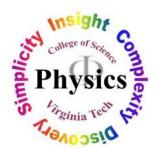
Epidemic spreading on preferred degree adaptive networks

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NSF-DMR Materials Theory

Motivation

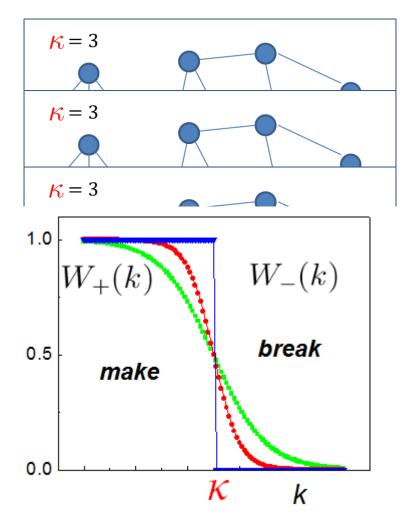
- Most epidemic models are based on regular lattices, *Erdös-Renyi or scale free networks*, with active nodes and static links.
 - > Active nodes: Links influence the nodes (epidemics, opinions, Ising model)
 - Active links: network topology changes
- Preferred degree networks: Nodes (individuals) have a preferred number of links (social connection). Make more realistic networks.
- Static epidemic model: active nodes, static links
- Adaptive model: active nodes and active links.
 - ➢ Feedback between Dynamics on the network and Dynamics of the network.
- Two community Coupled networks: Epidemic propagation from one community to other.



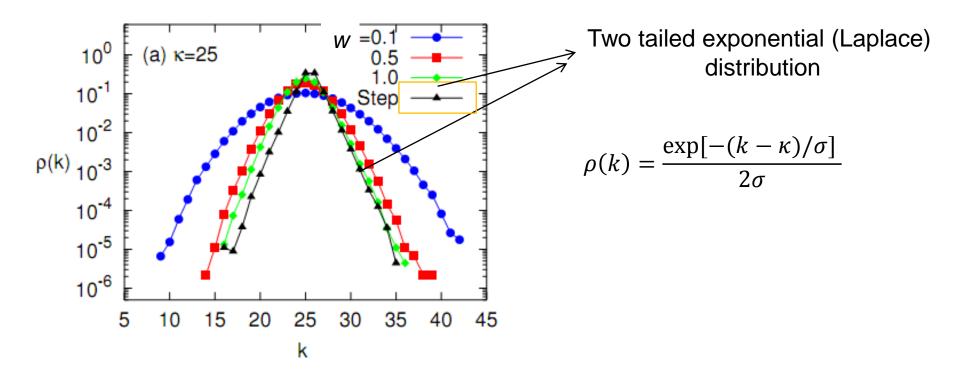
Preferred degree networks

- Nodes have preferred degree κ (Initially homogeneous).
- Select a random node *j* with degree k_j
 - > Make a link: $W_+(k_j)$
 - > Break a link : $W_-(k_j)$ $W_-(k_j) = 1 - W_+(k_j)$

•
$$W_+(k_j) = \frac{1}{1 + \exp(\frac{k-\kappa}{w})}$$



Degree distribution



All have same preferred degree κ

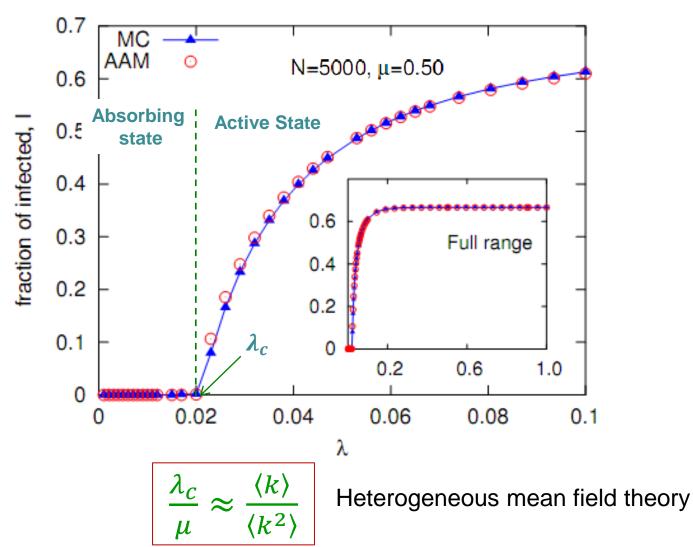
SIS disease dynamics

- Individuals are either Susceptible (S) or Infected (I)
- Susceptible meets an Infected and gets infected with rate λ $S + I \xrightarrow{\lambda} I + I$
- All infected reco
 S
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- Neglect all spatial structure.



