

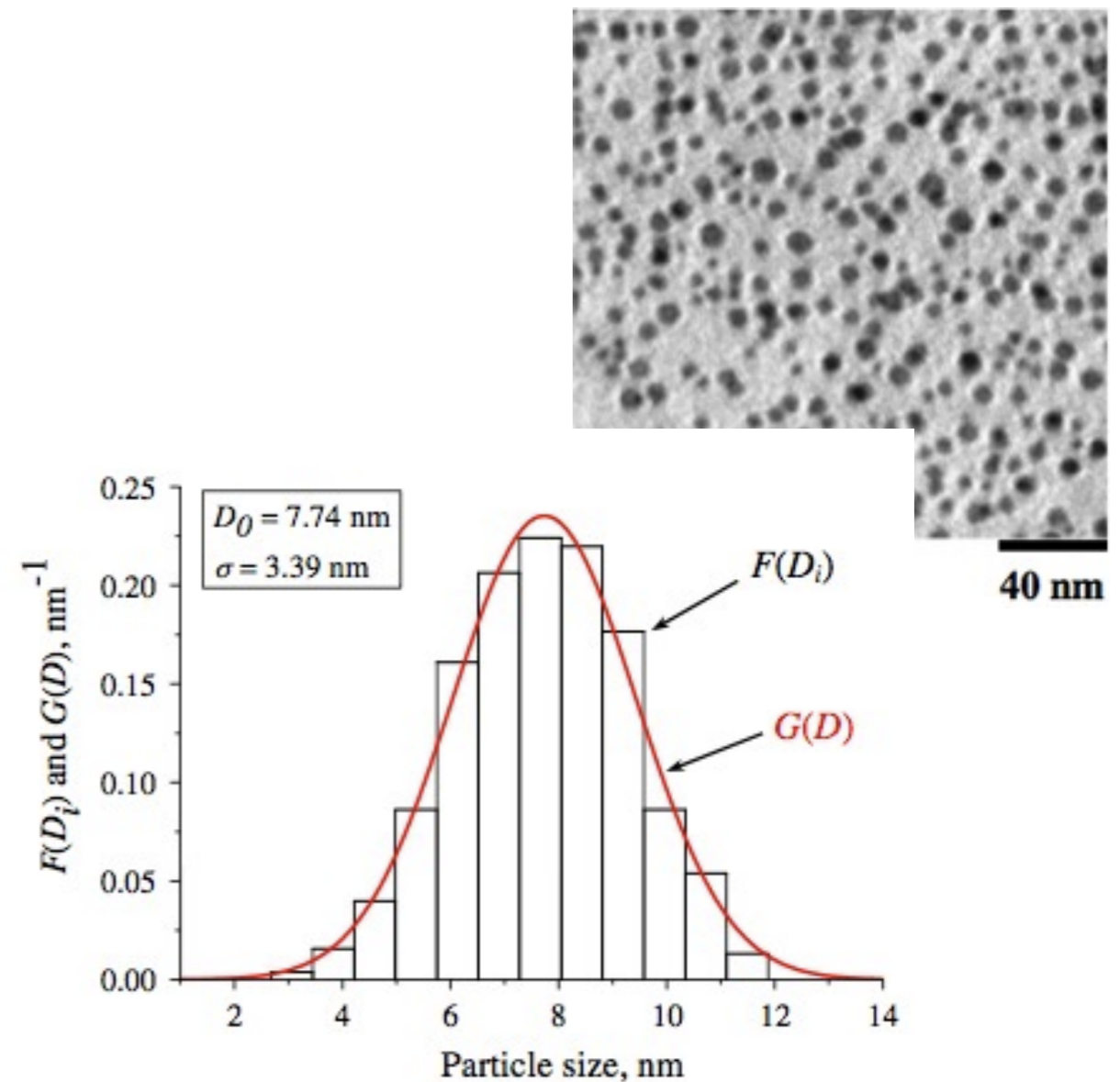
Effect of Size Distribution of Magnetic Nanoparticles on Metastability Across Dynamic Phase Boundary

