

STERILE NEUTRINO SEARCHES

JOSU HERNANDEZ-GARCIA

NuFact 2018 | WG5



SISSA
40!



HORIZON
2020

elusiVes

Based on

- JHEP 04 (2017) 153. MB, PC, EFM, JHG & JLP.
- arXiv 1803.02362. MB, EFM, JG, JHG & JS.

In collaboration with



Mattias Blennow



Pilar Coloma



Enrique Fernandez-
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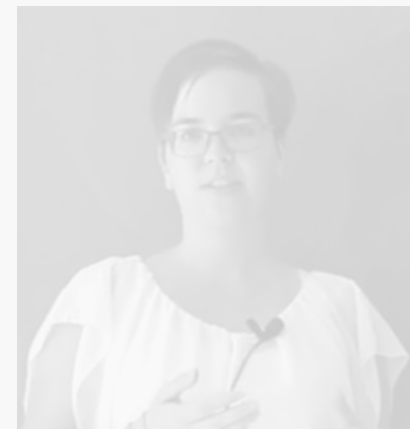
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INTRODUCTION

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The SM is successful and **predicts** a wide variety of phenomena that has been tested experimentally to an incredible accuracy.

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However, there are some **open problems** \Rightarrow **open opportunities**

Represent our **best window** for New Physics

INTRODUCTION: SM OPEN PROBLEMS

- Dark Matter
- Matter-antimatter asymmetry (BAU)
- Neutrino masses
- Flavor Puzzle
- Hierarchy problem
- Strong CP , Unification, ...

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- Dirac neutrino masses

All fermions get masses through the **Yukawa interaction**

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Not present in the SM

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- Majorana neutrino masses

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$$\frac{1}{2} c_{\alpha\beta}^{d=5} \left(\overline{\ell_{\alpha L}^c} \tilde{\phi}^* \right) \left(\tilde{\phi}^\dagger \ell_{\beta L} \right) + \text{h.c.} \xrightarrow[\text{EWSB}]{\text{after}} \frac{v_{\text{EW}}^2}{2} c^{d=5} \overline{\nu}_L^c \nu_L$$

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$d = 5 \Rightarrow$ Is SM low energy remnant of higher energy theory?

And therefore neutrinos are **strictly massless** in the SM.

The SM must be **extended** to account for neutrino oscillations.

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At *tree level* the *3 possible* realizations of the Weinberg op. are

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P. Minkowski, Phys. Lett. **B67** (1977) 421.

T. Yanagida. Proceedings of the Workshop on the Baryon Number of the Universe.

M. Gell-Mann, P. Ramond, and R. Slansky, Print-80-0576 (CERN).

R. N. Mohapatra and G. Senjanovic, Phys. Rev. Lett. **44** (1980) 912.

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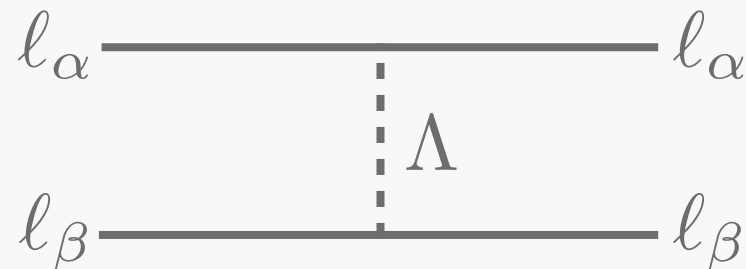
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M. Magg and C. Wetterich, Phys. Lett. **94B** (1980) 61–64.

J. Schechter and J. W. F. Valle, Phys. Rev. **D22** (1980) 2227.

C. Wetterich, Nucl. Phys. **B187** (1981) 343–375.

G. Lazarides, Q. Shafi, and C. Wetterich, Nucl. Phys. **B181** (1981) 287–300.

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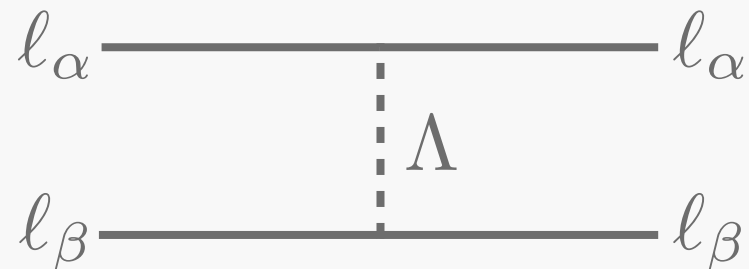
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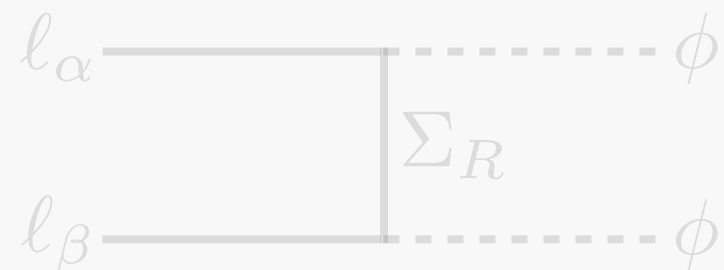
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INTRODUCTION: SM + TYPE I SEESAW

The SM is **enlarged** by an arbitrary number of N_R

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + i\overline{N_R}\not{\partial}N_R - \left(\frac{1}{2}\overline{N_{Ri}}(M_N)_{ij}N_{Rj}^c + (y_N)_{i\alpha}\overline{N_{Ri}}\phi^\dagger\ell_{L\alpha} \right) + \text{h.c.}$$

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Yukawa interaction

Dirac neutrino masses

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Allowed Majorana mass for N_R

New Physics **scale**

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Experimental verification **needed**.

INTRODUCTION: SM + TYPE I SEESAW

The neutrino mass matrix

$$U^T \begin{pmatrix} 0 & m_D^T \\ m_D & M_N \end{pmatrix} U = \begin{pmatrix} m & 0 \\ 0 & M \end{pmatrix}$$

diagonalized by the full **Unitary** mixing matrix U

$$U = \begin{pmatrix} N & \Theta \\ R & S \end{pmatrix}$$

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$$U = \begin{pmatrix} \text{light} & \text{heavy} \\ \text{active} & \text{sterile} \\ N & \Theta \\ R & S \end{pmatrix}$$

with $N \equiv (I - \alpha) U_{\text{PMNS}}$ and α lower triangular matrix

$$\alpha = \begin{pmatrix} \alpha_{ee} & 0 & 0 \\ \alpha_{\mu e} & \alpha_{\mu\mu} & 0 \\ \alpha_{\tau e} & \alpha_{\tau\mu} & \alpha_{\tau\tau} \end{pmatrix} \simeq \begin{pmatrix} \sum_{i=4}^n \frac{1}{2} |\Theta_{ei}|^2 & 0 & 0 \\ \sum_{i=4}^n \Theta_{\mu i} \Theta_{ei}^* & \sum_{i=4}^n \frac{1}{2} |\Theta_{\mu i}|^2 & 0 \\ \sum_{i=4}^n \Theta_{\tau i} \Theta_{ei}^* & \sum_{i=4}^n \Theta_{\tau i} \Theta_{\mu i}^* & \sum_{i=4}^n \frac{1}{2} |\Theta_{\tau i}|^2 \end{pmatrix}$$

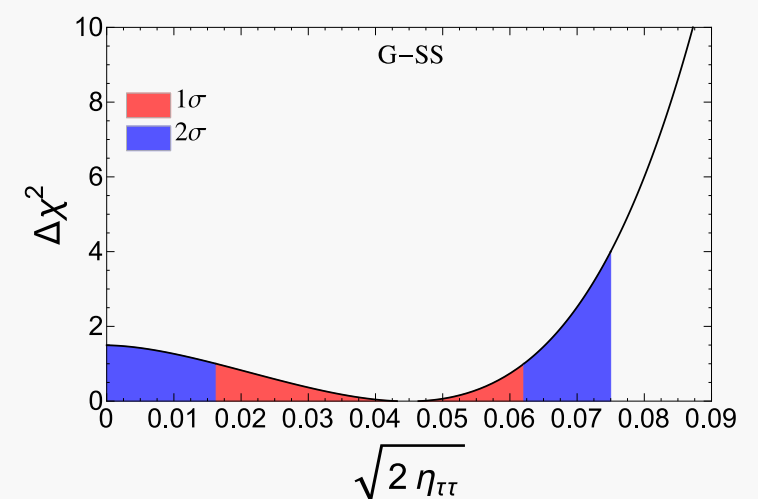
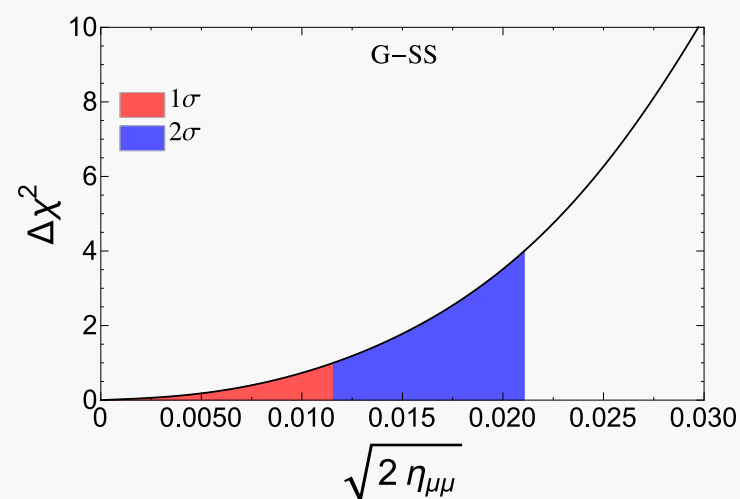
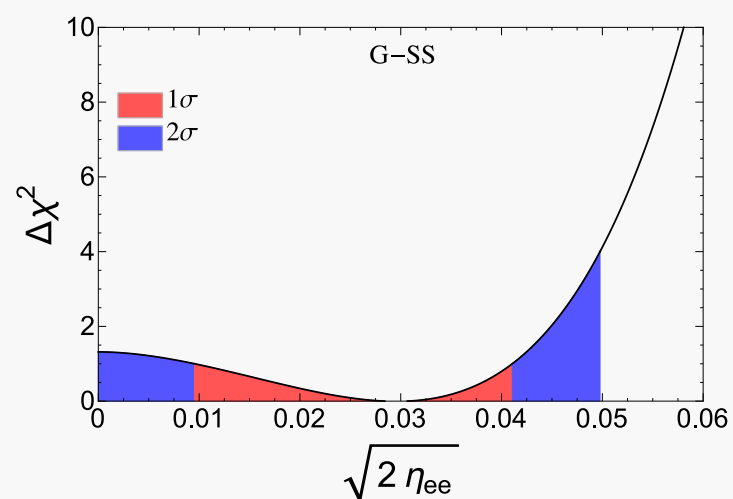
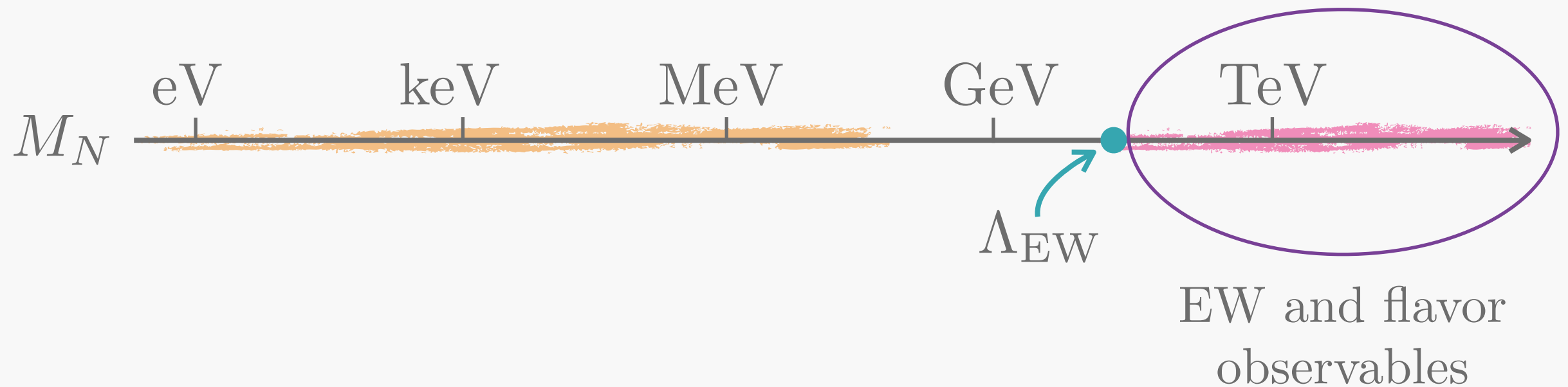
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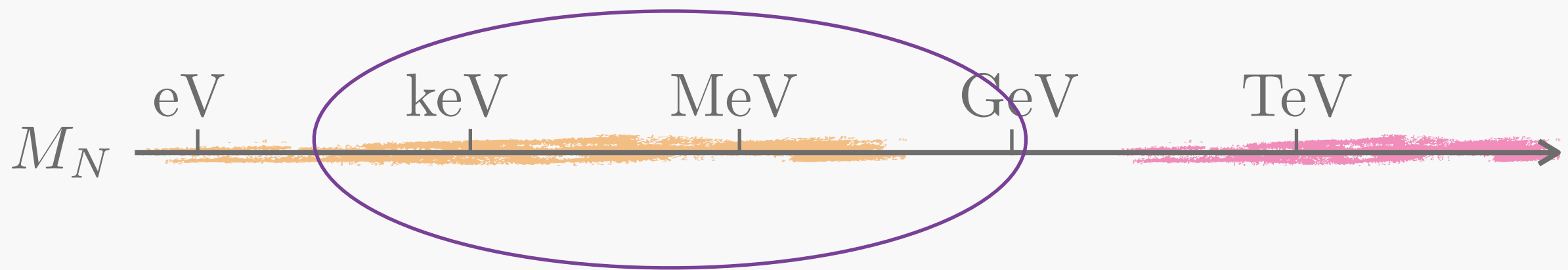


