

Helicity Correlated Beam Systematics in the Q_{weak} Experiment

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Q_{weak} will make a 4% measurement of Q_w^p using parity violating electron scattering (PVES) which arises from the interference between the electromagnetic(γ) and neutral weak currents(Z^0):

$$A_{\gamma Z^0} = \frac{1}{P_L} \frac{\sigma_+ - \sigma_-}{\sigma_+ + \sigma_-} \simeq -300\text{ppb}$$

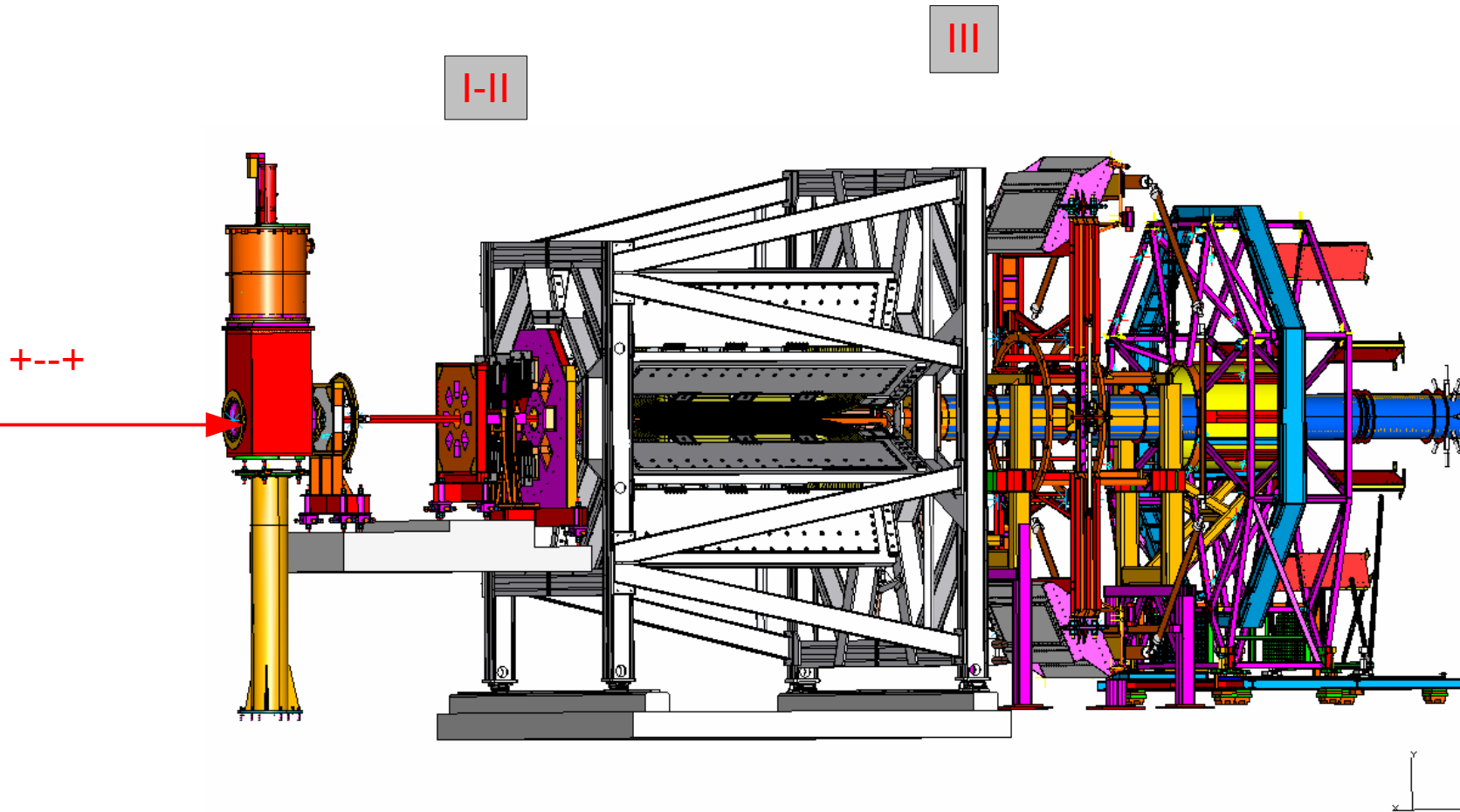
The Weak Charge of the Proton (Q_w^p) is heavily suppressed in the Standard Model (SM). Due to a near cancellation we are uniquely sensitive to $\text{Sin}^2\theta_w$:

$$Q_w^p = 1 - 4\text{Sin}^2\theta_w \approx -0.048$$

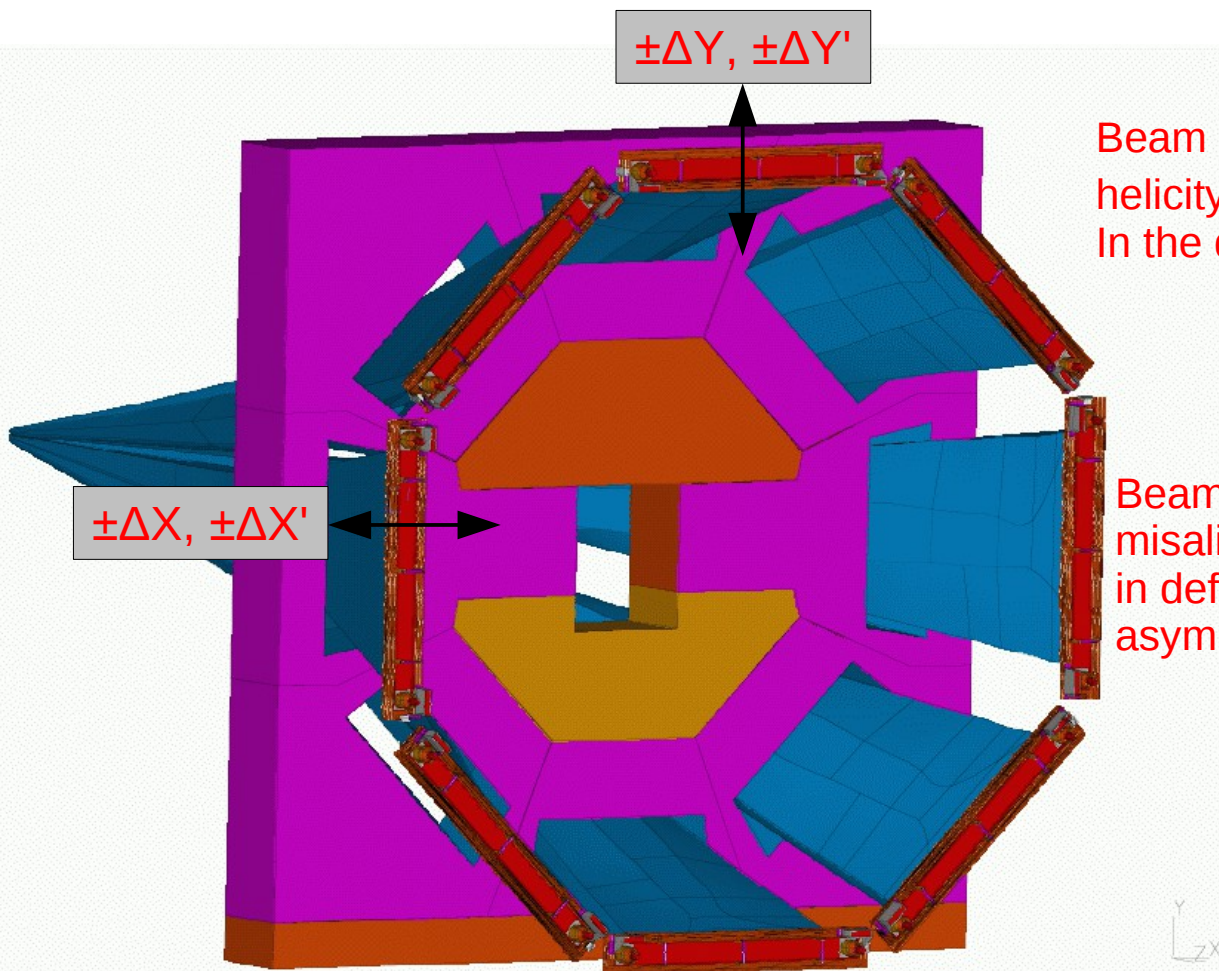
In the limit of low momentum transfer and small forward angle scattering, leading order term contains Q_w^p . The next highest order term contains the hadronic structure and is constrained by current world data.