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Department of Physics, Virginia Tech

Introduction

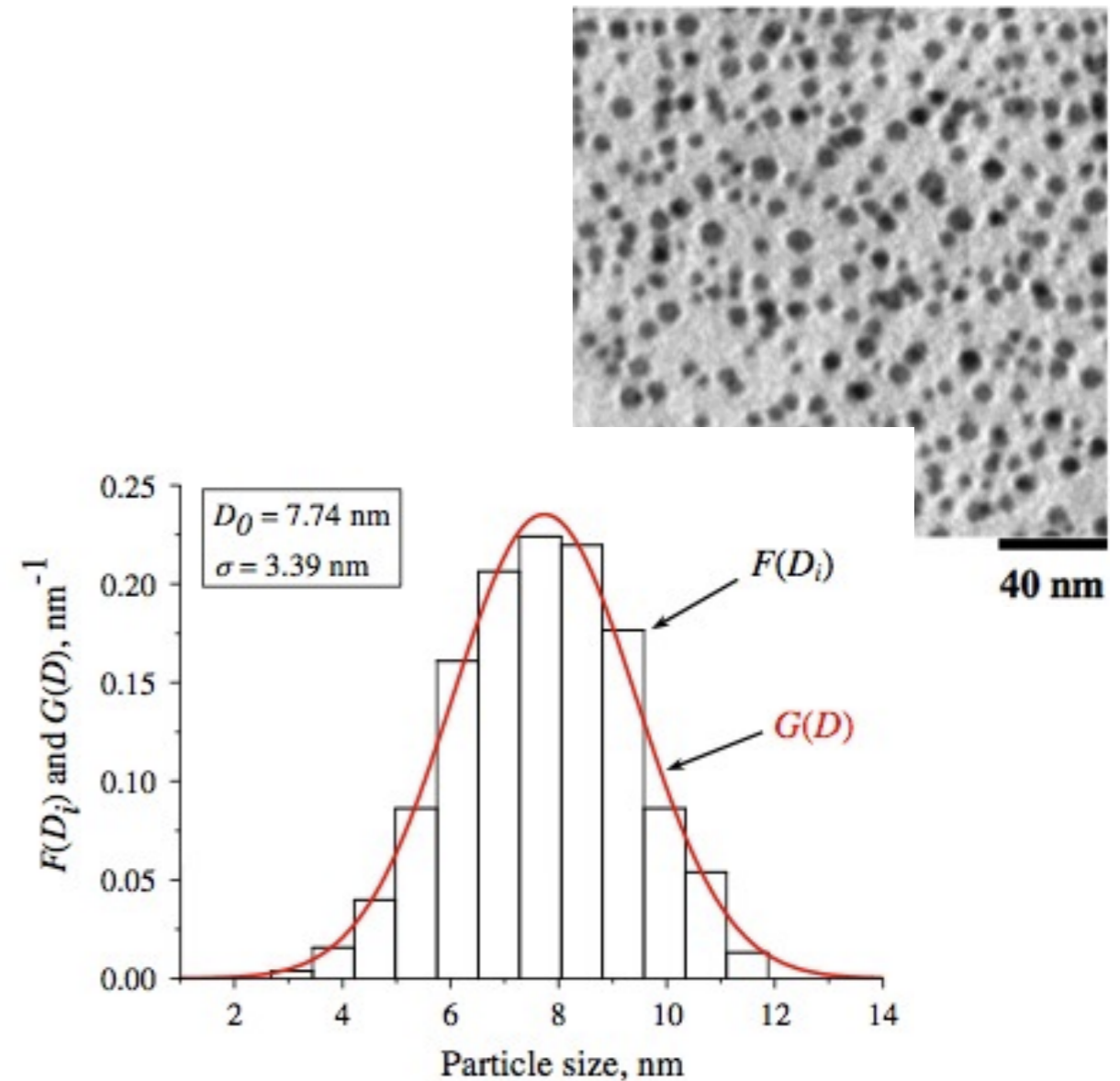
Introduction

- Experiments: a collection of magnetic nanoparticles have distribution in sizes and shapes and influence properties of the nanoparticles.