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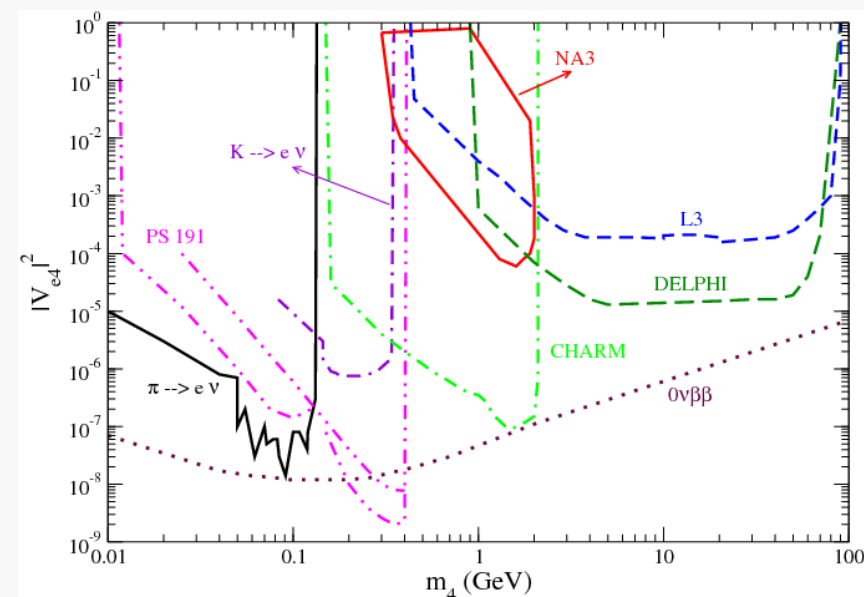
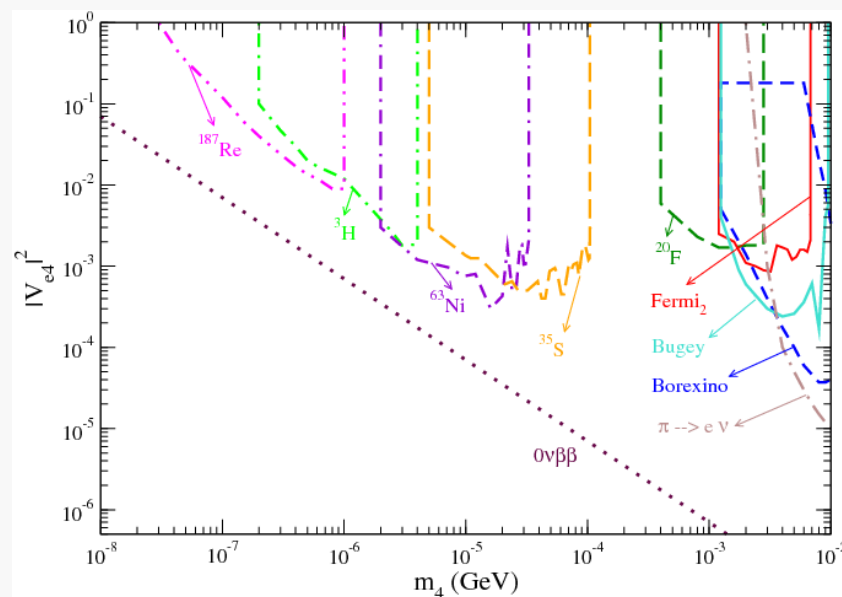


$$\theta \sim 10^{-2}$$

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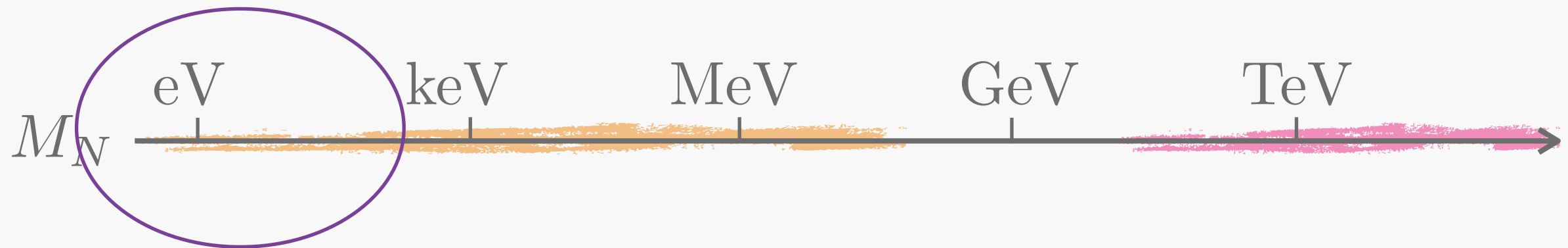


Kinks in β -decay and peaks
in meson decay searches

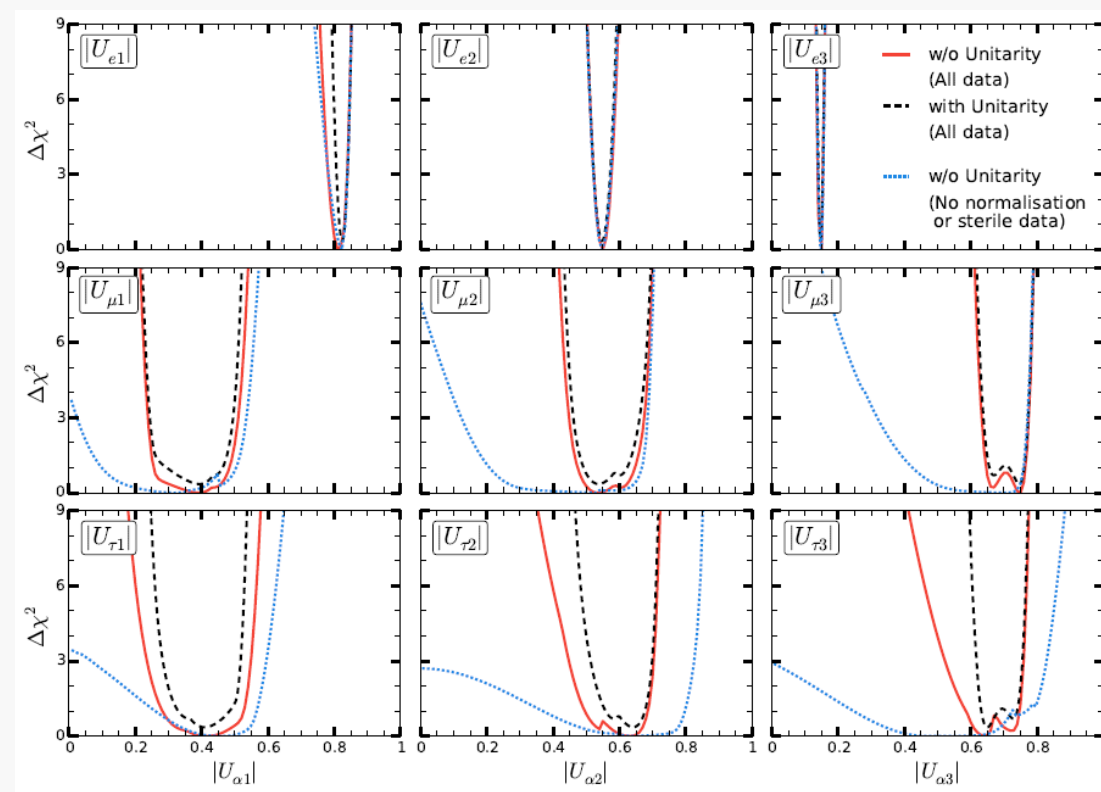


$$\theta \sim 10^{-4}$$

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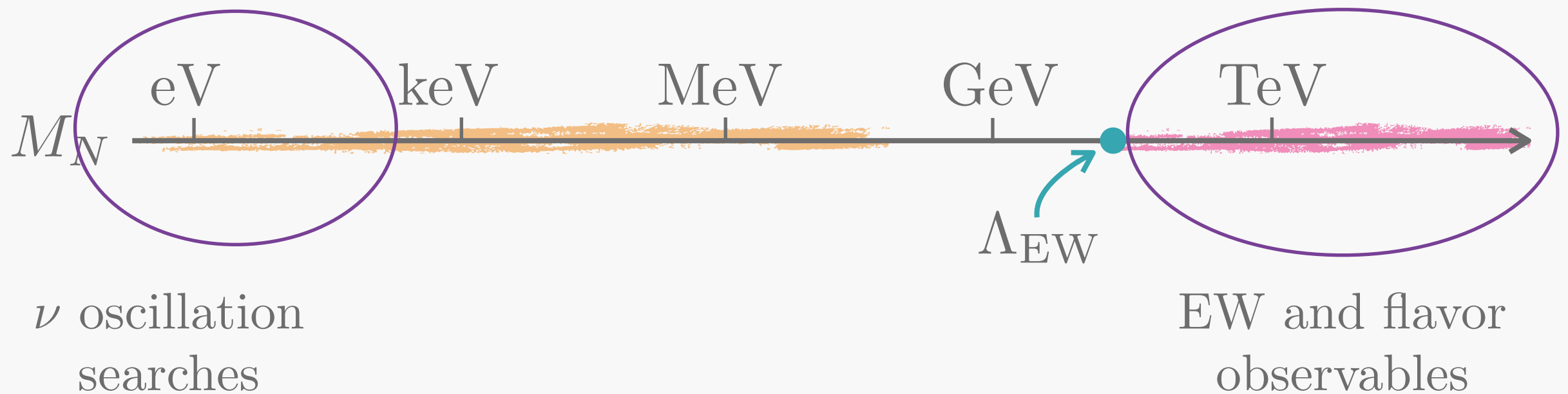


ν oscillation
searches



$$\theta \sim 10^{-1}$$

INTRODUCTION: SM + TYPE I SEESAW



At some level, both limits

- **Very high** ($M_N > \Lambda_{EW}$) neutrino \rightarrow Non-Unitarity
 - **Very light** ($M_N < \text{keV}$) neutrino \rightarrow sterile neutrinos
- will impact neutrino oscillation searches.

NON-UNITARITY VS STERILE NEUTRINOS AT DUNE

NON-UNITARITY VS STERILE NEUTRINOS

$$P_{\alpha\beta} = \sum_{i,j} U_{\alpha i} U_{\beta i}^* U_{\alpha j}^* U_{\beta j} e^{-i \frac{\Delta m_{ij}^2 L}{2E}} \quad \text{with} \quad U = \begin{pmatrix} \overset{\text{light}}{N} & \overset{\text{heavy}}{\Theta} \\ R & S \end{pmatrix} \begin{matrix} \text{active} \\ \text{sterile} \end{matrix}$$

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Averaged-out limit $\frac{\Delta m_{iJ}^2 L}{2E} \gg 1$

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Averaged-out limit and at LO

NON-UNITARITY VS STERILE NEUTRINOS

Non-Unitarity
(very **high** masses) = Averaged-out
sterile neutrinos
(very **light** masses)

$$P_{\alpha\beta} = \sum_{i,j} N_{\alpha i} N_{\beta i}^* N_{\alpha j}^* N_{\beta j} e^{-i \frac{\Delta m_{ij}^2 L}{2E}} \quad \text{at LO}$$

For $\frac{\Delta m_{ij}^2}{2E} \gg V_{\text{CC}}, V_{\text{NC}}$ this holds in matter.

However the **bounds** on the mixing in both limits are **different**.

NON-UNITARITY VS STERILE NEUTRINOS

Present bounds on the two limits

- Non-Unitarity
for $m > \Lambda_{\text{EW}}$ (at 2σ)

$$\alpha_{ee} \quad 1.3 \cdot 10^{-3}$$

$$\alpha_{\mu\mu} \quad 2.2 \cdot 10^{-4}$$

$$\alpha_{\tau\tau} \quad 2.8 \cdot 10^{-3}$$

$$|\alpha_{\mu e}| \quad 6.8 \cdot 10^{-4}$$

$$|\alpha_{\tau e}| \quad 2.7 \cdot 10^{-3}$$

$$|\alpha_{\tau\mu}| \quad 1.2 \cdot 10^{-3}$$

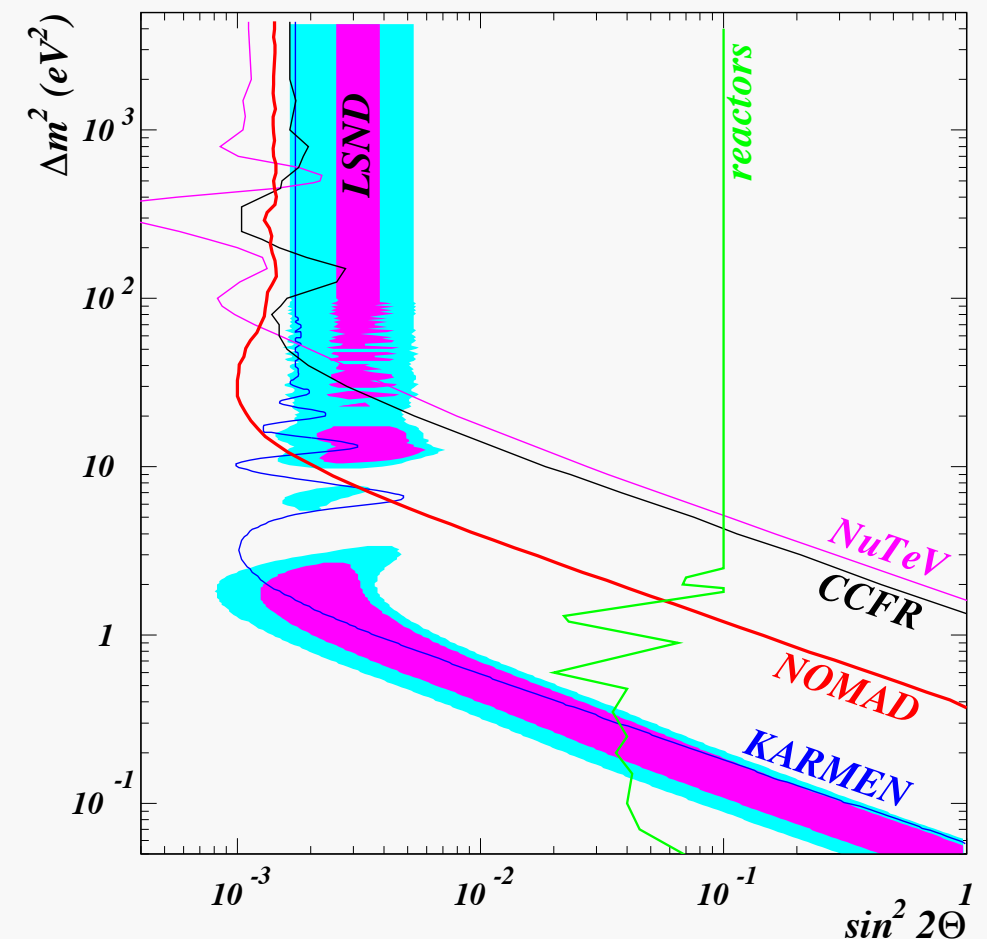
NON-UNITARITY VS STERILE NEUTRINOS

Present bounds on the two limits

- Non-Unitarity
for $m > \Lambda_{EW}$ (at 2σ)