$$A_{\gamma Z} \xrightarrow[\theta \rightarrow 0]{Q^2 \rightarrow 0} \frac{-G_F}{4\pi\alpha\sqrt{2}} [Q^2 Q_w^p + \underbrace{Q^4 B(Q^2)}]$$

Systematic error ~2%



- Forward scattering , 85% polarized electrons at $Q^2 \sim 0.03 \text{ GeV}^2$ and $I = 185 \text{ uA}$ from LH_2 target.
- Toroidal spectrometer provides momentum selection of elastically scattered electrons.
- Symmetric array of 8 Cerenkov detectors(800 MHz/bar).



Beam property changes by $\pm\Delta x_i$ during helicity flip can generate false asymmetries in the detector array.

Beam parameters such as: beam centroid, misalignments of detector array, and asymmetries in defining collimators can amplify false asymmetries.

The symmetry of the main detector array should help to suppress position and angle changes, however helicity correlated changes in the energy do not see a cancellation.

Q_{weak} would like to measure the sensitivities to these beam parameters in order to correct for false asymmetries.

<i>Uncertainty</i>	$\Delta A_{pv} / A_{pv}$	$\Delta Q_w / Q_w$
<i>Statistical:</i>	2.1 %	3.2%
<i>Systematic:</i>		
<i>Hadronic Structure</i>	-----	1.5%
<i>Beam Polarimetry</i>	1.0%	1.5%
<i>Absolute Q² Determination</i>	0.5%	1.0%
<i>Backgrounds</i>	0.5%	0.7%
<i>Helicity Correlated</i>		
<i>Beam Properties</i>	0.5% ± 1 ppb!	0.7%
<i>Total:</i>	2.5%	4.1%

Our goal is to keep total corrections at run's end to less than 10 ppb (assuming a 10% measurement).

$$\Delta A_{position} = \frac{\partial A}{\partial X_{position}} \Delta X_{position} \sim 100 \text{ ppm/mm} * 1 \text{ nm} = 0.1 \text{ ppb}$$

$$\Delta A_{Energy} = \frac{\partial A}{\partial E} \Delta E \sim 3 \text{ ppm/ppm} * \Delta E$$

Error this small → not a problem

ΔE should be no larger than 3.3 ppb

So how do we measure helicity correlated beam systematics?

Extraction from Natural Beam Motion: Covariance Analysis
– Jim Birchall(U. Manitoba) and Jan Balewski(MIT)

Detector response to natural beam motion is measured. Using a covariance analysis, orthogonalized sensitivities are determined and corrected using linear regression.

Driven Beam Modulation System – Qweak Beam Modulation Group

Using kicker coils the beam is modulated in position/angle. Measuring the detector response during modulation we are able to calculate the detector sensitivities. False asymmetries can then be corrected through linear regression.

Consider a first order model for the false asymmetry ϵ in the main detector:

$$\epsilon = a\delta x + b\delta x' + c\delta y + d\delta y' + e\delta E$$

One can calculate by multiplying through and taking the average:

$$\overline{\epsilon \delta x} = a\overline{\delta x^2} + b\overline{\delta x' \delta x} + c\overline{\delta y \delta x} + d\overline{\delta y' \delta x} + e\overline{\delta E \delta x}$$

$$\overline{\epsilon \delta x} = a\overline{\delta x \delta x} + b\overline{\delta x' \delta x} + c\overline{\delta y \delta x} + d\overline{\delta y' \delta x} + e\overline{\delta E \delta x}$$