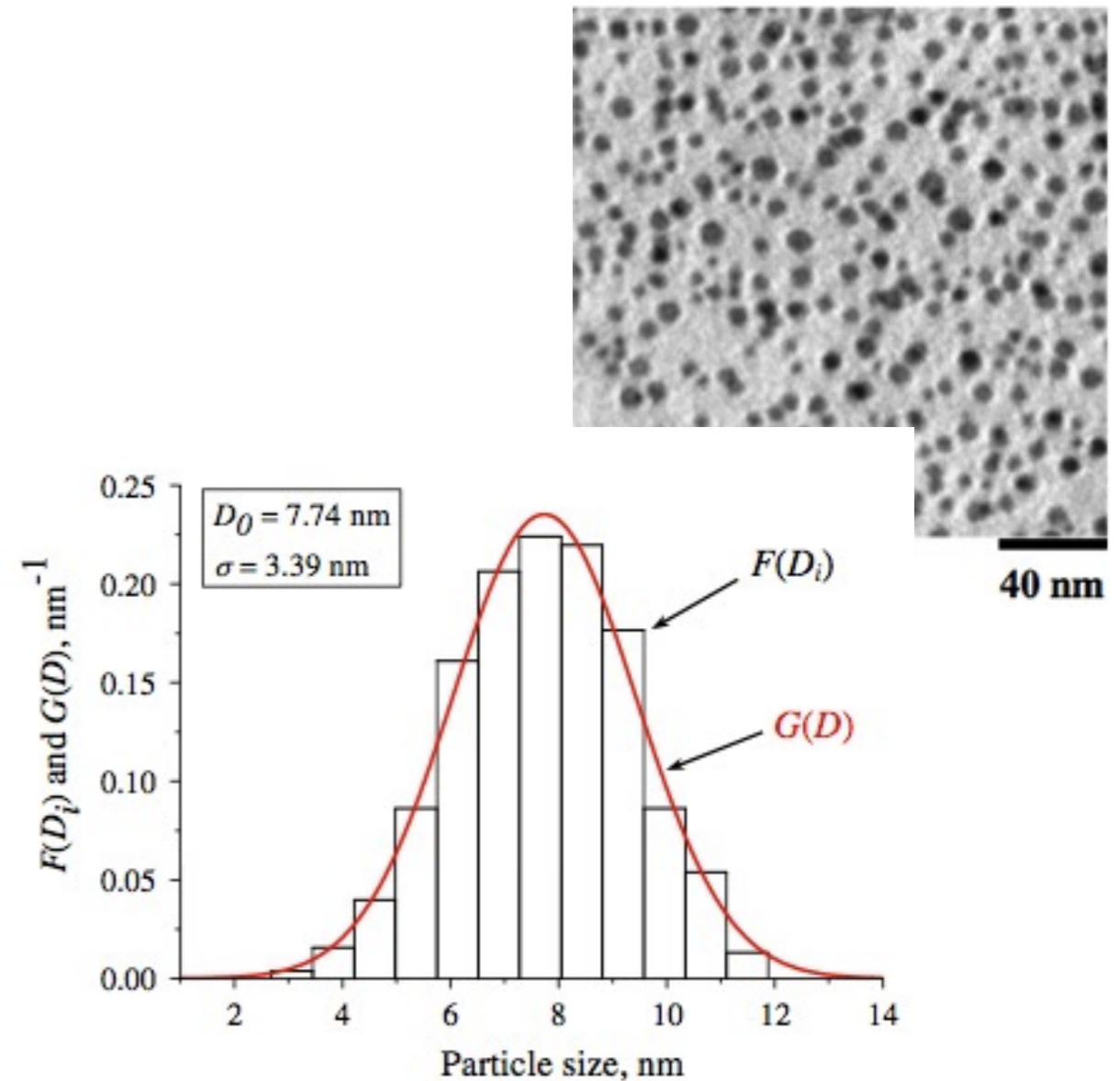
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- To simulate the size distribution, we used a Gaussian distribution in magnetic anisotropy parameter.
- We simulate metastability using kinetic Monte Carlo simulations.