SIS dynamics on static preferred degree network

Stationary Infection : $I(t \rightarrow \infty; \lambda)$





Adaptive behavior

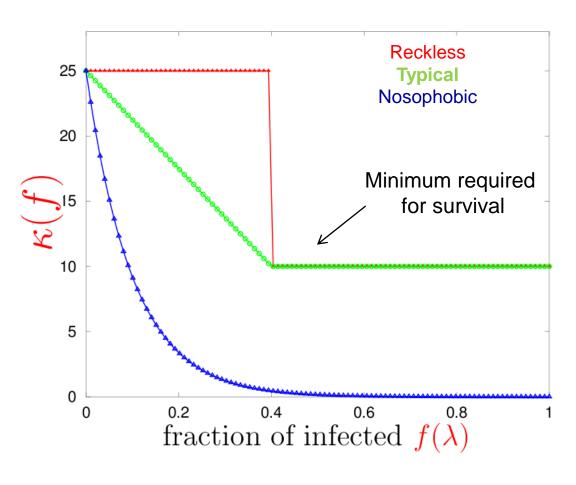
- People exhibit 'social distancing' when there is a raging epidemic.
- Modifies the model parameters: Social distancing causes infection probability to decrease (λ ↓)
- Modifies the contact structure (Network).
 Adaptive preferred degree κ(f)
- Our model: κ depends on global information directly linked to disease prevalence. (Flu, SARS etc).



Adaptive preferred degree $\kappa(f)$

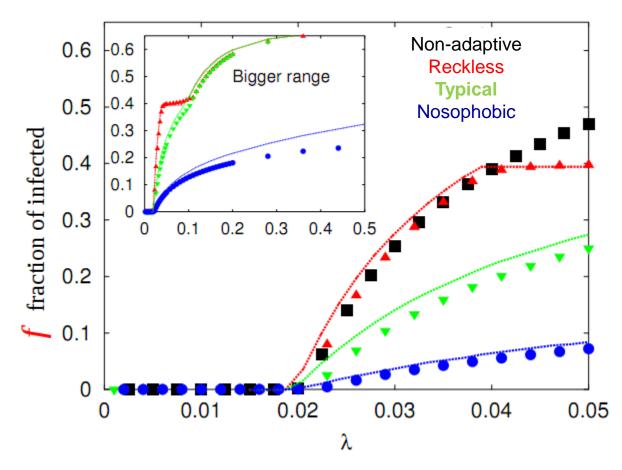
 $\kappa(f)$: Preferred degree of people depends on the state of the epidemic f(t) (fraction of infected at time t).

- RecklessTypical
 - Nosophobic (highly scared)





Infection phase diagram : Adaptive SIS



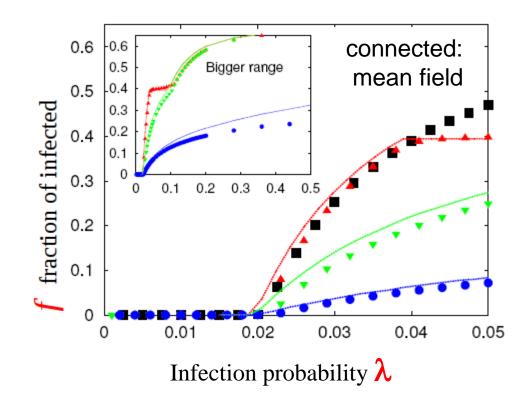
Adaptive SIS model with varying preferred degree **doesn't change the** epidemic threshold, but changes the level of infection in the active state.

Mean field analysis

- $\kappa(I) = \kappa_m f(I)$
- Mean field equation

 $\frac{dI}{dt} = -\mu I + \lambda_{eff}(I)S$

- $\lambda_{eff}(I) = 1 (1 \lambda)^{I\kappa(I)}$ Assumption: fraction of infected is same around every node.
- Steady state solution $\frac{dI}{dt} = 0$





Mean field predictions closely match simulations

Heterogeneous preferred degree

 Two community network (extroverts and introverts) different preferred degree and coupling

Simplest network with heterogeneous preference

- Questions:
 - > How does disease spread across different communities?
 - > Are extroverts more prone to contagious diseases?
 - How does disease depend on the interaction/coupling between the communities?