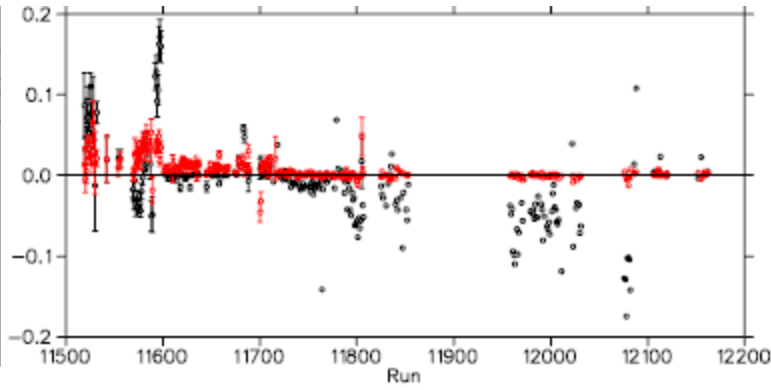
Taking the difference:

$$\begin{aligned} \text{cov}(\epsilon, \delta x) &= a \text{var}(\delta x) + b \text{cov}(\delta x', \delta x) + c \text{cov}(\delta y, \delta x) \\ &\quad + d \text{cov}(\delta y', \delta x) + e \text{cov}(\delta E, \delta x) \end{aligned}$$

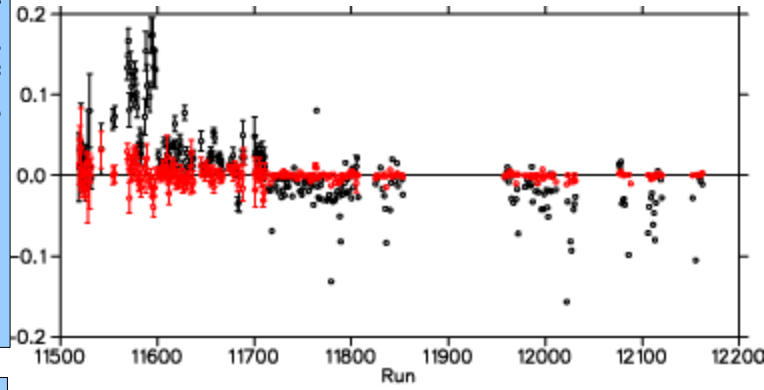
Doing the above for each variable, δx , $\delta x'$, δy , $\delta y'$, δE we can generate a set of five linear equations that can be solved in the usual way for sensitivities a , b , ...ect.

Natural Beam Motion Results

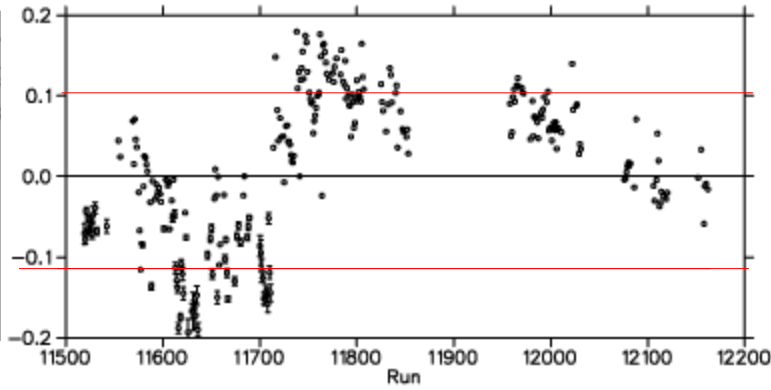
Correction x, y (ppm)