Spin $S=1$ Blume-Capel Model for ferromagnets

$$\mathcal{H} = -2J \sum_{\langle i,j \rangle} S_{iz} S_{jz} - H \sum_i S_{iz} - D \sum_i S_{iz}^2$$

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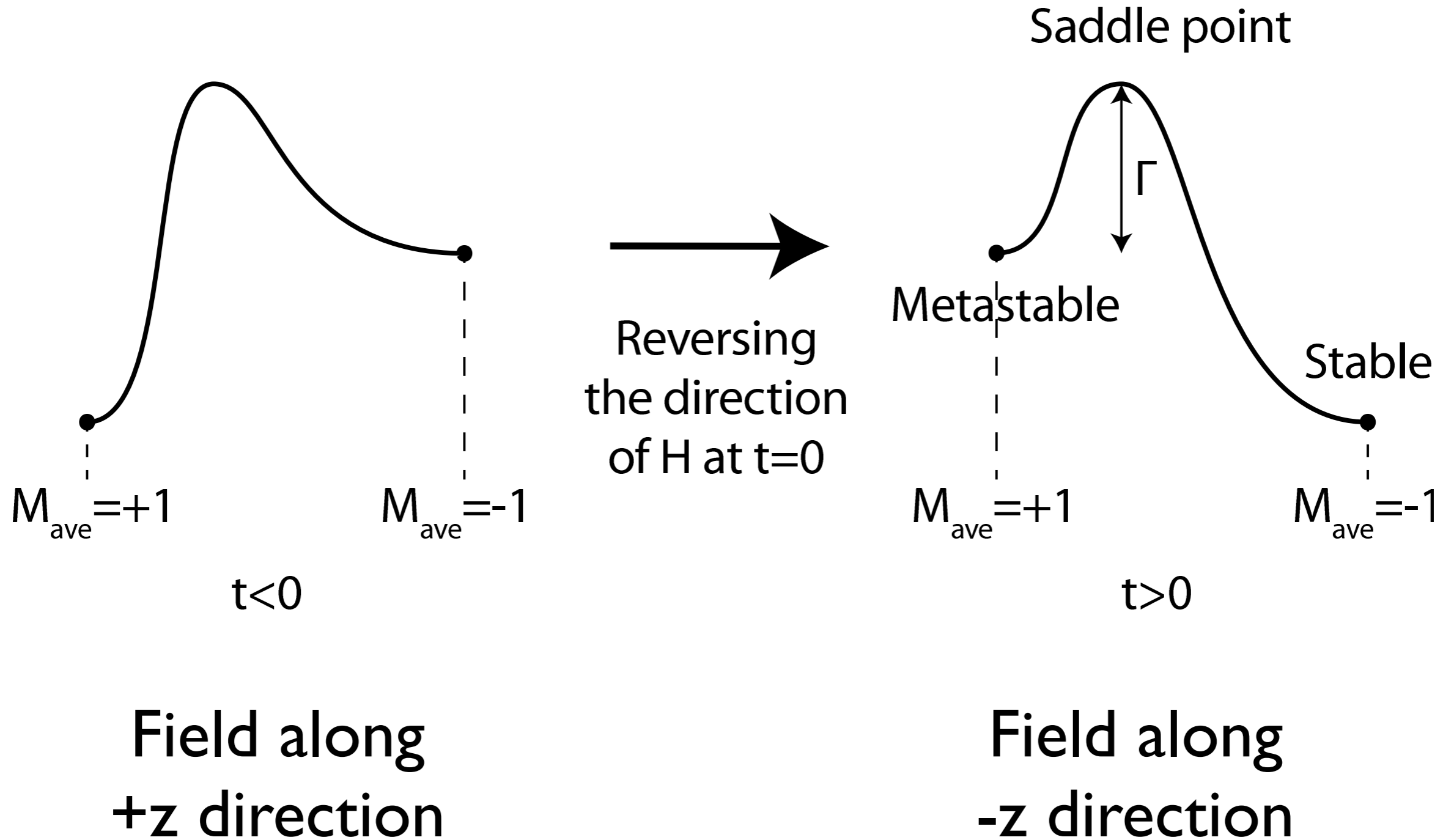
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- Spin $S=1$ can have a state of $M_z = \pm 1, 0$.
- D : Magnetic anisotropy parameter.
- $D > 0$ and we introduce Gaussian distribution.