Two community network

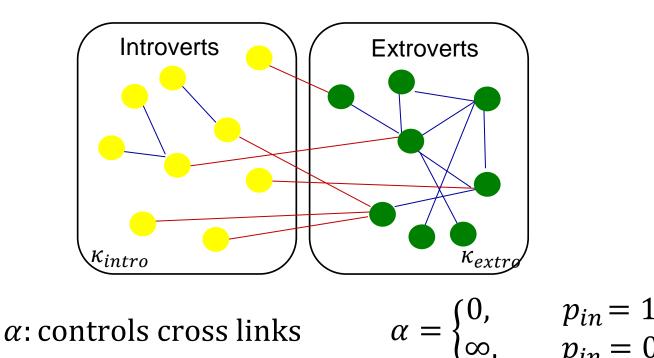
Decision to make *internal* (within) or *external* (across) link

$$p_{in} = \frac{k_{ex}}{k_{ex} + \alpha k_{in}}$$

$$p_{ex} = 1 - p_{in}$$

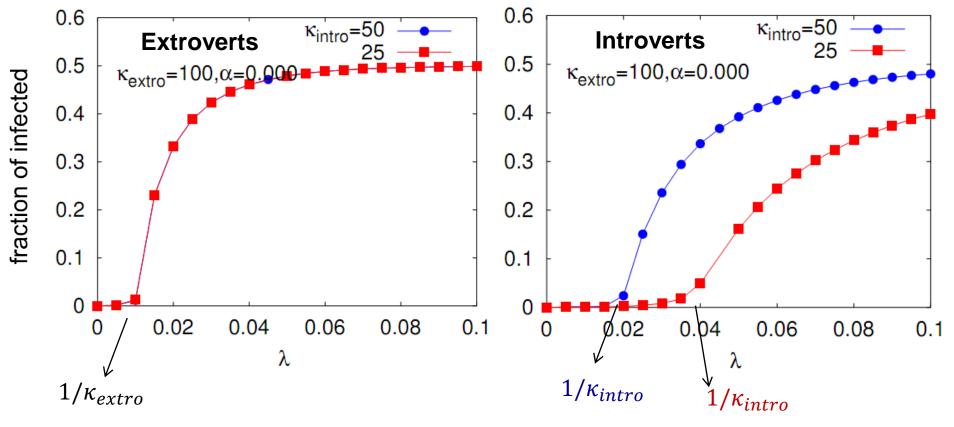
 k_{ex} external (cross) degree





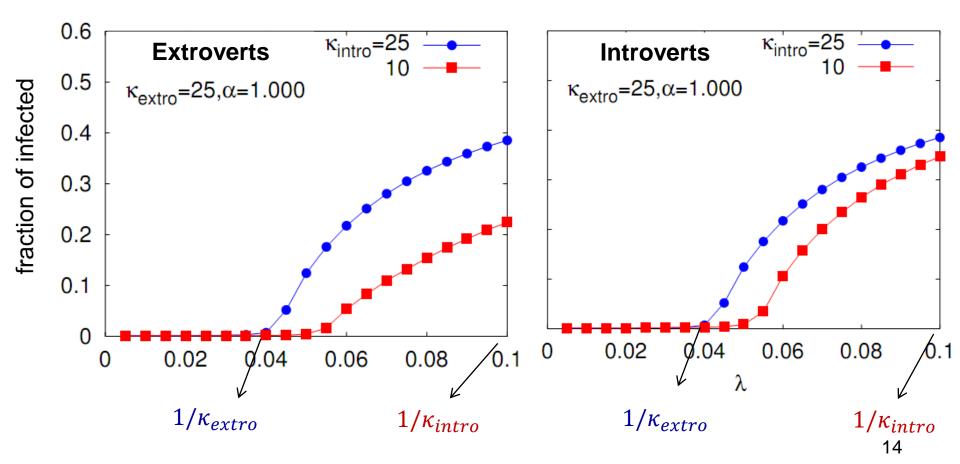
Results- uncoupled communities

 $\alpha = 0$ two transition points



Coupled communities

 $\alpha \neq 0$ transition point governed by **extroverts** and is not sharp



Summary

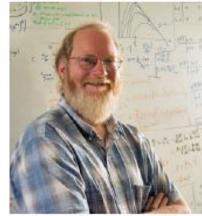
Behavior SIS model with active nodes and active links.
 Feedback between dynamics on the network and dynamics of the network.