α_{ee}	$1.3 \cdot 10^{-3}$
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- Averaged-out sterile neutrinos



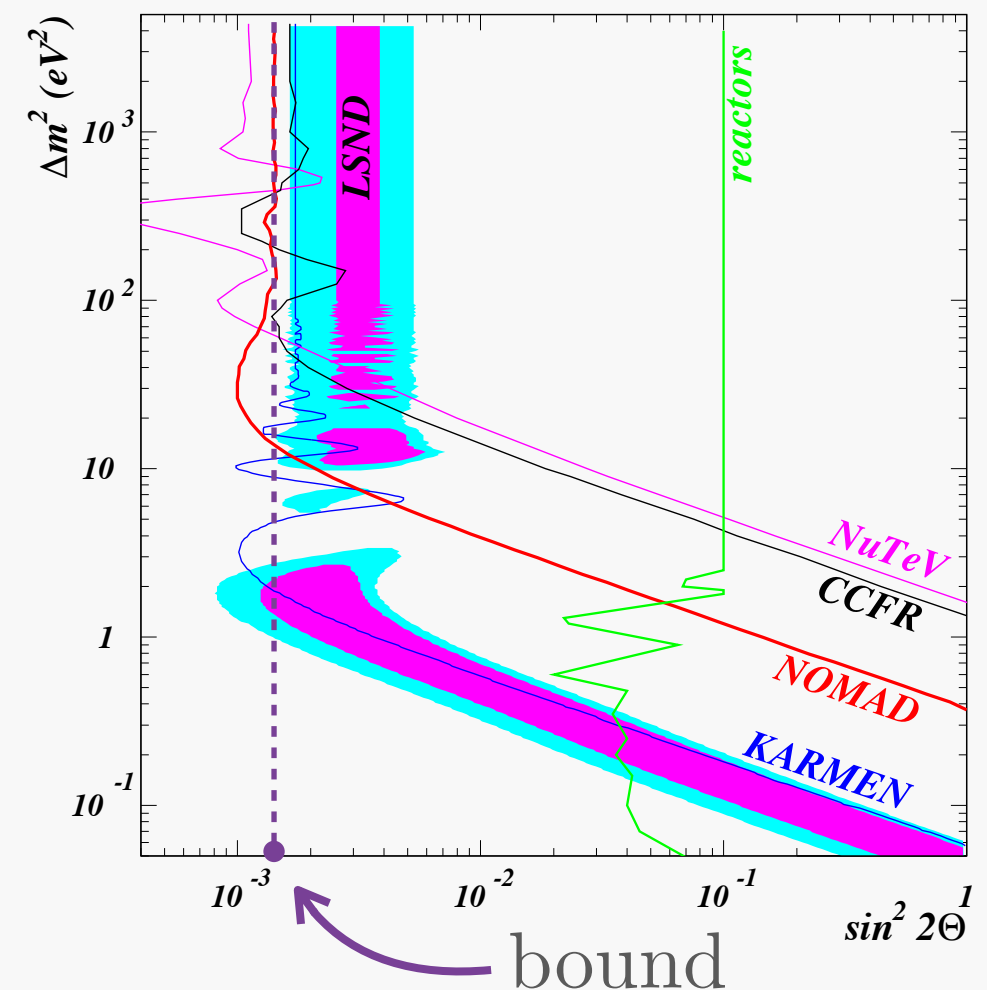
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$$\alpha_{ee} \quad 2.4 \cdot 10^{-2} \text{ [1]}$$

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$$\alpha_{\tau\tau} \quad 1.0 \cdot 10^{-1} \text{ [3]}$$

$$|\alpha_{\mu e}| \quad 2.5 \cdot 10^{-2} \text{ [4]}$$

$$|\alpha_{\tau e}| \quad 6.9 \cdot 10^{-2}$$

$$|\alpha_{\tau\mu}| \quad 1.2 \cdot 10^{-2} \text{ [5]}$$

[1] Bugey-3 [2] SK [3] MINOS [4,5] NOMAD

NON-UNITARITY VS STERILE NEUTRINOS

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too small to be tested at
 ν oscillation experiments

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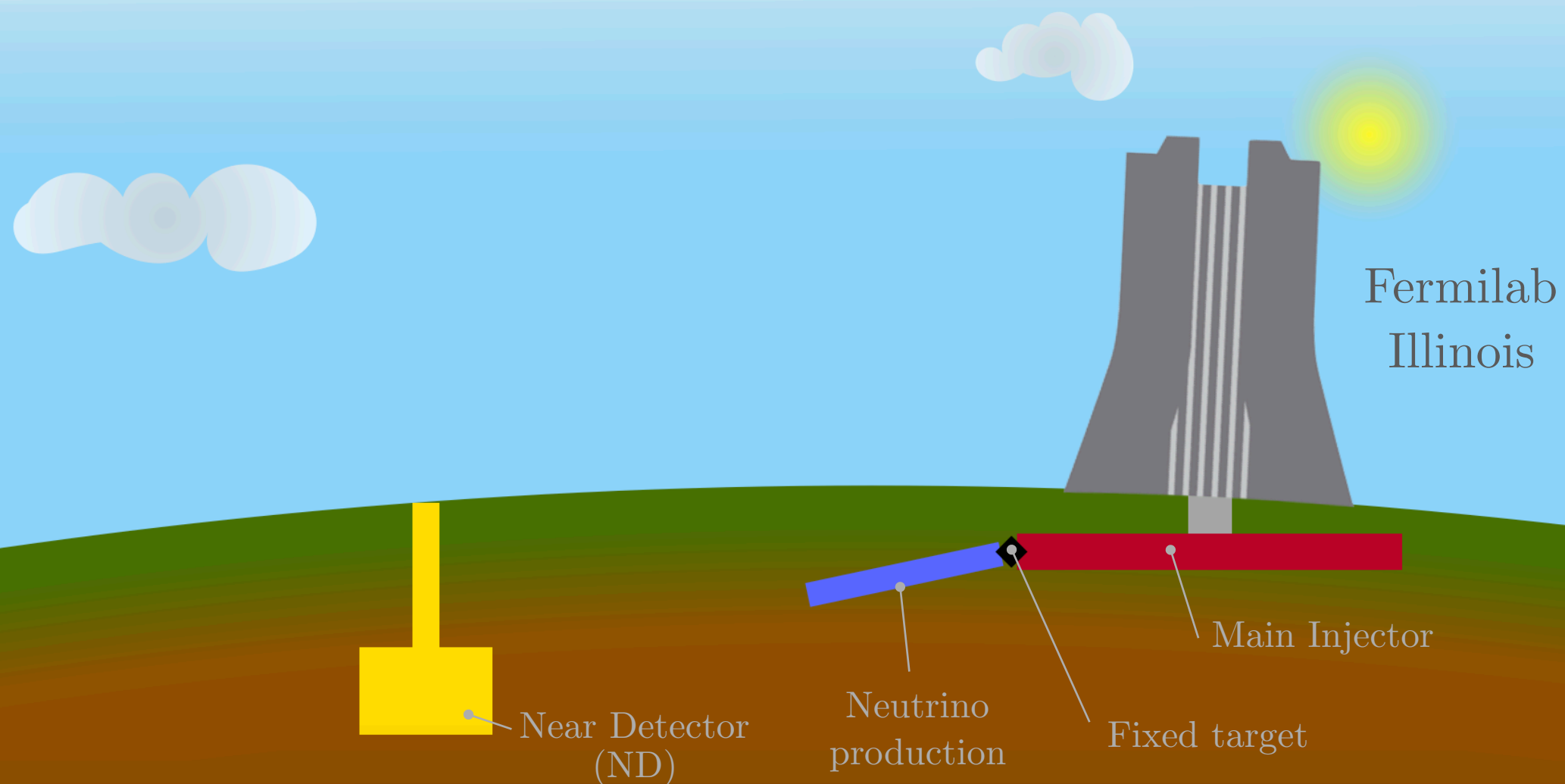
$$|\alpha_{\tau\mu}| \quad 1.2 \cdot 10^{-2} \text{ [5]}$$

could be probed??

NON-UNITARITY VS STERILE ν AT DUNE

What is DUNE?

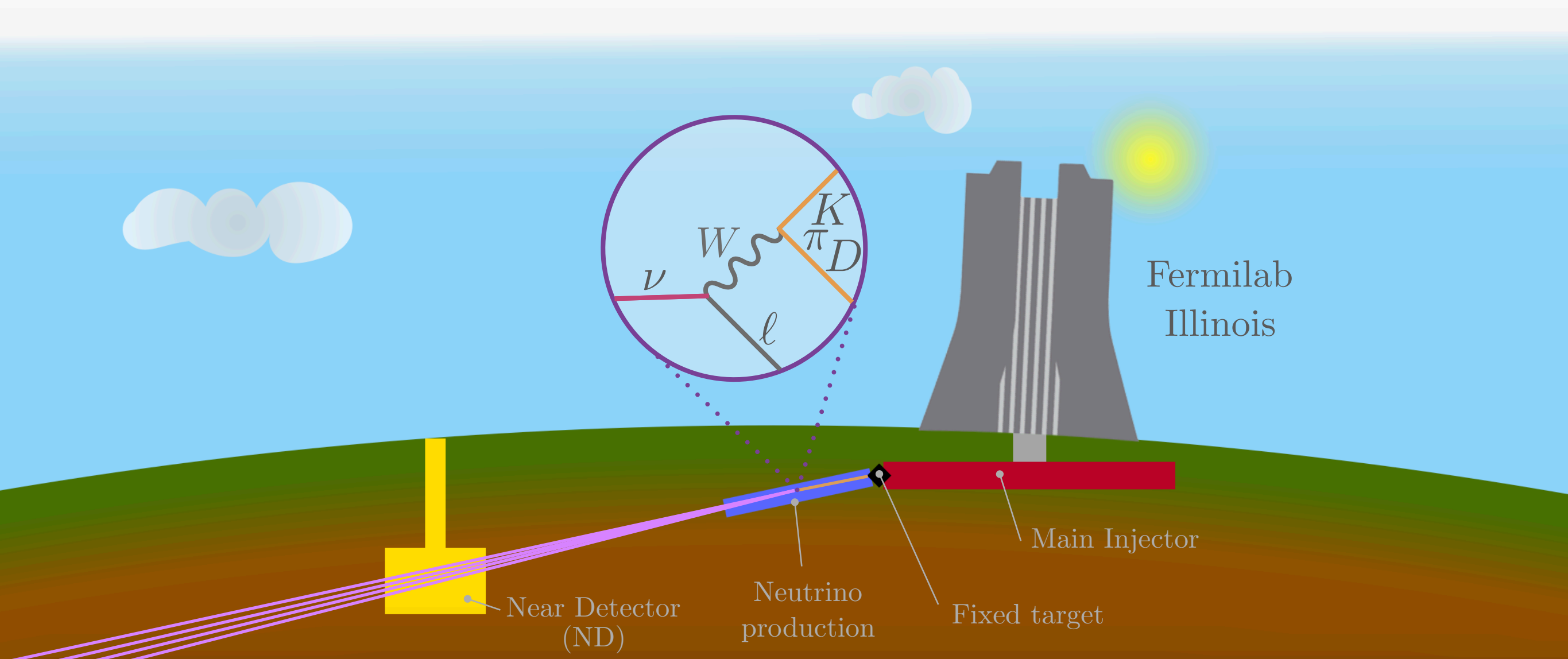
Deep Underground Neutrino Experiment



NON-UNITARITY VS STERILE ν AT DUNE

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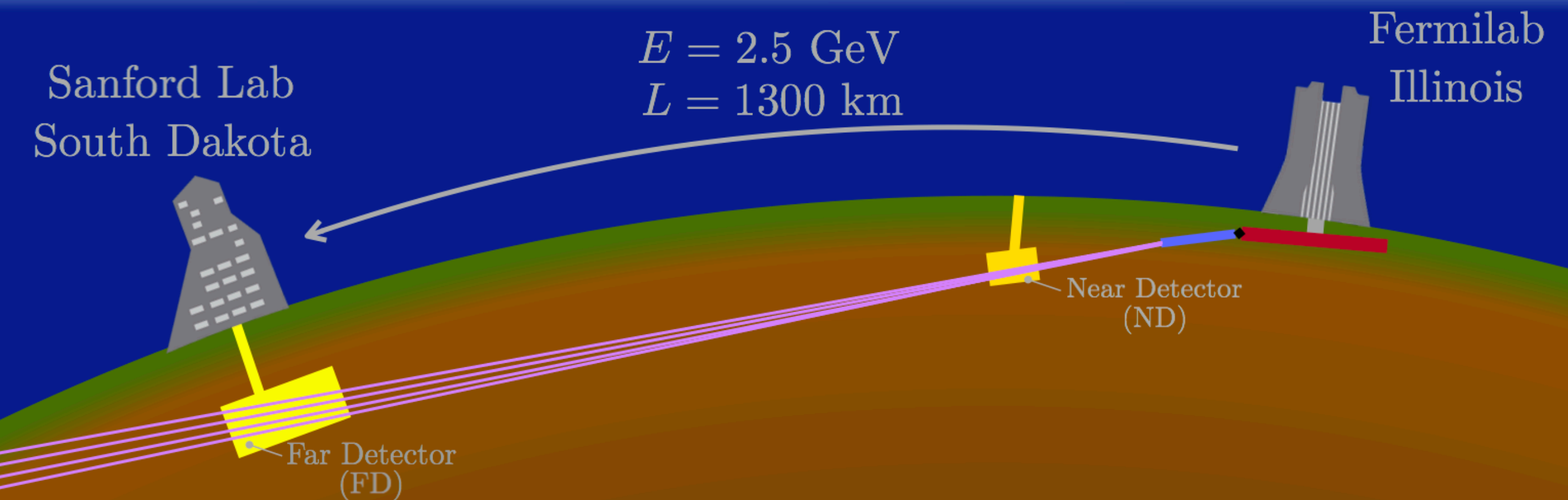
Deep Underground Neutrino Experiment



NON-UNITARITY VS STERILE ν AT DUNE

What is DUNE?

