DUNE and CPT-violating neutrinos

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 - Hermiticity of the Hamiltonian
 - Locality
 - Lorentz invariance
- If CPT is violated, one of the three ingredients above must be violated, resulting in a gigantic impact on fundamental physics

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• Neutrinos might give better bounds

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$$\chi^2(\Delta x) = \chi^2(|x - \overline{x}|) = \chi^2(x) + \chi^2(\overline{x})$$

• We use the same data as in the Valencia global fit as of August 2017 (excluding atmospheric experiments)

Phys.Lett. B782 (2018) 633-640, P.F. de Salas, D.V. Forero, CAT, M. Tórtola, J.W.F. Valle https://globalfit.astroparticles.es/

Current bounds $(\sin^2 \theta_{12})$

- The solar angle for neutrinos is measured by solar experiments
- The antineutrino counterpart is measured by KamLAND



Current bounds (Δm_{21}^2)

- The same experiments measure the solar mass splittings for neutrinos
- Also in this case the antineutrino part is measured by KamLAND



Current bounds $(\sin^2 \theta_{13})$

- $\sin^2 \theta_{13}$ measured by solar experiments and accelerators (T2K, NOvA, MINOS, K2K)
- Apart from reactor experiments (Daya Bay, RENO, Double Chooz, KamLAND) we include data from T2K and MINOS for $\sin^2 \overline{\theta}_{13}$



Current bounds $(\sin^2 \theta_{23})$

- $\sin^2 \theta_{23}$ is measured by all long-baseline accelerators (T2K, NOvA, MINOS, K2K)
- For antineutrinos we use only data from T2K and MINOS (no NOvA antineutrinos in 2017)



Current bounds (Δm_{31}^2)

- For the atmospheric mass splitting we use data from all of the LBLs in neutrino mode
- For antineutrinos we use T2K, MINOS and the short baseline reactors



• We obtain the current bounds at 3σ C.L.

$$\begin{aligned} |\Delta m_{21}^2 - \Delta \overline{m}_{21}^2| &< 4.7 \times 10^{-5} \text{eV}^2, \\ |\Delta m_{31}^2 - \Delta \overline{m}_{31}^2| &< 3.7 \times 10^{-4} \text{eV}^2, \\ |\sin^2 \theta_{12} - \sin^2 \overline{\theta}_{12}| &< 0.14, \\ |\sin^2 \theta_{13} - \sin^2 \overline{\theta}_{13}| &< 0.03, \\ |\sin^2 \theta_{23} - \sin^2 \overline{\theta}_{23}| &< 0.32 \end{aligned}$$

Phys.Lett. B780 (2018) 631-637, G. Barenboim, CAT, M. Tórtola

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- The bound on both mass splittings is better than the one of the kaons
- We want to see, if DUNE can improve some of these bounds

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- We use disappearance and appearance channels
- Matter effects are taken into account



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- To do so we compute as before

$$\chi^2(\Delta x) = \chi^2(|x - \overline{x}|) = \chi^2(x) + \chi^2(\overline{x})$$

being x any of the oscillation parameters

• The parameters of oscillations to create the data are

parameter	value
Δm_{21}^2	$7.56 \times 10^{-5} \mathrm{eV}^2$
Δm^2_{31}	$2.55\times 10^{-3} \mathrm{eV}^2$
$\sin^2 heta_{12}$	0.321
$\sin^2 \theta_{23}$	0.43,0.50,0.60
$\sin^2 heta_{13}$	0.02155
δ	1.50π

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- We perform a scan over the (2 times) 4dimensional parameter-space
- In neutrino mode $\sin^2 \theta_{13}$ is left free, but in antineutrino mode we put a prior on $\sin^2 \overline{\theta}_{13}$

• There is no sensitivity to $\Delta \delta$ and $\Delta \sin^2 \theta_{13}$



• This changes in the case of $\Delta(\Delta m_{31}^2)$ and $\Delta \sin^2 \theta_{23}$





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- It could improve the current limits by one order of magnitude
- We could obtain

 $\Delta(\Delta m_{31}^2) < 8.1 \times 10^{-5} \mathrm{eV}^2$

at 3σ C.L.