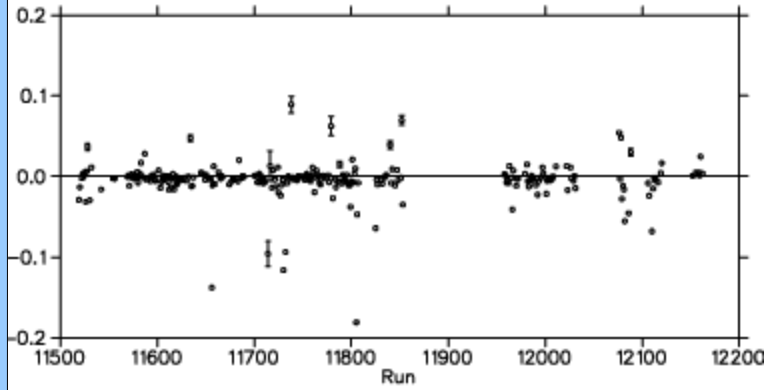
Correction x', y' (ppm)



Correction E (ppm)

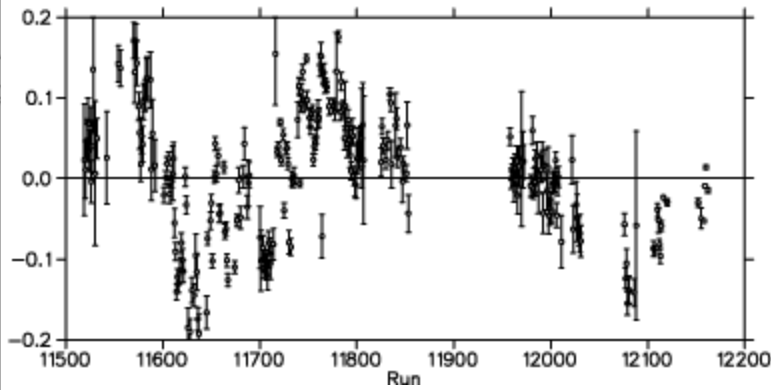


Correction for charge (ppm)



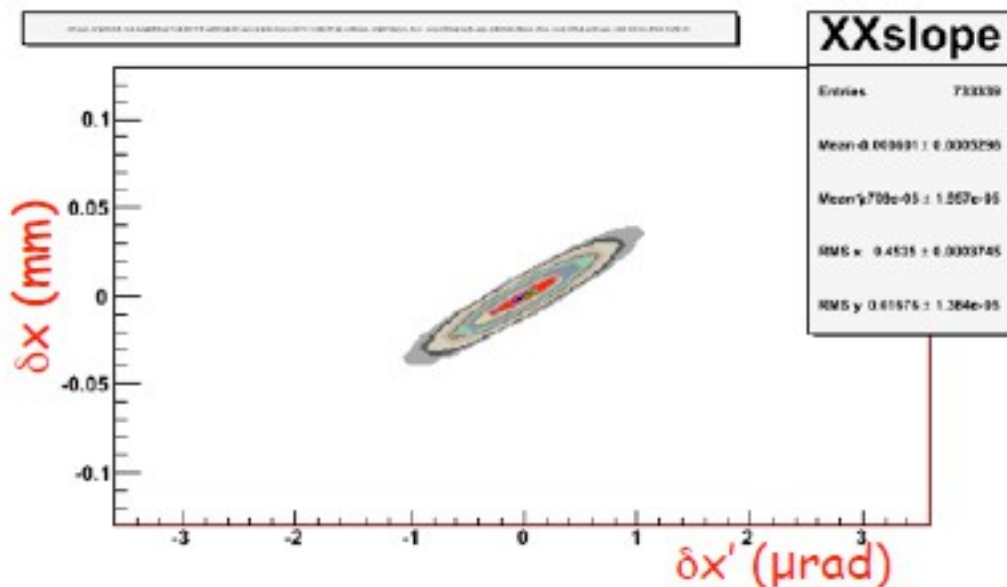
Red Y
Black X

Total Correction x, y (ppm)



Sum of corrections dominated by Energy correction,
 $\pm \frac{1}{2}$ our physics asymmetry!

Energy very important.