Deep Underground Neutrino Experiment



NON-UNITARITY VS STERILE ν AT DUNE

The role of the Near Detector (ND)

If flux and cross section at FD **normalized** with ND data

$$\overline{P}_{\alpha\beta} = \frac{P_{\alpha\beta}(L_{\text{FD}})}{P_{\alpha\beta}(L_{\text{ND}})}$$

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Non-Unitarity = sterile ν
osc. **averaged** at the ND

DUNE setup $\rightarrow \Delta m^2 \gtrsim 100 \text{ eV}^2$

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- No

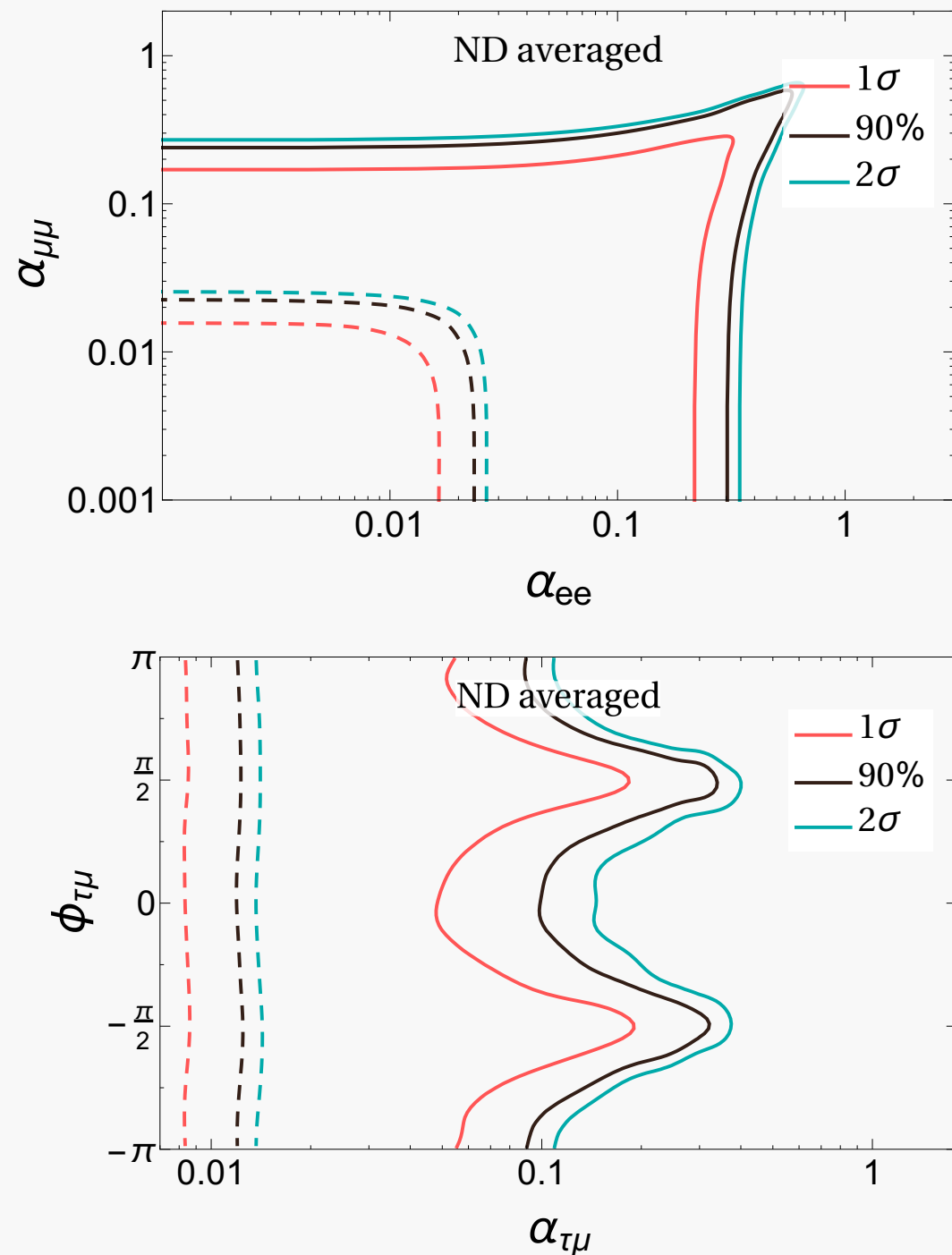
$$\overline{P}_{\alpha\beta} = \sum_{i,j} N_{\alpha i} N_{\beta i}^* N_{\alpha j}^* N_{\beta j} e^{-i \frac{\Delta m_{ij}^2 L}{2E}}$$

sterile neutrino oscillations
undeveloped at the ND

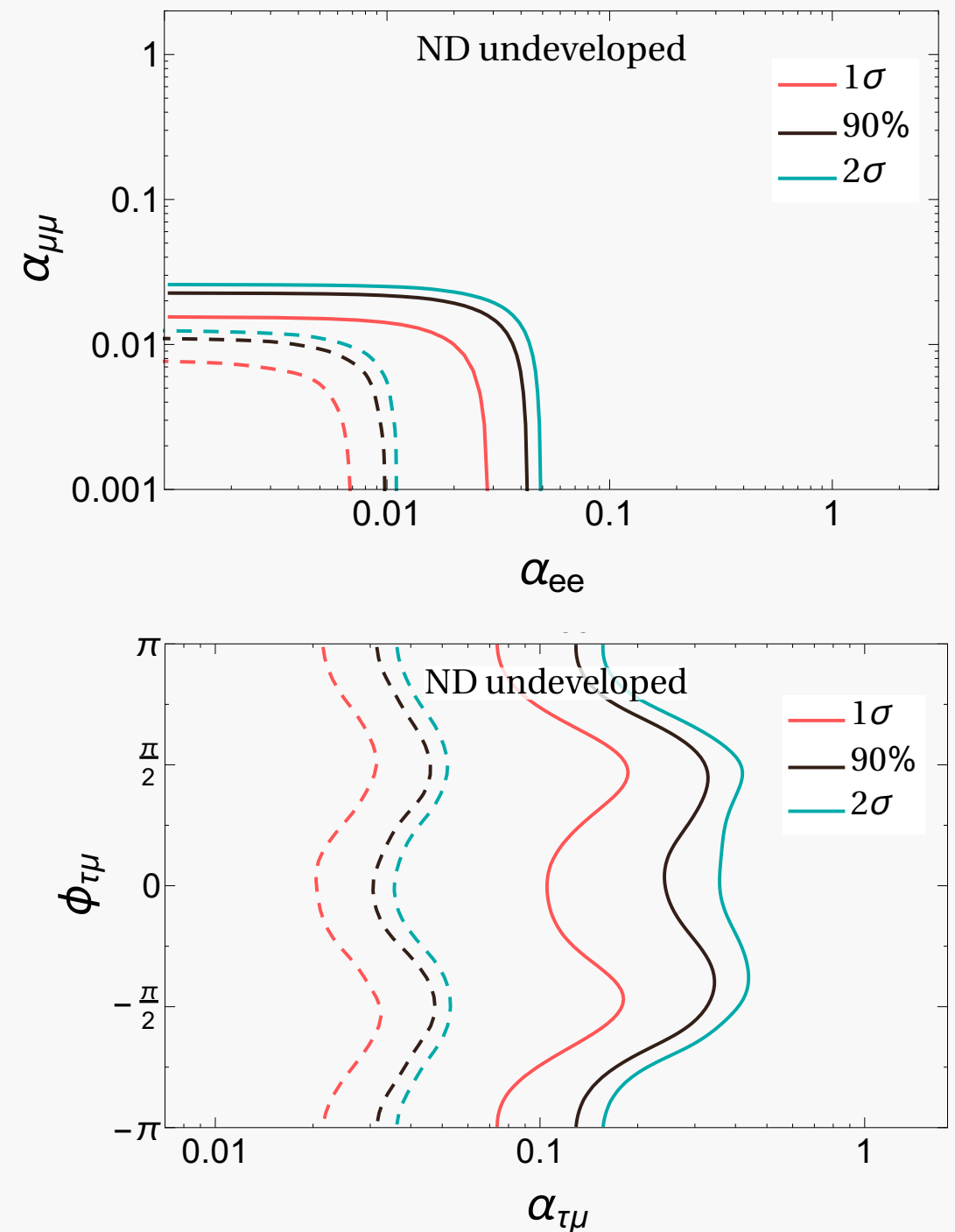
DUNE setup $\rightarrow \Delta m^2 \sim (0.1, 1) \text{ eV}^2$

NON-UNITARITY VS STERILE ν AT DUNE

- Yes \rightarrow ND averaged

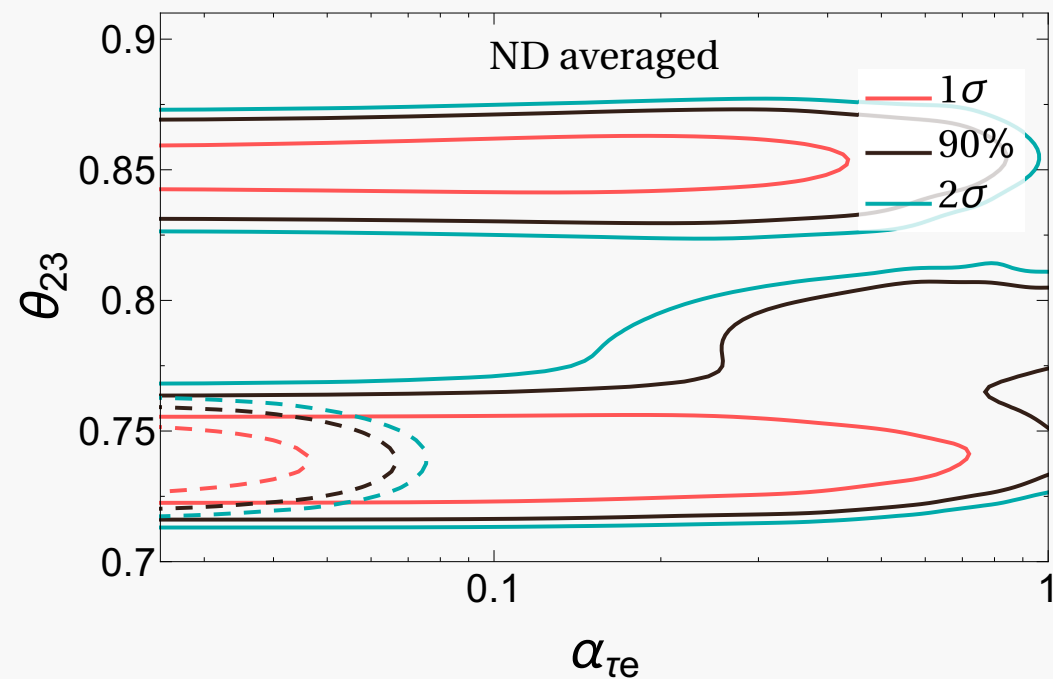
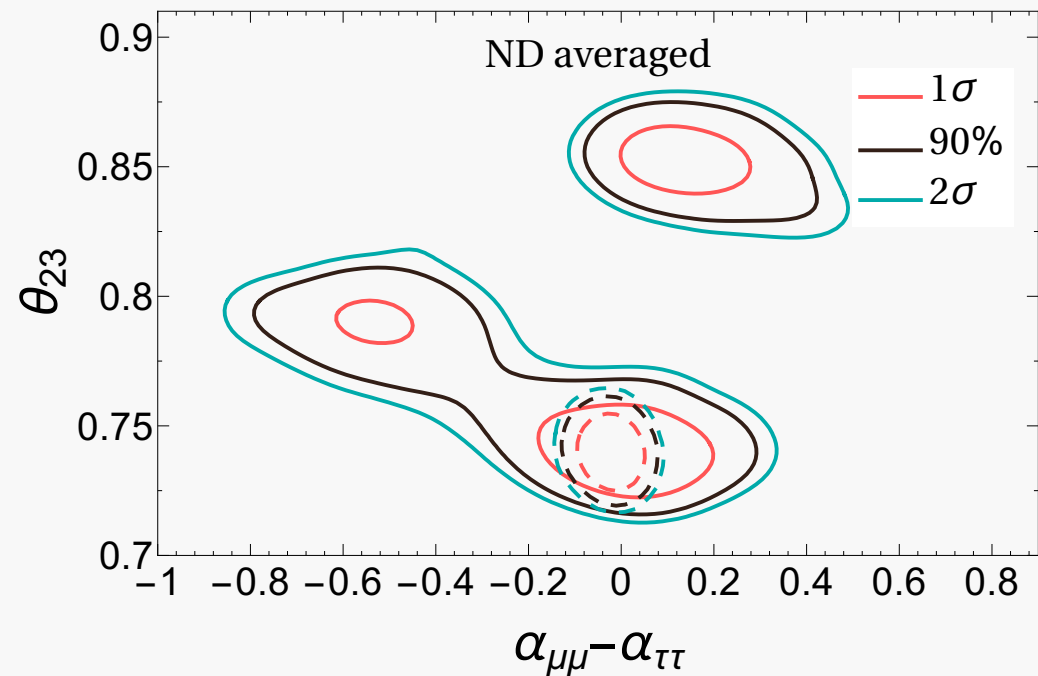