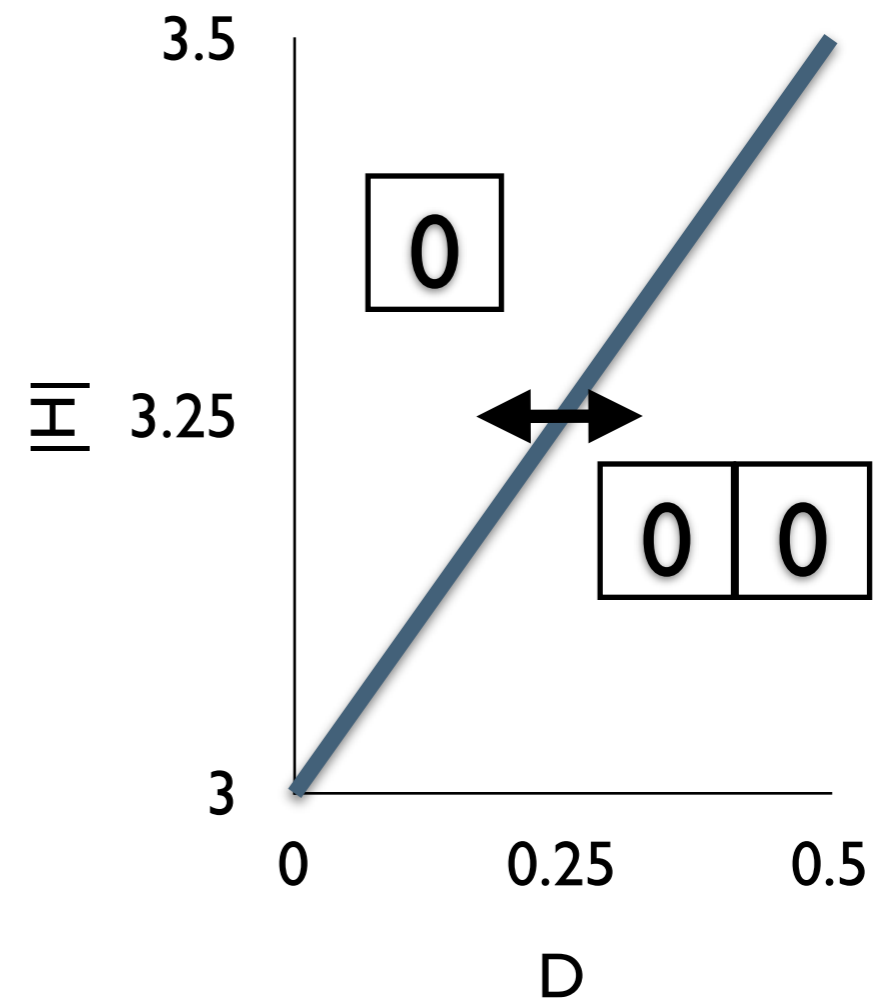
Metastability



- We are interested in the **single-droplet (SD) regime** where the metastable decay is driven by a single critical droplet.