 For the atmospheric angle we obtain increasing sensitivity for maximal mixing









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- If CPT is not conserved this leads to impostor (fake) solutions in the fits
- To perform the standard fit you would calculate

$$\chi^2_{\rm total} = \chi^2(\nu) + \chi^2(\overline{\nu})$$

and then minimize this function

• This was done for $\sin^2 \theta_{23} = 0.5$, $\sin^2 \overline{\theta}_{23} = 0.43$

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A special case: Probing the T2K results



• T2K studied neutrino and antineutrino oscillations separated

 $\sin^2 \theta_{23} = 0.51, \quad \Delta m_{32}^2 = 2.53 \times 10^{-3} \text{eV}^2$ $\sin^2 \overline{\theta}_{23} = 0.42, \quad \Delta \overline{m}_{32}^2 = 2.55 \times 10^{-3} \text{eV}^2$

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Results are consistent with CPT conservation



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• We assumed these values to be true and simulated DUNE with parameters

parameter	value
Δm_{31}^2	$2.60 \times 10^{-3} \mathrm{eV}^2$
$\Delta \overline{m}_{31}^2$	$2.62 \times 10^{-3} \mathrm{eV}^2$
$\sin^2 heta_{23}$	0.51
$\sin^2\overline{\theta}_{23}$	0.42
$\Delta m_{21}^2, \Delta \overline{m}_{21}^2$	$7.56\times 10^{-5}\mathrm{eV}^2$
$\sin^2 \theta_{12}, \sin^2 \overline{\theta}_{12}$	0.321
$\sin^2 \theta_{13}, \sin^2 \overline{\theta}_{13}$	0.02155
$\delta,\overline{\delta}$	1.50π

• We find that, if these values turn out to be the true values, DUNE would measure CPT violation at more than 3σ confidence level



- The good determination of $\overline{\theta}_{13}$ helps in the determination of $\overline{\delta}$





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- For the other two parameters it is the other way around
- Octant for antineutrinos is resolved at more than 3σ confidence level

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• Mass splittings are consistent with CPT conservation, atmospheric angles are not

Would such a result really indicate a violation of CPT invariance?

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- The effective 2-neutrino Hamiltonian is given by

$$\mathcal{H}_F = \frac{1}{2E} \left\{ U \begin{pmatrix} 0 & 0 \\ 0 & \Delta m^2 \end{pmatrix} U^{\dagger} + A_{CC} \begin{pmatrix} \epsilon_{\mu\mu}^m & \epsilon_{\mu\tau}^m \\ \epsilon_{\mu\tau}^{m*} & \epsilon_{\tau\tau}^m \end{pmatrix} \right\}$$

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• The survival probability in matter is then

$$P_{\mu\mu} = 1 - \sin^2 2\tilde{\theta} \sin^2 \left(\frac{\Delta \tilde{m}^2}{4E}\right)$$

• NSI affect different neutrinos and antineutrinos

$$\Delta m_{\nu}^{2} \cos 2\theta_{\nu} = \Delta m^{2} \cos 2\theta + \epsilon_{\tau\tau}^{m} A$$
$$\Delta m_{\nu}^{2} \sin 2\theta_{\nu} = \Delta m^{2} \sin 2\theta + 2\epsilon_{\mu\tau}^{m} A$$

$$\Delta m_{\overline{\nu}}^2 \cos 2\theta_{\overline{\nu}} = \Delta m^2 \cos 2\theta - \epsilon_{\tau\tau}^m A$$
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- The apparent CPT-violating result from T2K might be induced by NSI
- We checked this for DUNE!
CPT versus NSI

• Perform the analysis exactly as before, but add also the two NSI parameters $\epsilon^m_{\mu\tau}, \epsilon^m_{\tau\tau}$

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- This time we include only the disappearance channel
- At the end sum the χ^2 grids and marginalize over all parameters, except the ones of interest

CPT versus NSI

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- Nothing special in the case of $\epsilon^m_{\mu\tau}$



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- Indeed, the spectra for the NSI best fit and CPT-violating parameters are the same
- Anyway, this value is excluded at close to 5σ



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- If CPT is violated in nature we are committing errors in our analysis by combining neutrino with antineutrino results
- If the results measured by T2K turn out to be true, DUNE would measure CPT violation at more than 4σ
- NSI could not explain the apparent CPT violation measured by T2K