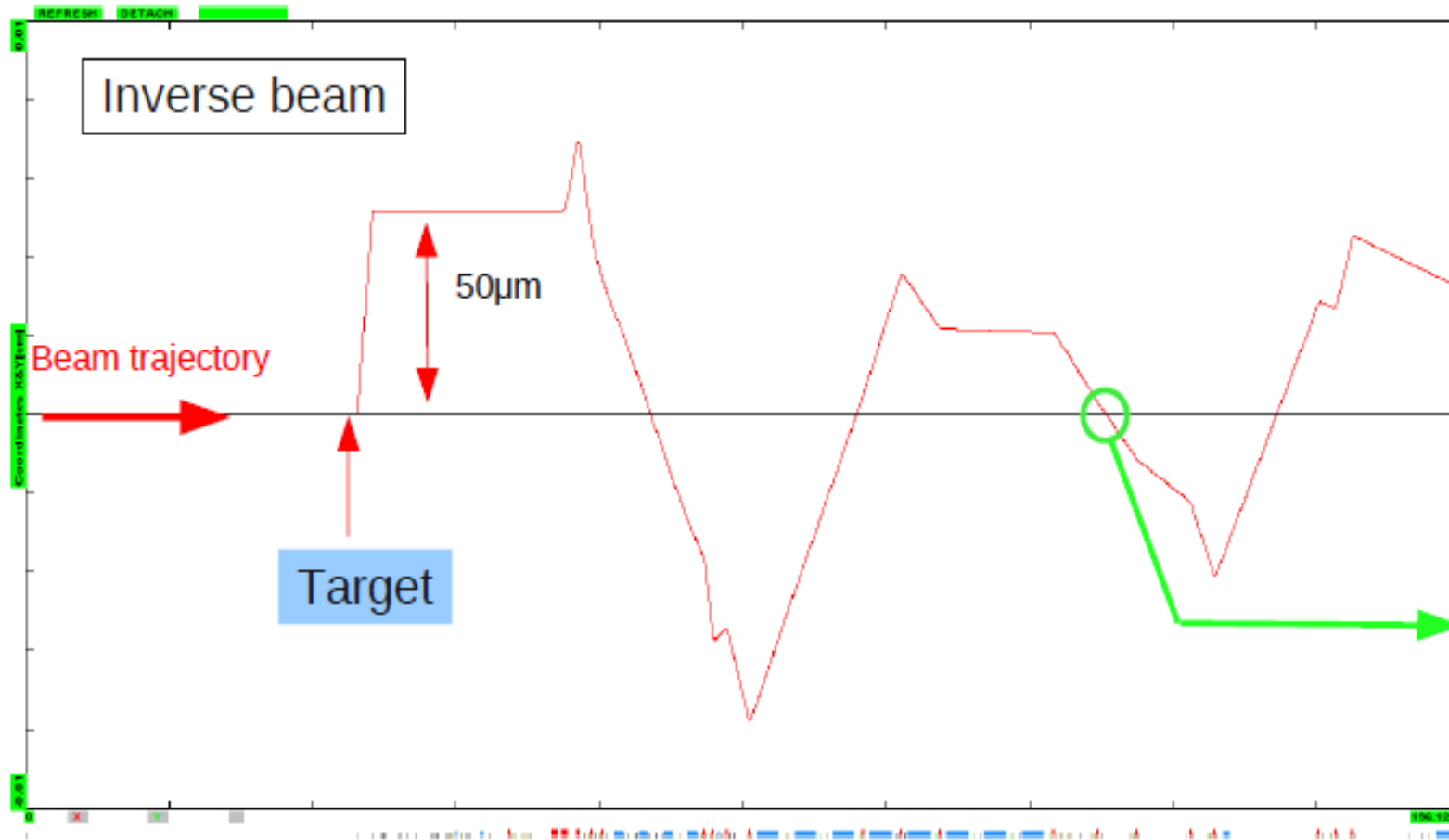
Natural beam motion highly correlated – hard to decouple.

Correlation of $\delta x, \delta x'$ was found to be very high.

Correlation coefficient $\sim 0.999!$

Because the natural jitter of the beam is so small it takes a long time to get a precise measurement of the sensitivity slopes.