- No \rightarrow ND undeveloped

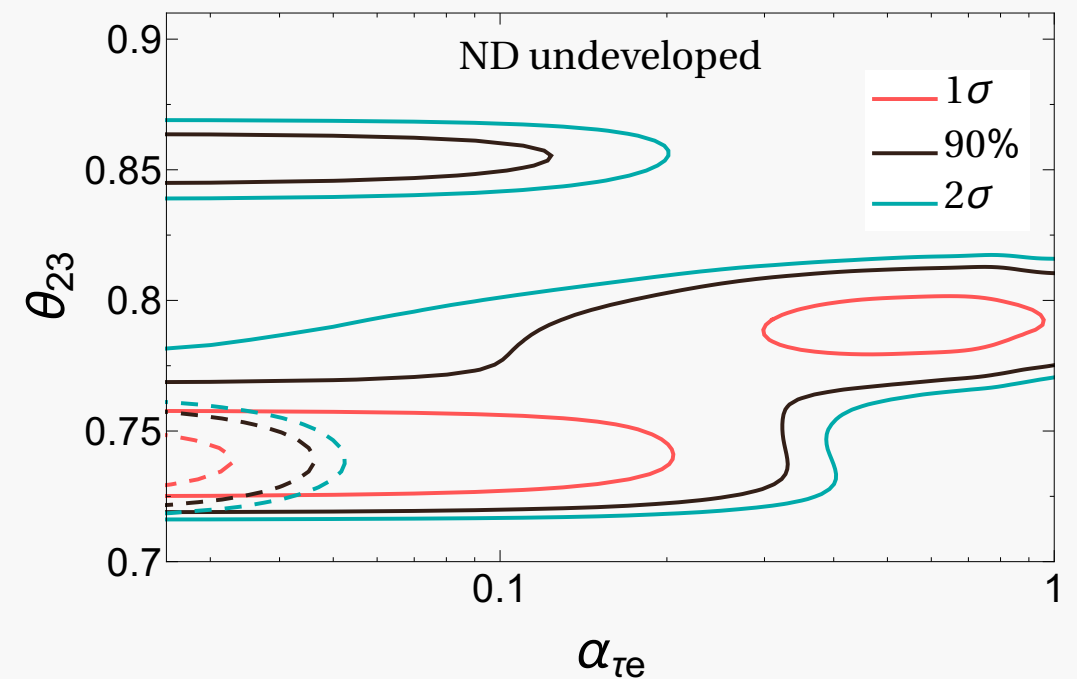
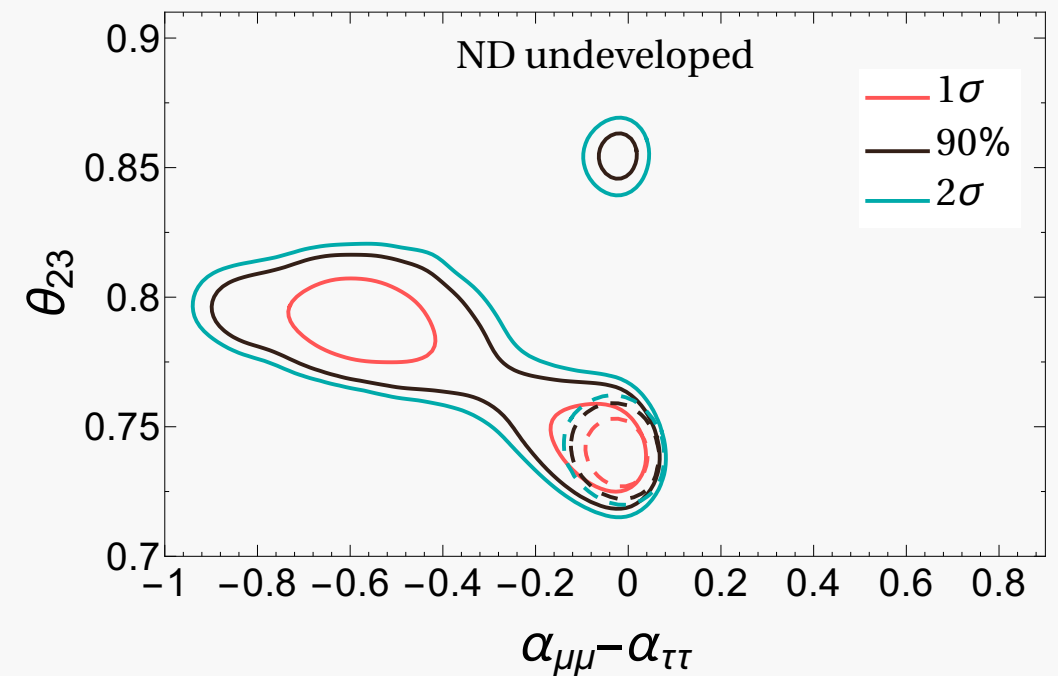


NON-UNITARITY VS STERILE ν AT DUNE

- Yes \rightarrow ND averaged



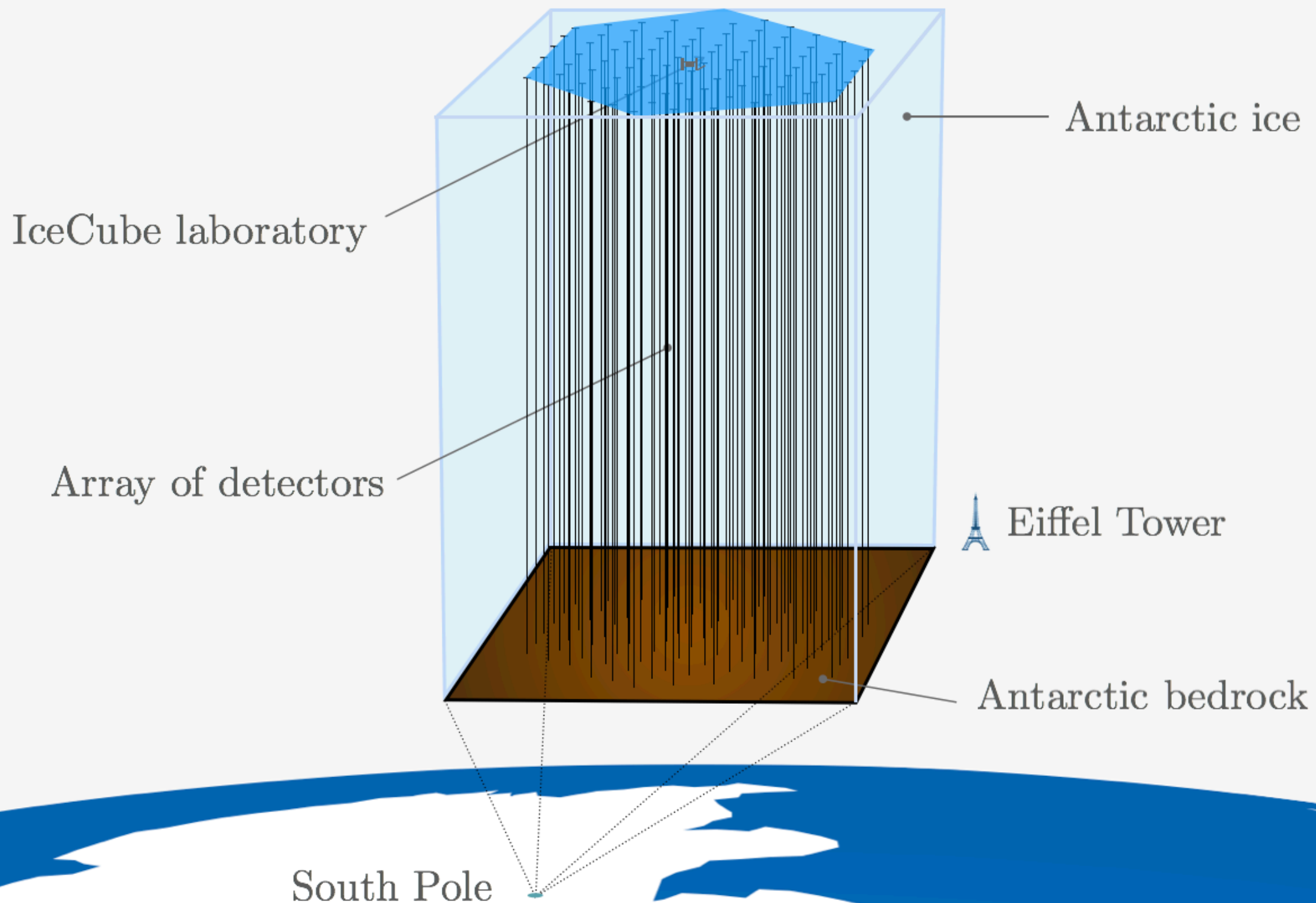
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STERILE NEUTRINOS ABOVE 10 EeV AT ICECUBE

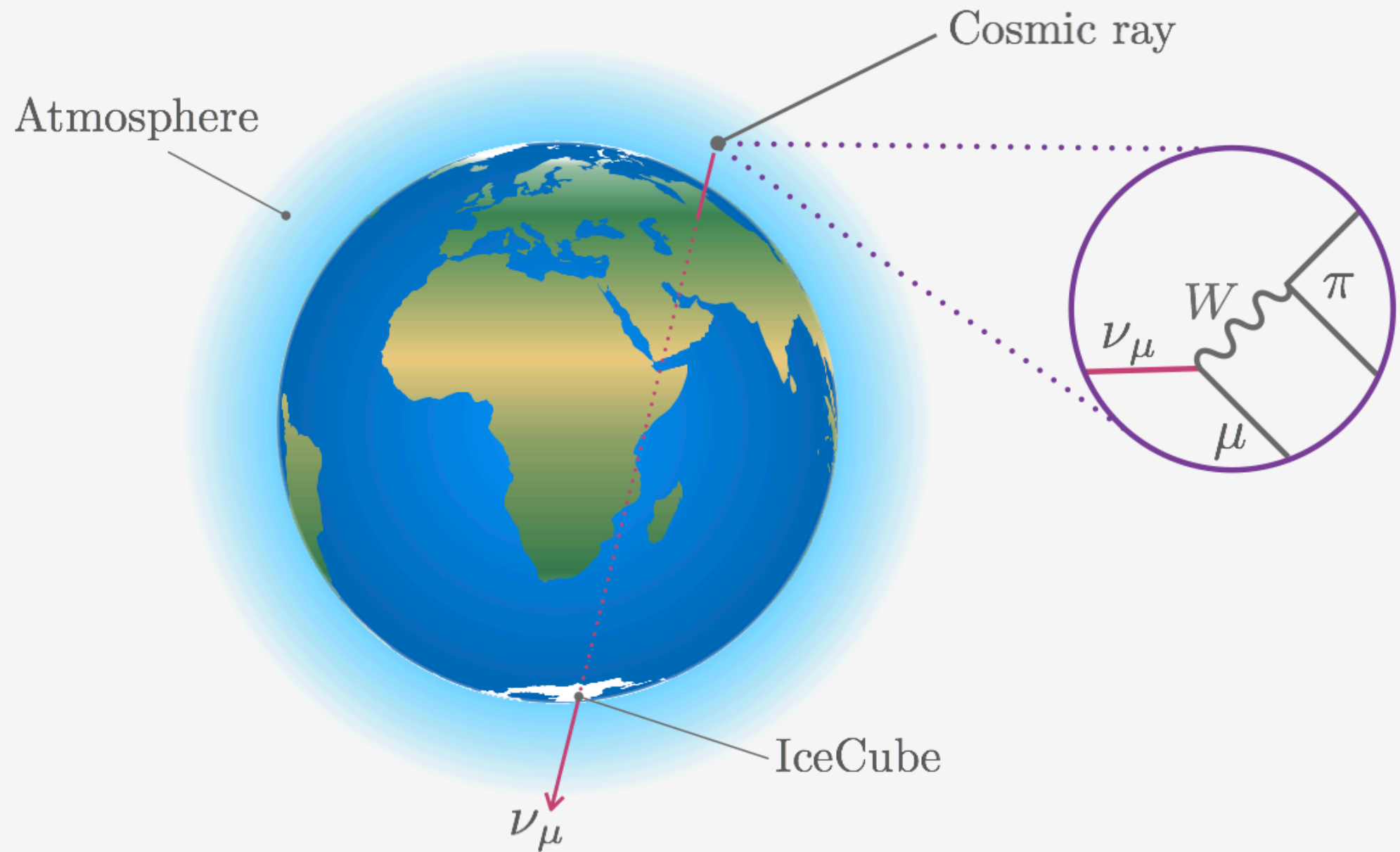
STERILE ν ABOVE 10 eV AT ICECUBE

- What is IceCube?



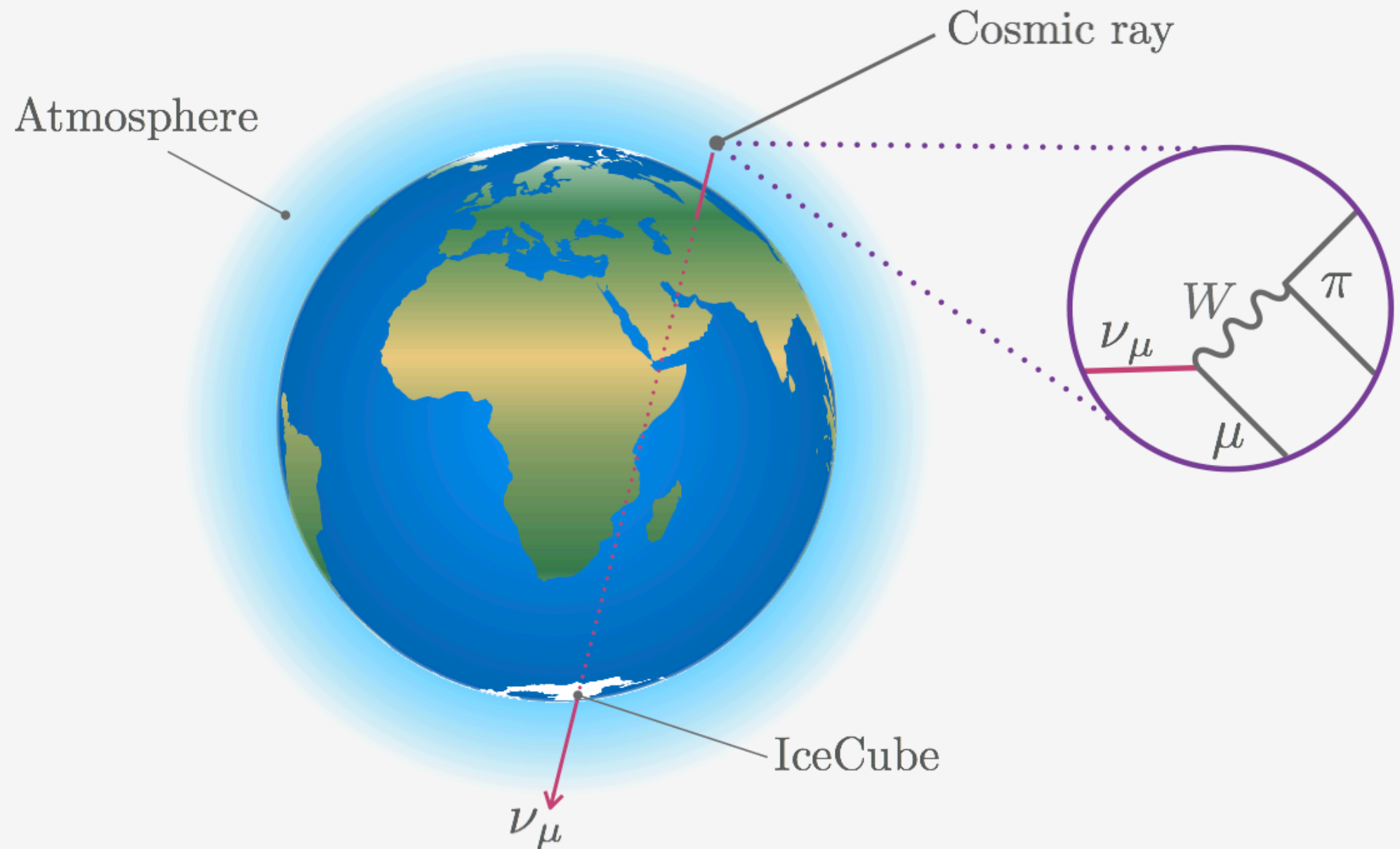
STERILE ν ABOVE 10 EeV AT ICECUBE

- What is IceCube?