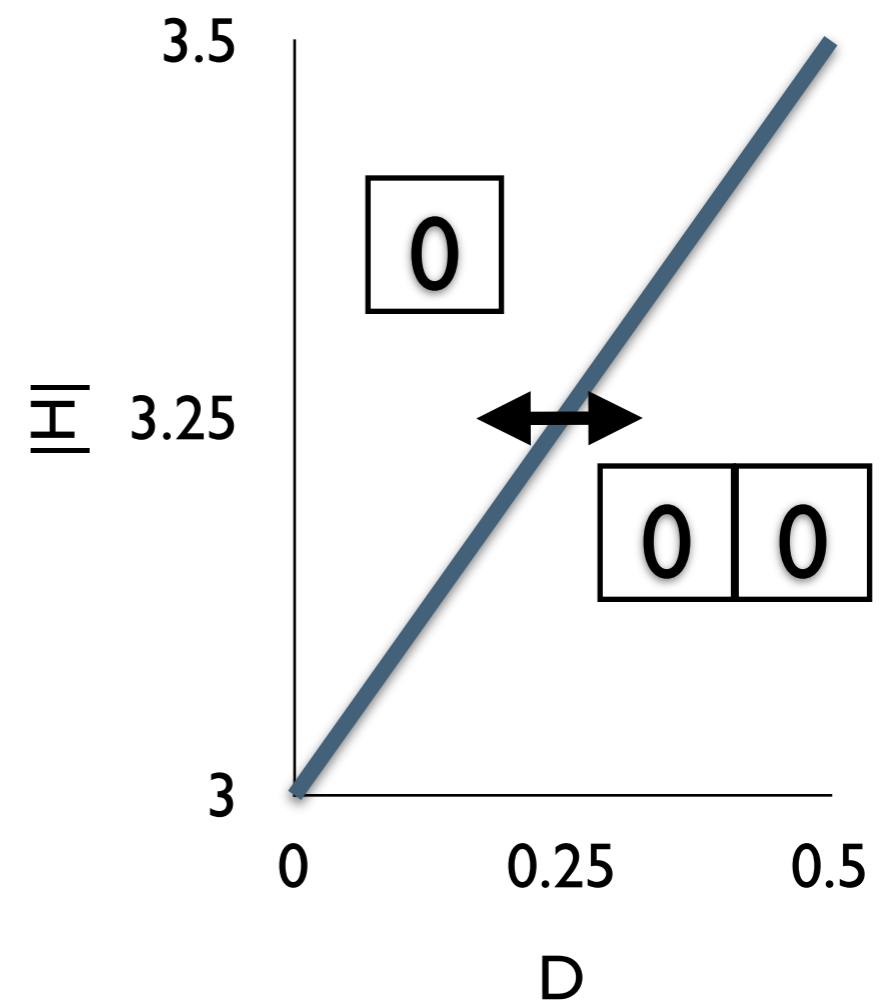
- We are interested in the **single-droplet (SD) regime** where the metastable decay is driven by a single critical droplet.
- For our model, SD regime appears when $|H| < D + 4$ and $T \rightarrow 0$. $L >$ droplet size.