- The beam modulation system used pairs of coils positioned along the beamline to “kick” the electron beam onto a trajectory resulting in a “pure” X, X', Y, Y' offset at the target.
- An SRF cavity is used to modulate the beam energy.
- Has the advantage of producing a more linearly independent set of slopes.



Time reversal invariance of the electromagnetic interaction → upstream rays tell us how to perturb downstream for proper modulation

Crossing point which We will use to kick the beam onto the desired trajectory.

Using a ray tracing program (OPTIM), we can determine the trajectory of the beam by sending rays upstream from the target. By kicking the beam on to the “magic orbit” we can produce desired position/angle on the target.

$$\Delta A = \sum_{i=1..5} \frac{1}{\bar{Y}} \frac{\partial Y}{\partial x_i} \Delta x_i + \frac{\partial A_{md}}{\partial A_q} \Delta A_q$$

The goal is to determine the normalized detector sensitivities, which are not directly measurable. However using the relation:

$$\frac{\partial Y}{\partial C_j} = \sum_i \frac{\partial Y}{\partial M_i} \frac{\partial M_i}{\partial C_j}$$

M ≡ Monitor {targetX, targetY, Energy, targetXSlope, targetYSlope
C ≡ Coil {Parameterization of ramp function, ie. Phase of modulation}
Y ≡ Main Detector Yield.

$$\frac{\partial Y}{\partial M_i} = \frac{\partial Y}{\partial C_j} \left(\frac{\partial M_i}{\partial C_j} \right)^{-1}$$

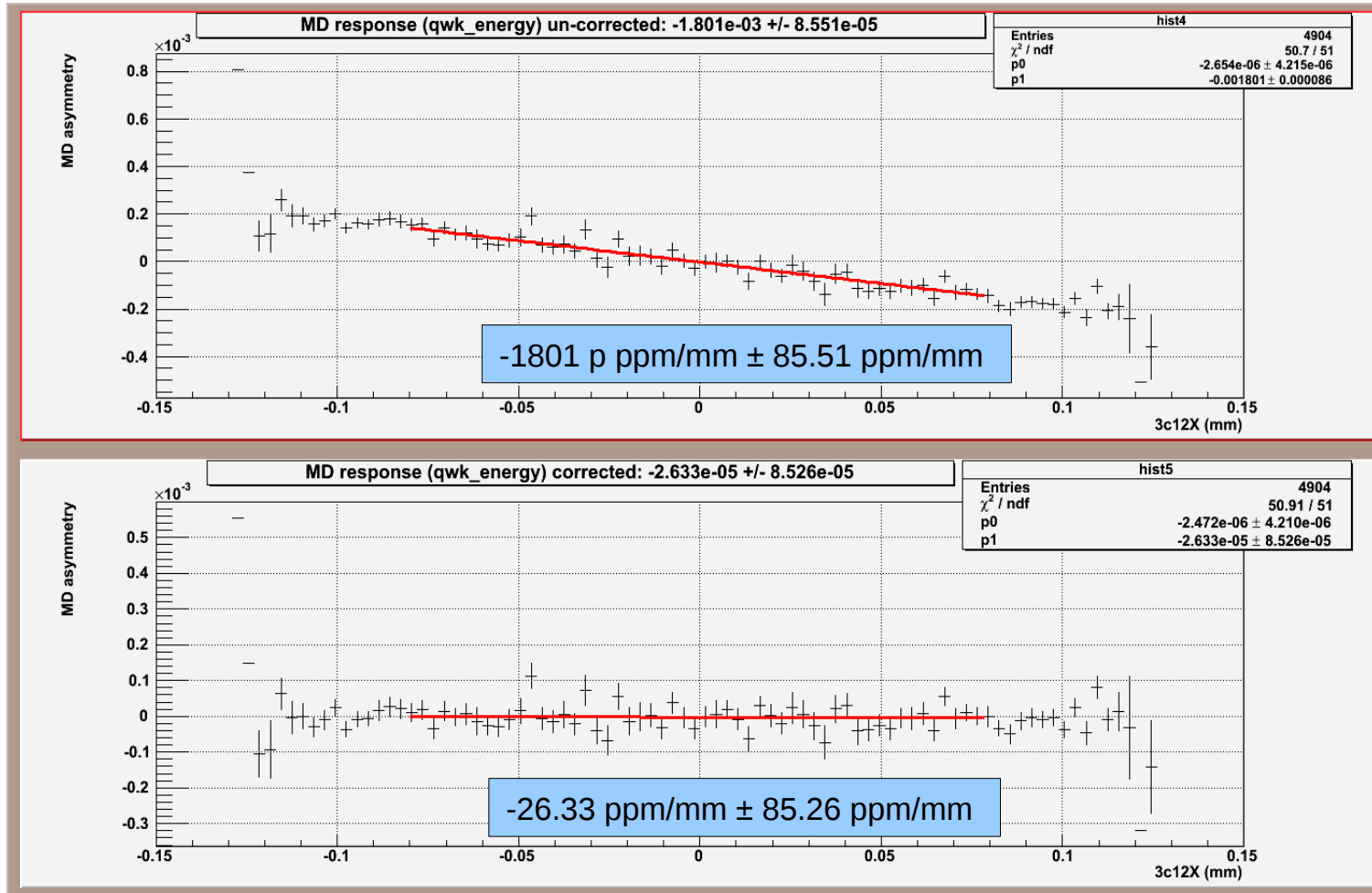
Matrix inversion gives us detector sensitivities in the target basis + 3C12X. Slopes in terms of Monitor and Coil are calculated algebraically using a simple fit to a regression line:

$$Y = \hat{\beta}_j C_j$$

$$M_i = \hat{\beta}_k C_k$$

$$\hat{\beta} = \frac{\sum_i (x_i - \bar{x})(y_i - \bar{y})}{\sum_i (x_i - \bar{x})^2} = \frac{\text{Cov}[x, y]}{\text{Var}[x]}$$

As a first check we see if we can zero out the modulated data.



Extracted sensitivities completely zero out energy dependence detector asymmetry.

Monitor	Unregressed	Regressed	Regressed + ΔA_q	
Target X	483.9 ± 46.42	-112.4 ± 46.36	176.3 ± 46.28	$20\sigma \rightarrow 2\sigma \rightarrow 3\sigma$
Target Y	847.7 ± 62.81	-223.5 ± 62.73	-53.71 ± 62.62	$13\sigma \rightarrow 3.5\sigma \rightarrow 0.8\sigma$
3C12X	-1400 ± 40.18	-454.2 ± 40.20	-14.69 ± 40.14	$35\sigma \rightarrow 11\sigma \rightarrow 0.4\sigma$
Target X'	12.70 ± 1.26	-8.34 ± 1.26	-0.60 ± 1.26	$10\sigma \rightarrow 7\sigma \rightarrow 0.5\sigma$
Target Y'	25.85 ± 1.99	-17.44 ± 1.99	-10.51 ± 1.99	$13\sigma \rightarrow 9\sigma \rightarrow 5\sigma$

Beam Modulation corrections greatly reduce slopes in first pass but still leave significant corrections to be made.

Beam Modulation correction + correction for charge asymmetry shows significant improvement. Target X and target Y' still not fully corrected.

The fact that the slopes are reduced after correcting for charge differences proves two things we already knew:

- There are small but significant non-linearities in the system (signal chain and/or beam position monitors).
- These charge differences are strongly correlated with position differences.

These new results highlight, however, the importance of including charge differences in Qweak's natural beam motion linear regression to properly account for correlations between position and charge.

Summary

- Understanding and correcting for Helicity Correlated Beam Systematics is an important part of making a precise measurement of Q_w^p .
- Both Natural Beam Motion analysis and Driven Beam Modulation provide
- powerful tools to measure these effects.

Future Work

- Driven Modulation Analysis has been shown to correct modulated data → Self consistent. Need to look more closely at correction of non-modulated data.
- Investigate the effects of charge asymmetry on sensitivity slopes.
- Look at analysis using different detectors.
- Make Driven Modulation Analysis a permanent staple of Q_{weak} physics analysis.