STERILE ν ABOVE 10 EeV AT ICECUBE

- What is IceCube?



The ν_μ **oscillates** during its propagation

IceCube measures $P_{\mu\mu}$ with strong **matter effects**

STERILE ν ABOVE 10 eV AT ICECUBE

- The neutrino oscillation probability

We compute $\nu_\mu \rightarrow \nu_\mu$ probability $P_{\mu\mu}$ for

- small heavy-active mixing angles
- averaged-out regime \Rightarrow large Δm^2 ($\Delta m^2 \gtrsim 100 \text{ eV}^2$)
- ν_e does not participate in oscillations

$$P_{\mu\mu} = (1 - \alpha_{\mu\mu})^4 \left(1 - \sin^2(2\theta_m) \sin^2 \left(\frac{\Delta_m L}{2} \right) \right) + \sum_{s=4}^n |U_{\mu s}|^4$$

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At **leading order** in α and **neglecting** Δm_{31}^2

$$P_{\mu\mu} \simeq 1 - V_{\text{NC}}^2 |\alpha_{\tau\mu}|^2 L^2$$

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For the particular case of **just one** extra neutrino

$$P_{\mu\mu} \simeq 1 - V_{\text{NC}}^2 |U_{\tau 4}|^2 |U_{\mu 4}|^2 L^2$$

STERILE ν ABOVE 10 E ν AT ICECUBE

- Details of the analysis

The atmospheric neutrino flux has been computed with

HondaGaisser* + QGSJET II-04

The impact of different flux models has been studied.

T.K. Gaisser, T. Stanev, and S. Tilav, Front. Phys. (Beijing) **8** (2013) 748–758

S. Ostapchenko, Phys. Rev. **D83** (2011) 014018 *Gaisser-Hillas H3a correction

STERILE ν ABOVE 10 E ν AT ICECUBE

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The propagation of the neutrinos simulated using [nuSQuIDS](#).

STERILE ν ABOVE 10 E ν AT ICECUBE

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After propagating flux **for every value** of sterile ν parameter, the **expected** number of events N_i^{th} in every bin of reconstructed **zenit angle** computed using the provided MonteCarlo.

STERILE ν ABOVE 10 E ν AT ICECUBE

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After propagating flux for every value of sterile ν parameter, the expected number of events N_i^{th} in every bin of reconstructed zenith angle computed using the provided MonteCarlo.

The observable is **energy independent** \Rightarrow

- **only one** energy bin
- **40** bins for reconstructed zenith angle

STERILE ν ABOVE 10 E ν AT ICECUBE

- Details of the analysis

Log-likelihood computed

$$L = - \sum_i \left[N_i^{\text{th}} - N_i^{\text{data}} + N_i^{\text{data}} \log \left(\frac{N_i^{\text{data}}}{N_i^{\text{th}}} \right) \right]$$

reconstructed
zenit angle bins

observed

predicted

STERILE ν ABOVE 10 E ν AT ICECUBE

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Log-likelihood computed

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Minimized for nuisance parameters to include systematic errors

- uncertainty in pion-kaon ratio of the initial flux
- efficiency of the Digital Optical Modules (DOMs)
- overall flux normalization

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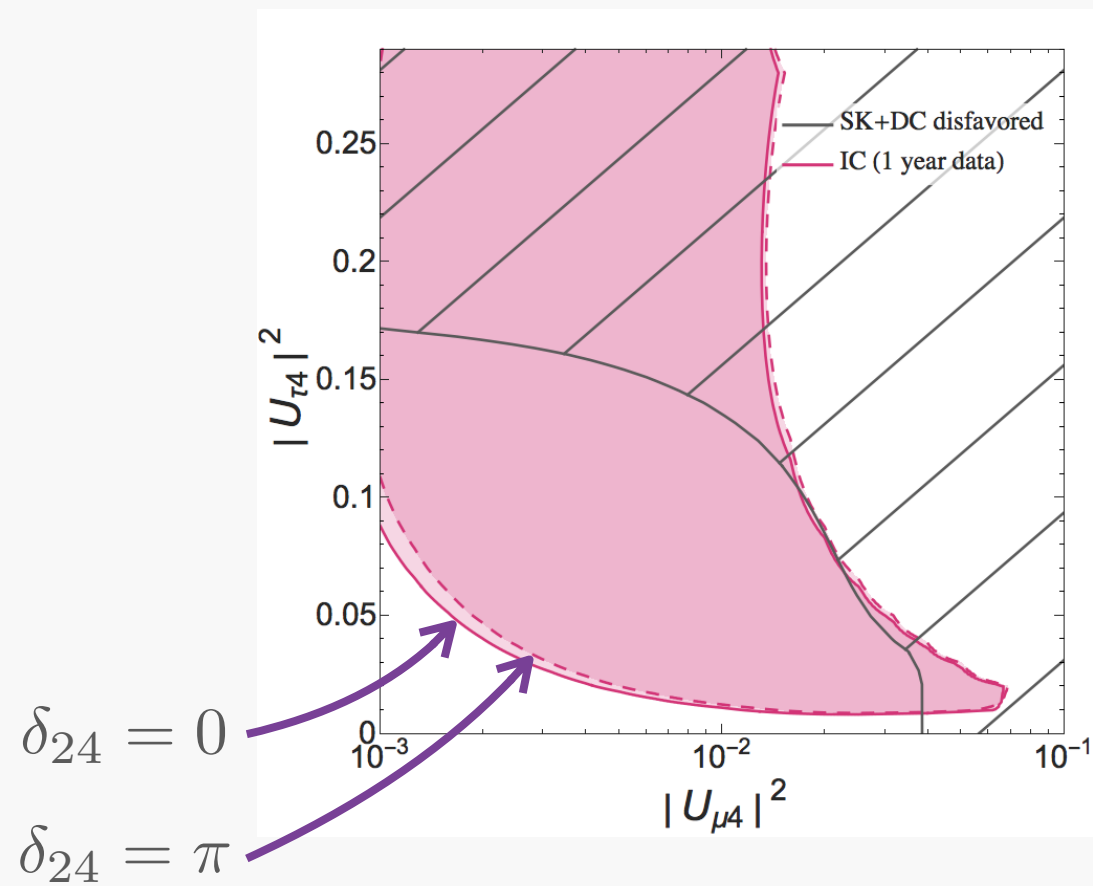
- uncertainty in pion-kaon ratio of the initial flux
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Standard osc. parameters set to actual **best-fit** values of NuFIT.

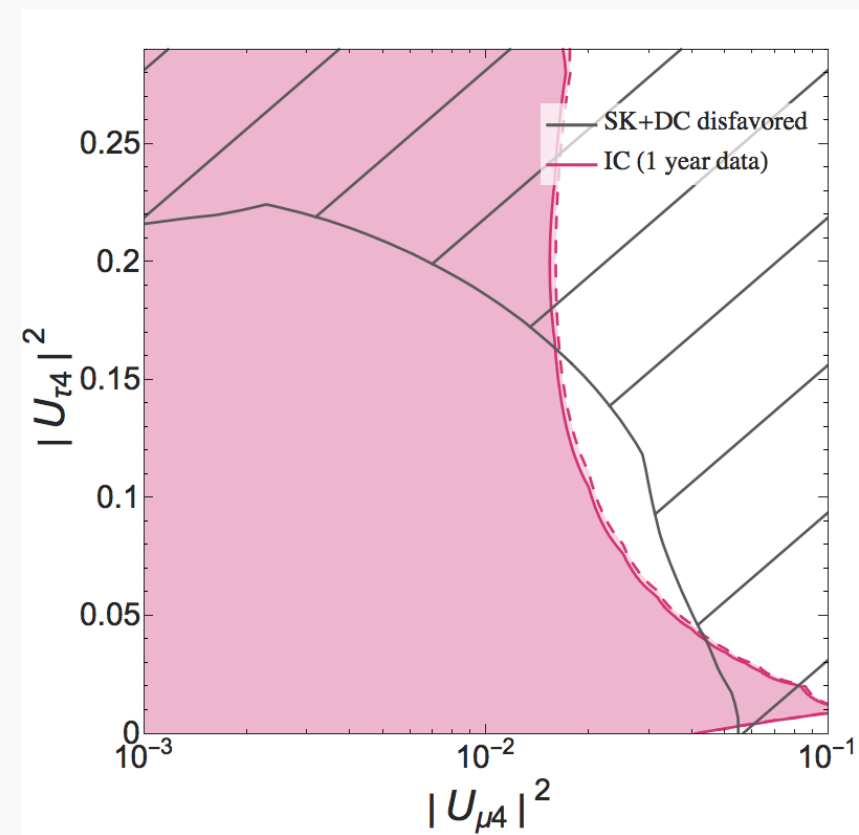
STERILE ν ABOVE 10 E ν AT ICECUBE

- Constraints obtained for the public 1 year-data

90%



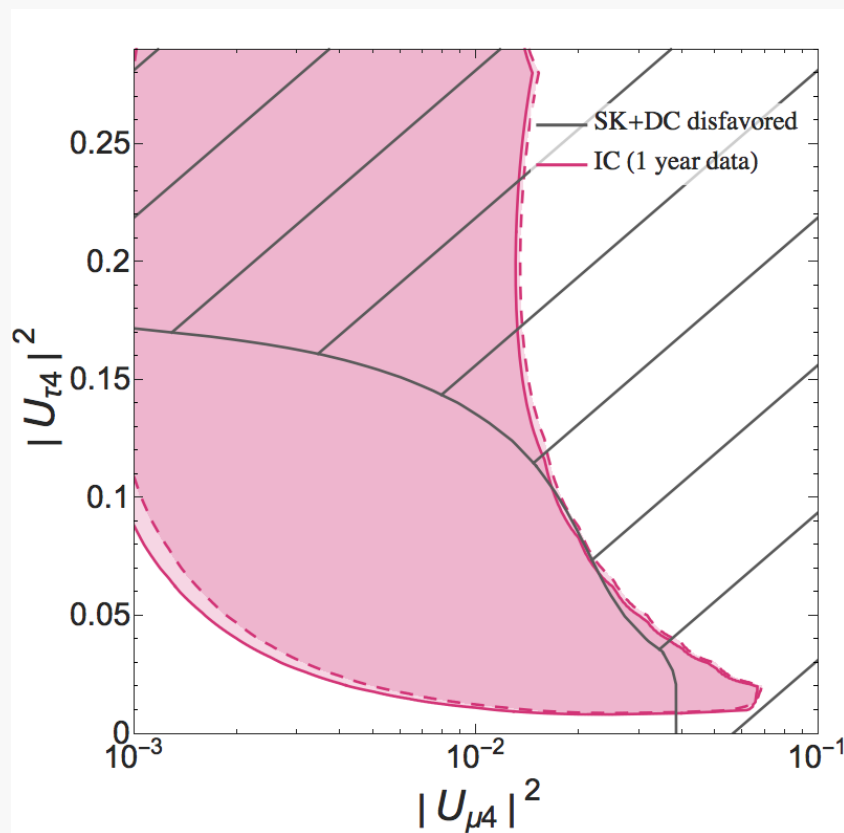
99%



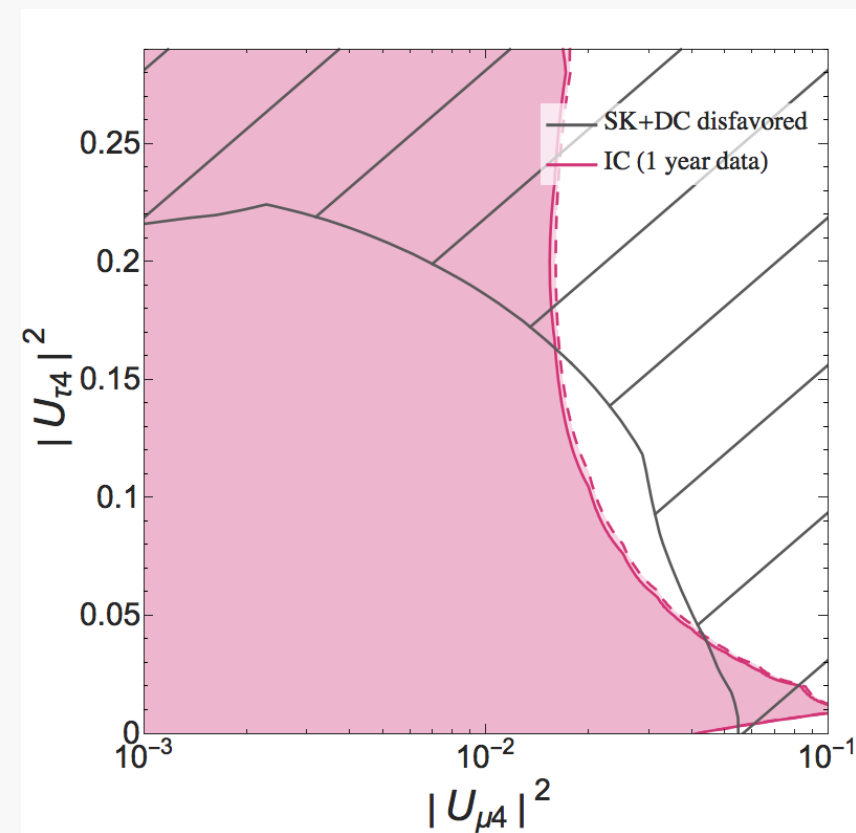
STERILE ν ABOVE 10 EeV AT ICECUBE

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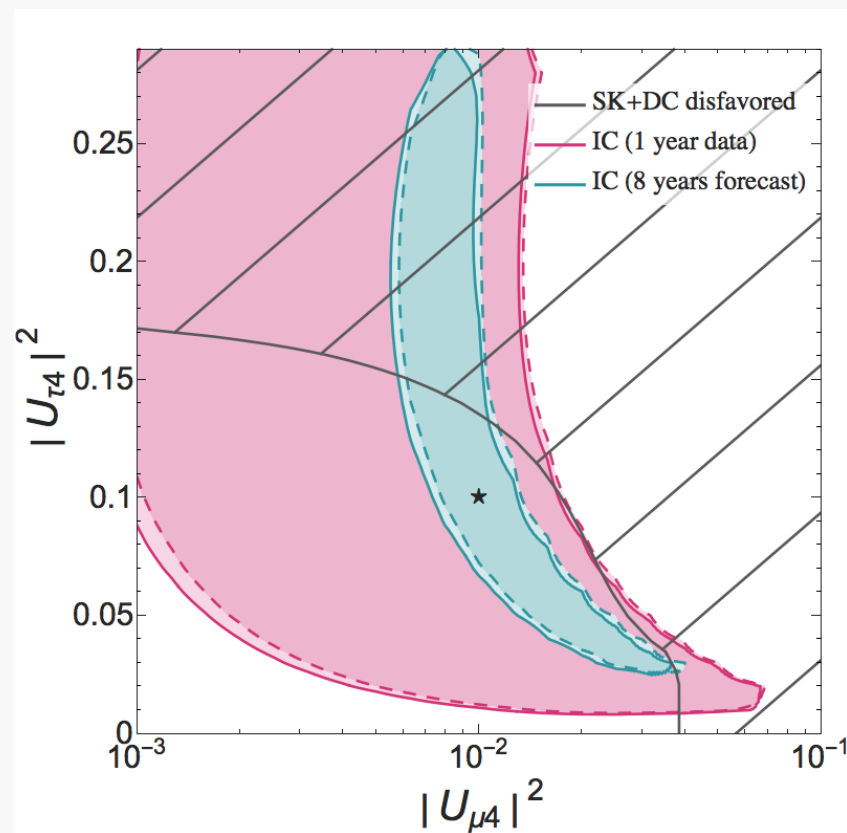
Mild preference (2.3σ 1 dof) for non-zero mixing