Kinetic Monte Carlo Simulation



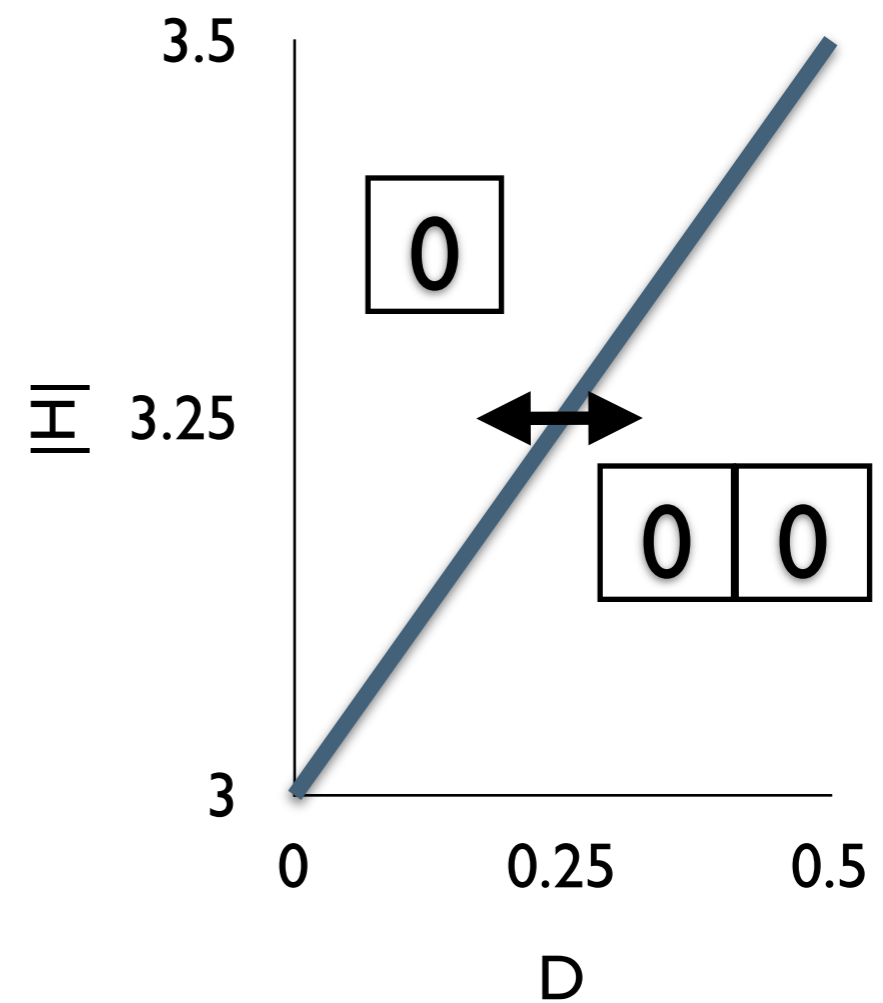
Kinetic Monte Carlo Simulation

- 2D square lattice ($L \times L$) with periodic boundary condition.



