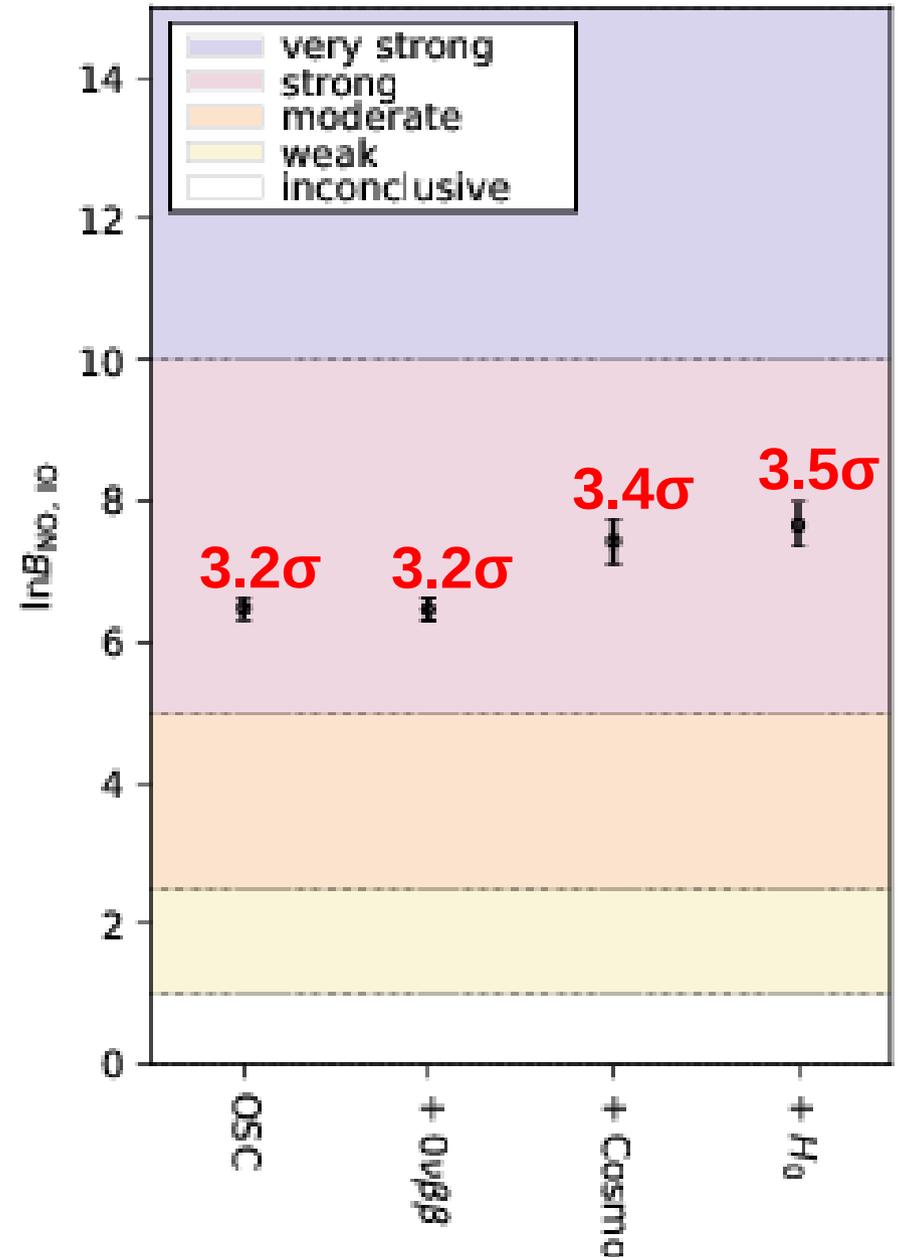
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Results

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 - Only oscillation data
 - OSC plus decay data
 - OSC+ $0\nu\beta\beta$ plus CMB plus BAO
 - As before, but with an prior on the Hubble constant
- Strong preference for NO in all cases (driven by oscillation data)



Conclusions

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- We exclude a large part for of the parameter space for the CP phase
- The octant problem remains unsolved, although the value now tends towards the second octant
- By combining several datasets, including cosmological observations and $0\nu\beta\beta$ -data we disfavor inverted mass ordering with 3.5σ

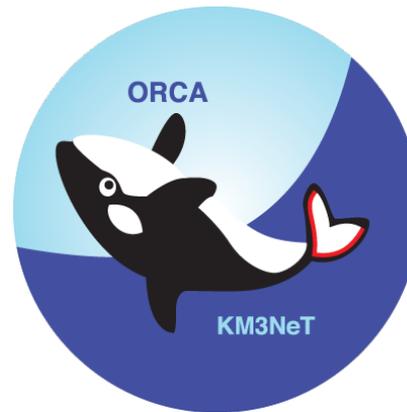
Stay tuned for the future!

RENO-50

DUNE



INO



HYPER
HK

Thank you!