Between 0.75 and 3σ depending on the binning and flux adopted

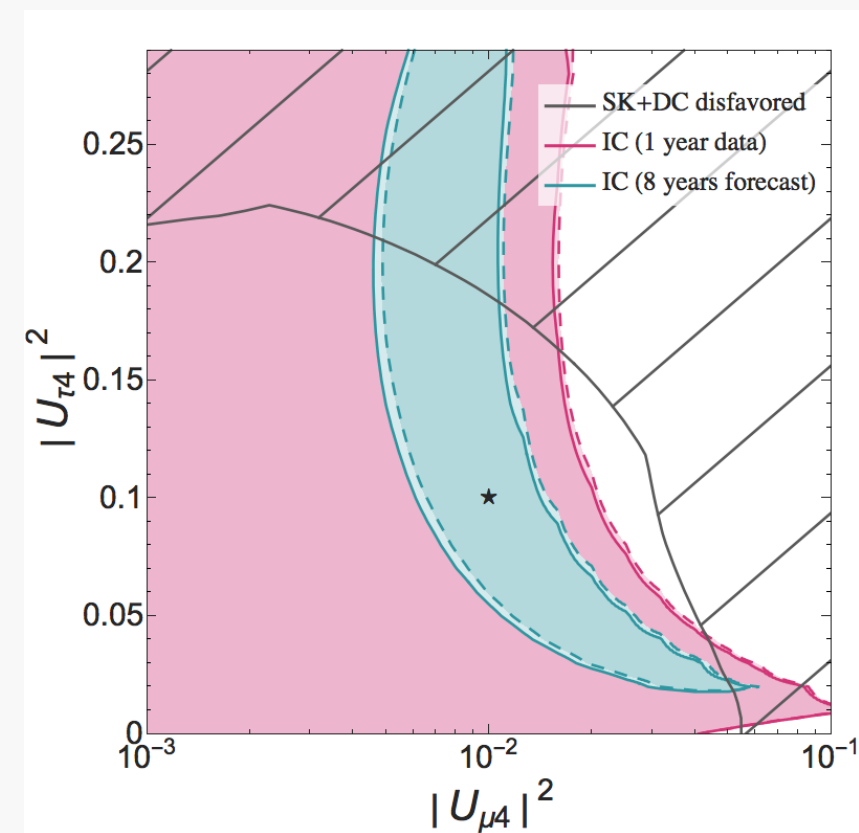
STERILE ν ABOVE 10 E ν AT ICECUBE

- Constraints obtained for the 8-years forecast

90%



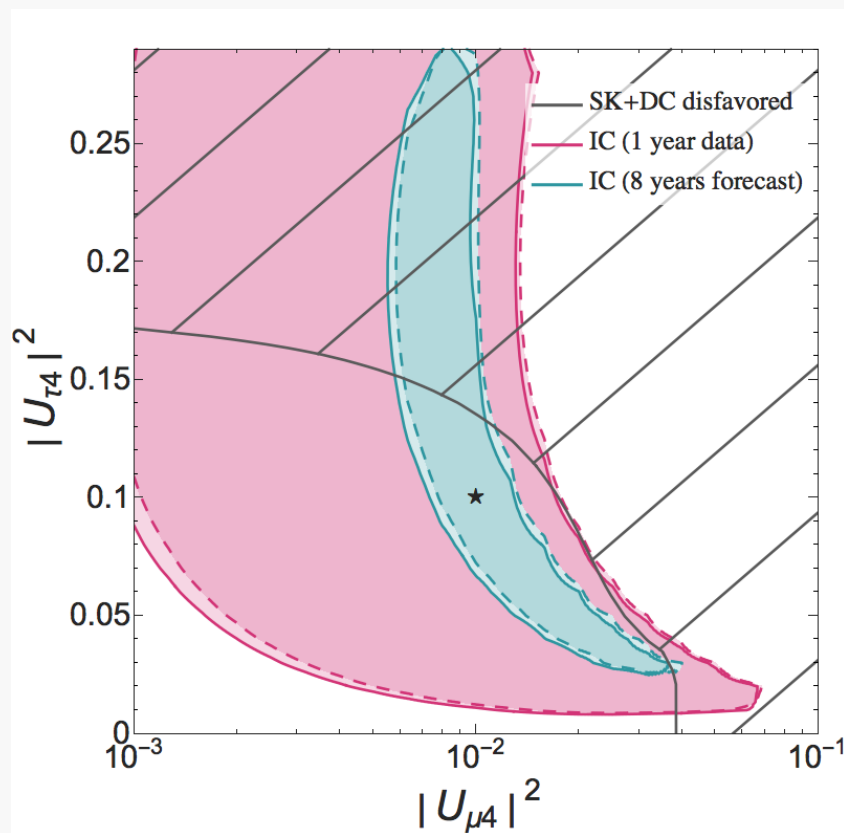
99%



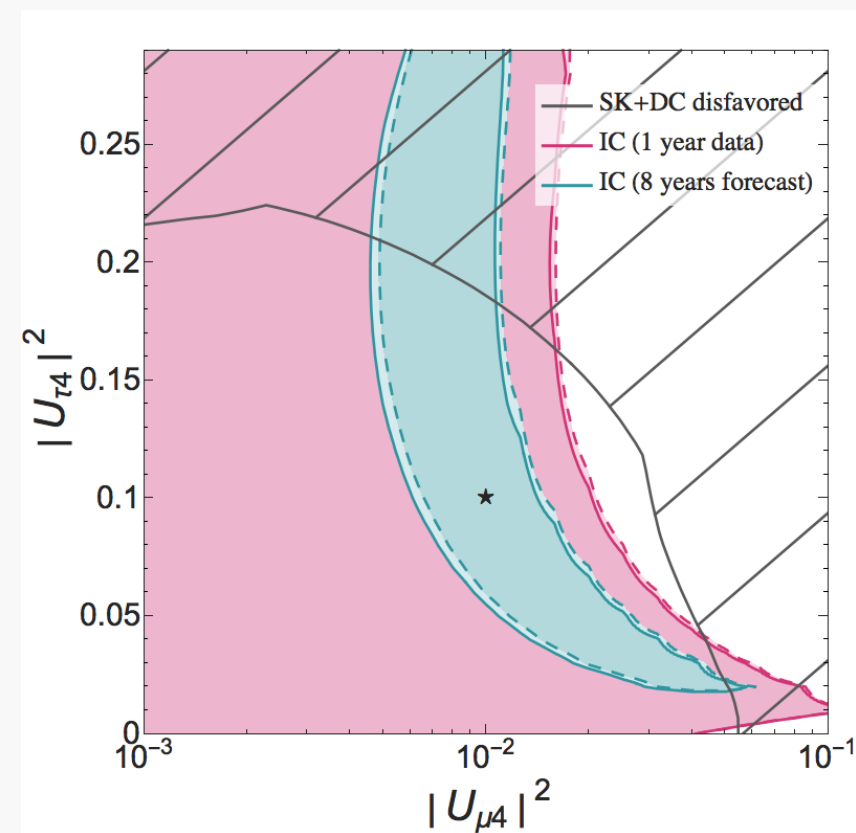
STERILE ν ABOVE 10 EeV AT ICECUBE

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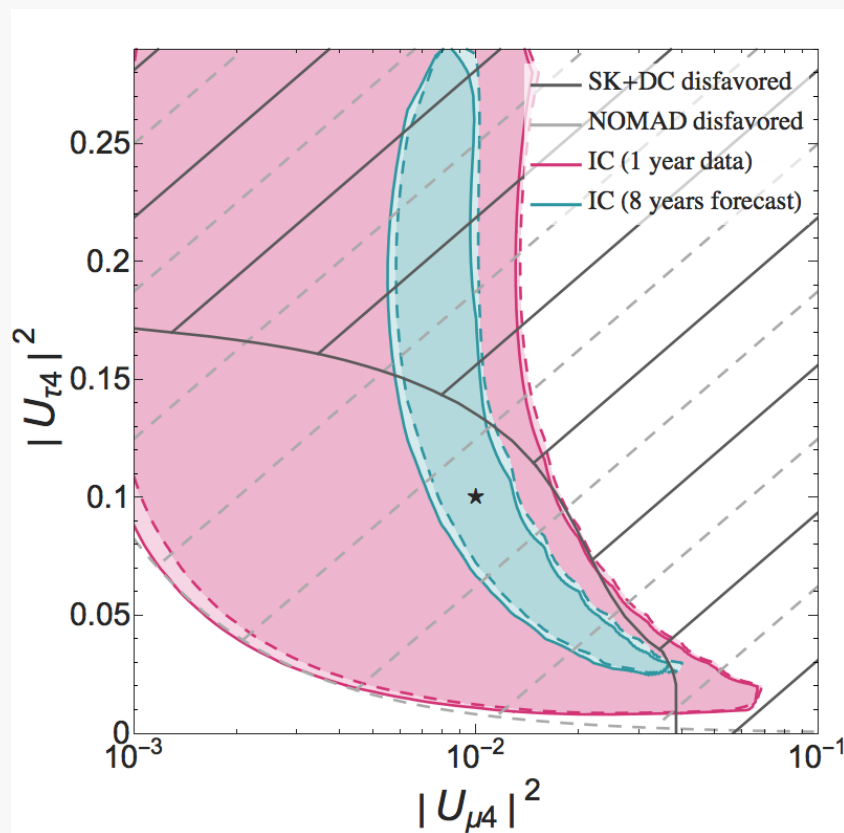


Overlap with sterile ν interpretation of upward shower observed by ANITA

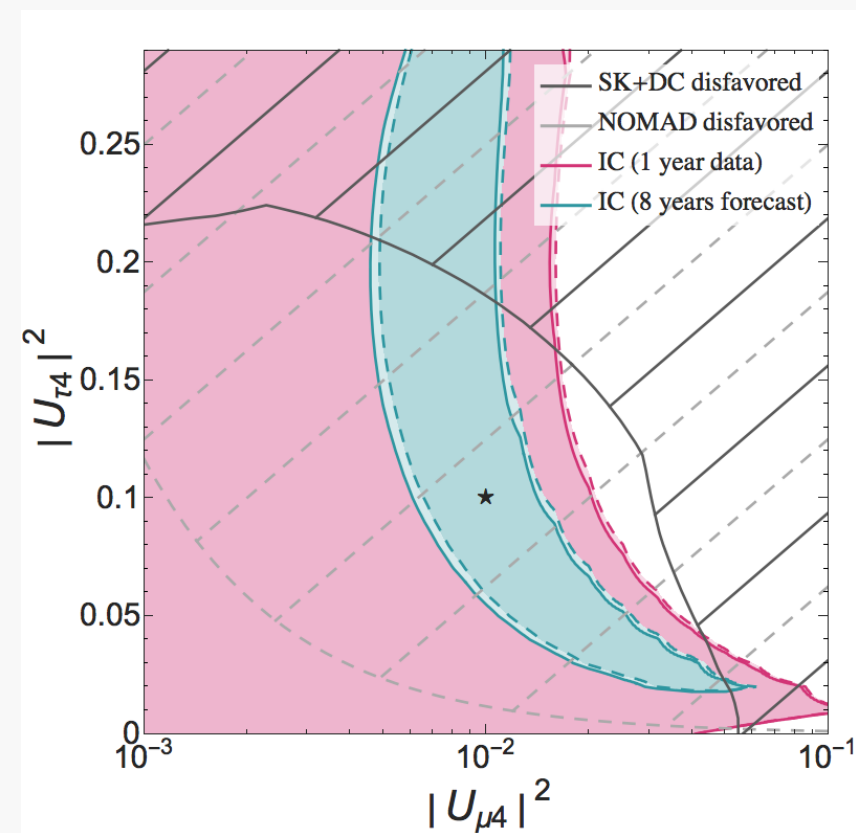
STERILE ν ABOVE 10 EeV AT ICECUBE

- Constraints obtained for the 8-years forecast

90%



99%



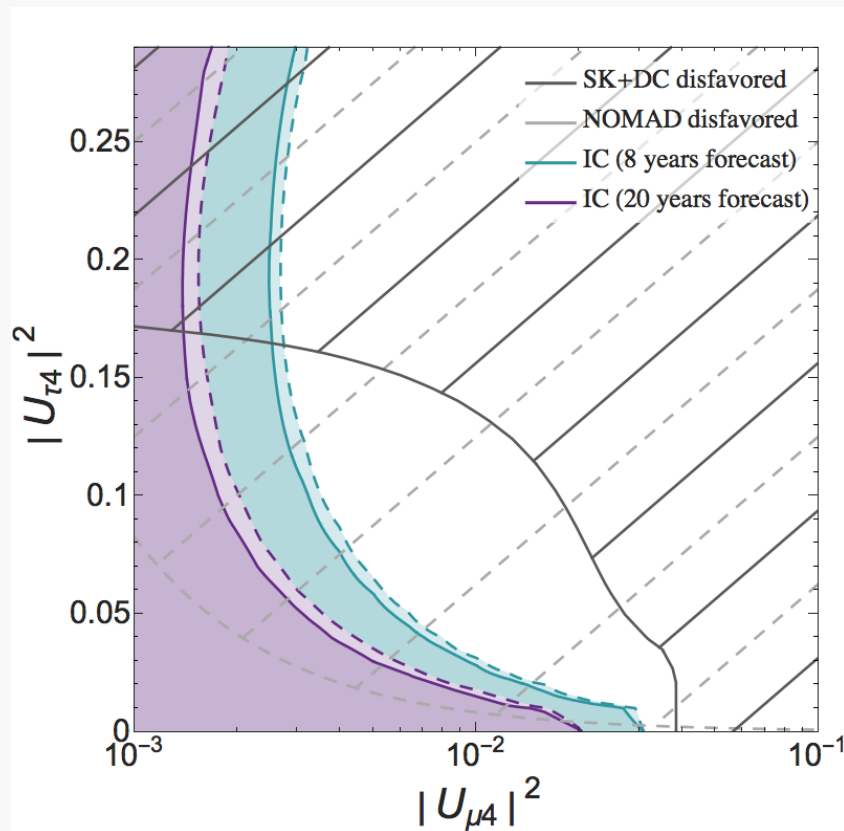
NOMAD explored $\nu_\mu \rightarrow \nu_\tau$ with negligible matter effects

$$P_{\mu\tau} \simeq 4|U_{\tau 4}|^2|U_{\mu 4}|^2 \sin^2 \left(\frac{\Delta m_{41}^2 L}{4E} \right) \Rightarrow |U_{\mu 4}|^2|U_{\tau 4}|^2 < 8.3 \cdot 10^{-5} \text{ (90\% CL)}$$