- Adaptive SIS model with varying preferred degree doesn't change the epidemic threshold, but changes the level of infection in the active state.
- Generalizations to more realistic problems:
 - Population with different preferred degrees:
 - Epidemic on a realistic model network with different degree distribution
 - Population with mixed behavior:

 $N = N_{reckless} + N_{typical} + N_{nosophobic}$

Collaborators







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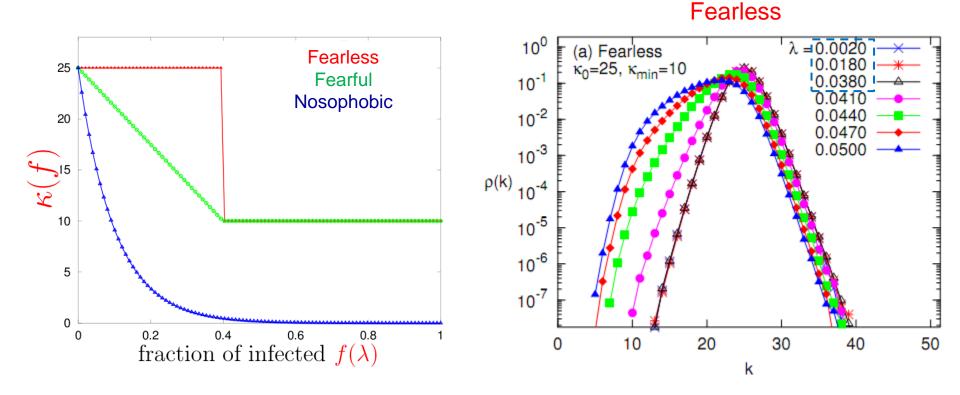


Preferred degree networks

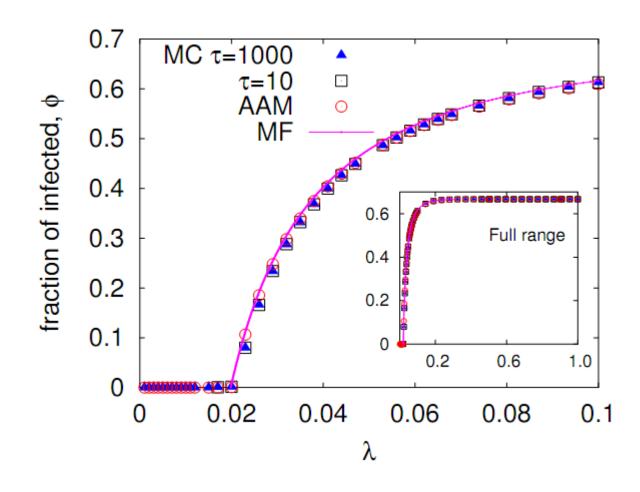
- Make new friends, break old ties (establish/cut contacts) according to some *preference*
- Preferences can be dynamic.
- Preference can vary from person to person



Effect on Network



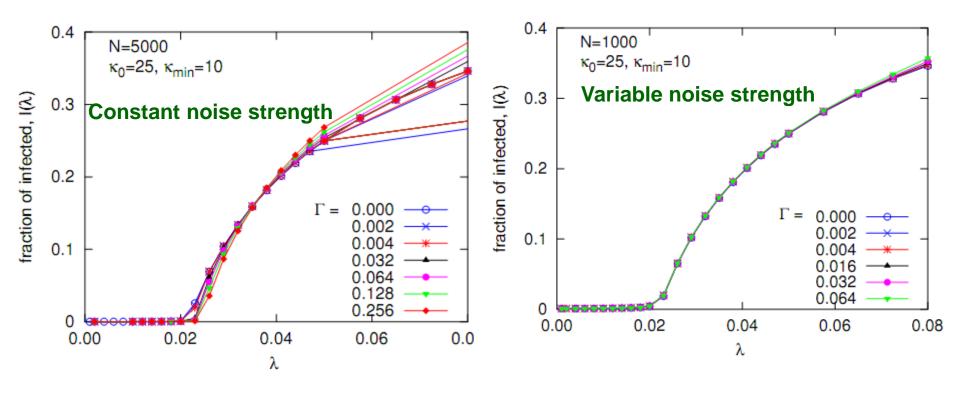
Degree distribution peak centers at $\kappa(f)$, corresponding to fraction of infected $f(\lambda)$.



SIS phase diagram near transition point, comparison with mean field theories.

Noisy perception

$$I_{perc}(t) = I(t) + \eta(t)$$



$$\langle \eta(t)\eta(t')\rangle = \Gamma\delta(t-t')$$

 $\langle \eta(t)\eta(t')\rangle = \Gamma I(t)\delta(t-t')$

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