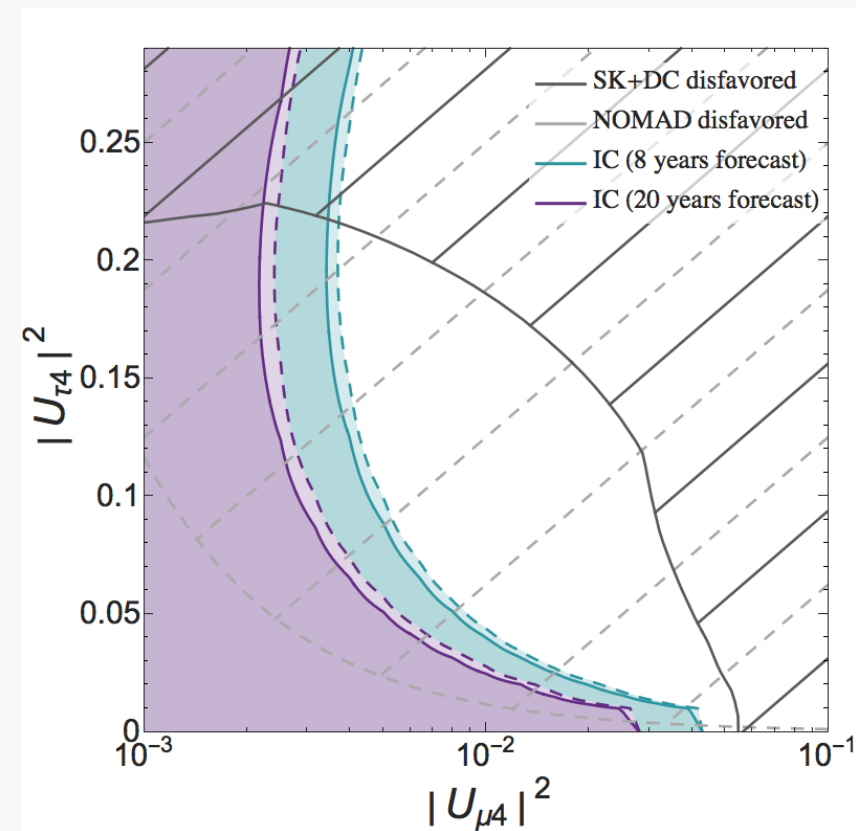
STERILE ν ABOVE 10 EeV AT ICECUBE

- Constraints obtained for 8-years and 20-years forecasts

90%



99%



SUMMARY

SUMMARY

Neutrino masses and mixings point to a New Physics scale where L is broken.

Non-Unitarity induced by heavy neutrinos and oscillations of light sterile neutrinos in the averaged out regime share the same phenomenology at leading order.

Non-Unitarity from heavy neutrinos beyond the reach of near-future neutrino oscillation experiments ($\theta \sim \mathcal{O}(10^{-2})$), contrary to previous claims in the literature.

Light sterile neutrino limit can be probed at present and near-future neutrino oscillation experiments ($\theta \sim \mathcal{O}(10^{-1})$).

Important to consider the role of the Near Detector.

SUMMARY

The capabilities of IceCube to search for sterile ν above 10 eV by analyzing its atmospheric ν sample has been studied.

The 1-year data shows a mild preference for non-zero mixing, between 0.75 and 3σ depending on the binning and flux adopted.

At 99% CL the obtained bounds improve over the SK and DC present constraints in some part of the parameter space.

The results overlap with the favored region for the sterile ν interpretation of the upward shower observed by ANITA.

The preferred mixings are in tension with NOMAD data, and non-standard matter interactions needed to reconcile results.

8 years of IceCube data would be sufficient to confirm or exclude the present preference.

THANKS

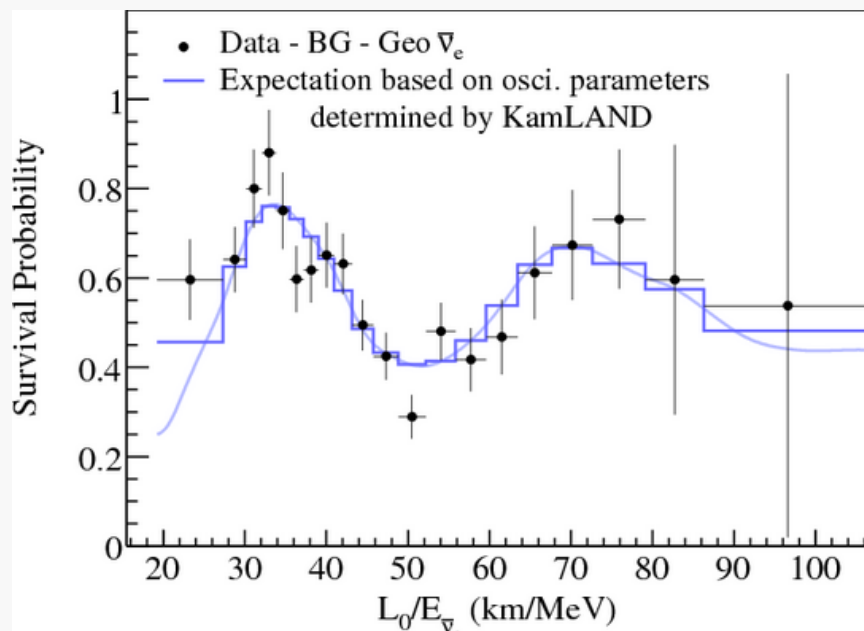
This project has received funding/support from the European Union's
Horizon 2020 research and innovation programme under the
Marie Skłodowska-Curie grant agreement No 674896.

BACK-UP

INTRODUCTION: SM OPEN PROBLEMS

- Dark Matter
- Matter-antimatter asymmetry (BAU)
- Neutrino masses

Experimental neutrino oscillation evidence

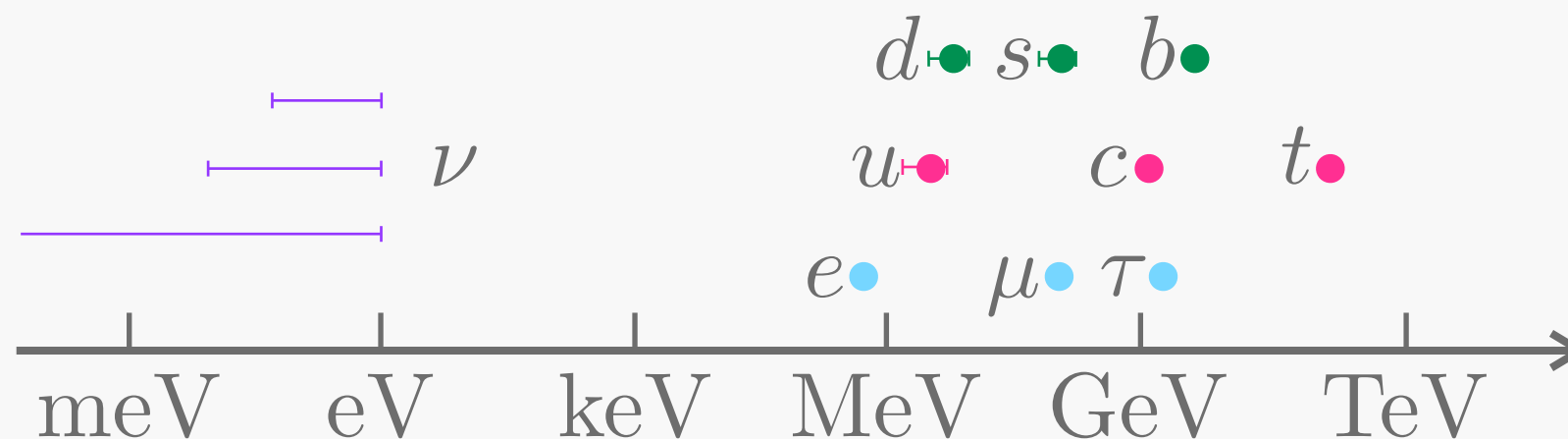


⇒ Neutrinos have masses

⇒ L_α violated

INTRODUCTION: SM OPEN PROBLEMS

- Dark Matter
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- Flavor Puzzle



No SM explanation for Yukawa [ordering](#).

INTRODUCTION: SM OPEN PROBLEMS

- Dark Matter
- Matter-antimatter asymmetry (BAU)
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- Flavor Puzzle

$$V_{\text{CKM}} = \begin{pmatrix} \text{large} & \text{medium} & \text{small} \\ \text{medium} & \text{large} & \text{small} \\ \text{small} & \text{small} & \text{large} \end{pmatrix} \begin{matrix} d & s & b \\ u \\ c \\ t \end{matrix}$$

$$U_{\text{PMNS}} = \begin{pmatrix} \text{large} & \text{medium} & \text{small} \\ \text{medium} & \text{large} & \text{medium} \\ \text{small} & \text{medium} & \text{large} \end{pmatrix} \begin{matrix} 1 & 2 & 3 \\ e \\ \mu \\ \tau \end{matrix}$$

Dissimilar pattern of quark and lepton mixings.

INTRODUCTION: LEPTONIC MIXING MATRIX

If neutrinos are massive, it will be a **misalignment** between physical (mass) and flavor eigenstates

$$\nu_{\alpha} = (U_{\text{PMNS}})_{\alpha i} \nu_i$$

INTRODUCTION: LEPTONIC MIXING MATRIX

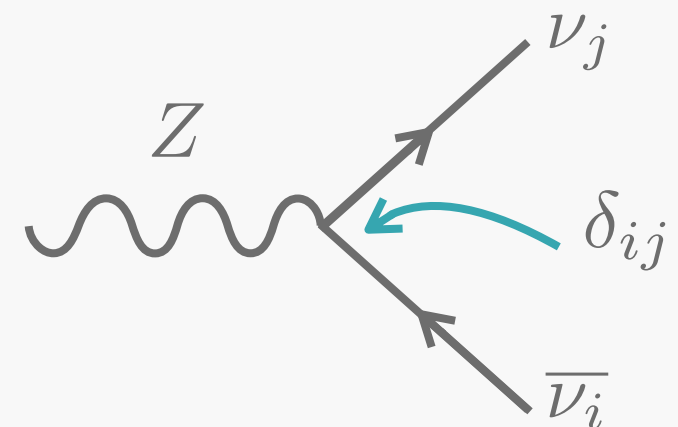
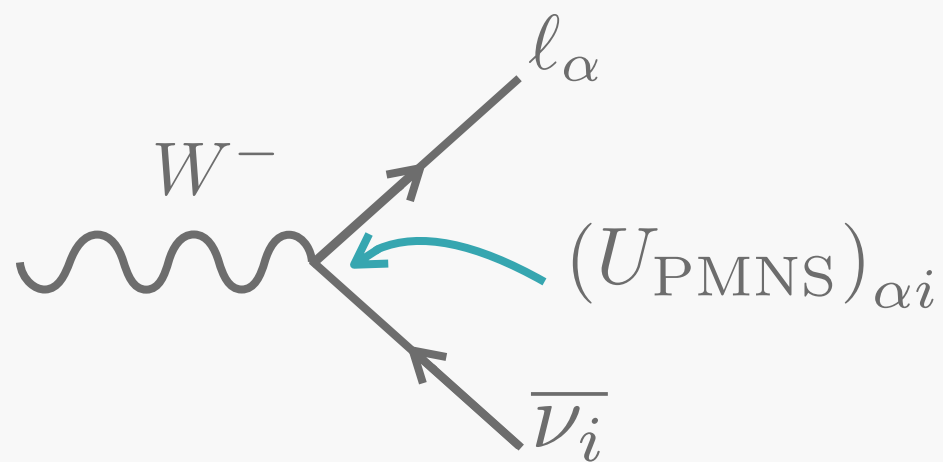
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Pontecorvo-Maki-Nakagawa-Sakata (PMNS) **mixing matrix**.

CC: $(U_{\text{PMNS}})_{\alpha i} \nu_i \bar{\ell}_\alpha W^-$

NC: $\delta_{ij} \nu_i \bar{\nu}_j Z$



STERILE ν ABOVE 10 E ν AT ICECUBE

- About the IceCube public data

1-year of high-energy through-going muons released by IceCube

- IceCube detector stage with 86 strings
- up-going track events (avoid background from cosmic μ)
- distances traveled $L \sim 10^4$ km

STERILE ν ABOVE 10 EeV AT IceCube

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The selected events have

- reconstructed energies between 400 GeV and 20 TeV
- reconstructed $\cos \theta_z$ between -1 and 0.2