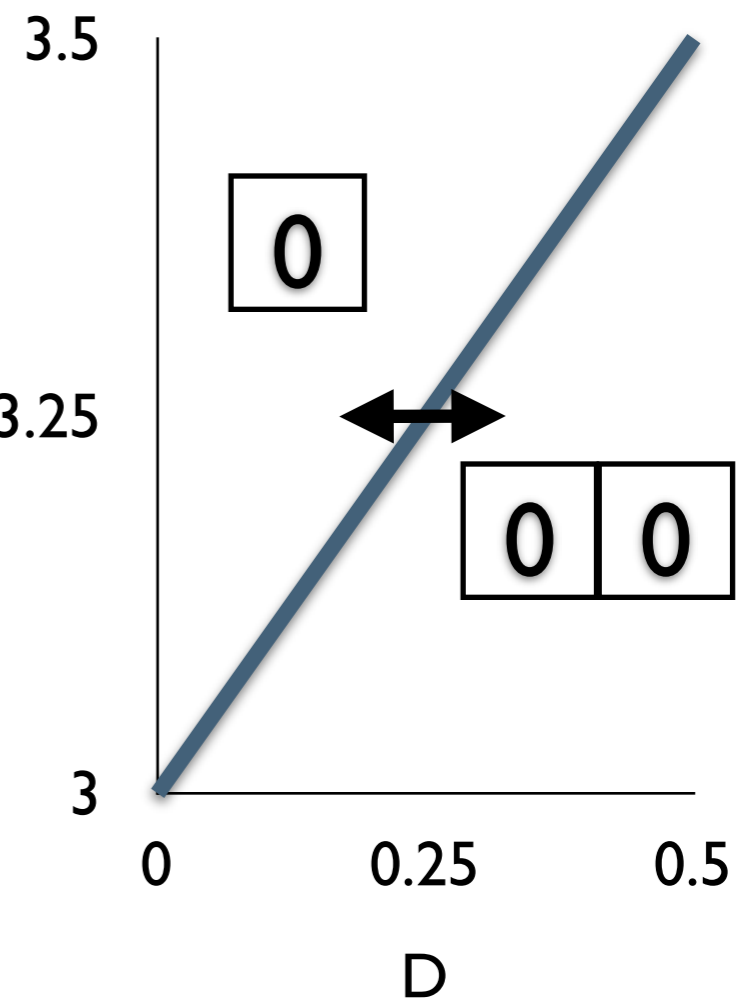
Kinetic Monte Carlo Simulation

- 2D square lattice ($L \times L$) with periodic boundary condition.
- 2000 thermal escapes.



Kinetic Monte Carlo Simulation

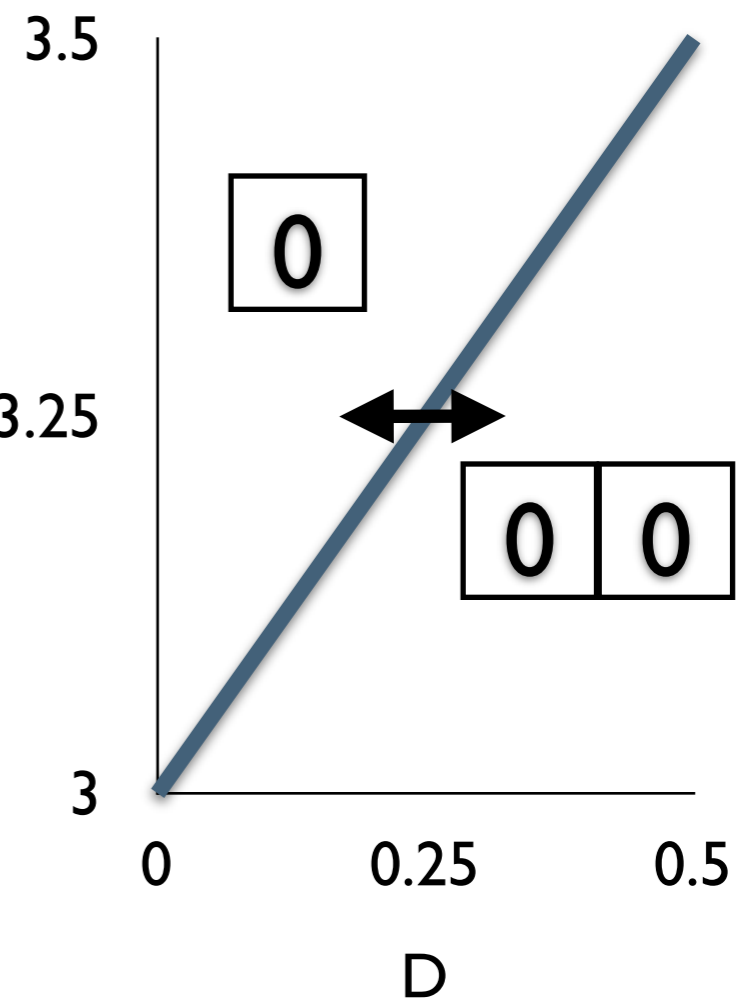
- 2D square lattice ($L \times L$) with periodic boundary condition.
- 2000 thermal escapes.
- A distribution across phase boundary $\bar{\Xi}$ at $H = -3.25$ (fixed) and $D_0 = 0.25$



Kinetic Monte Carlo Simulation

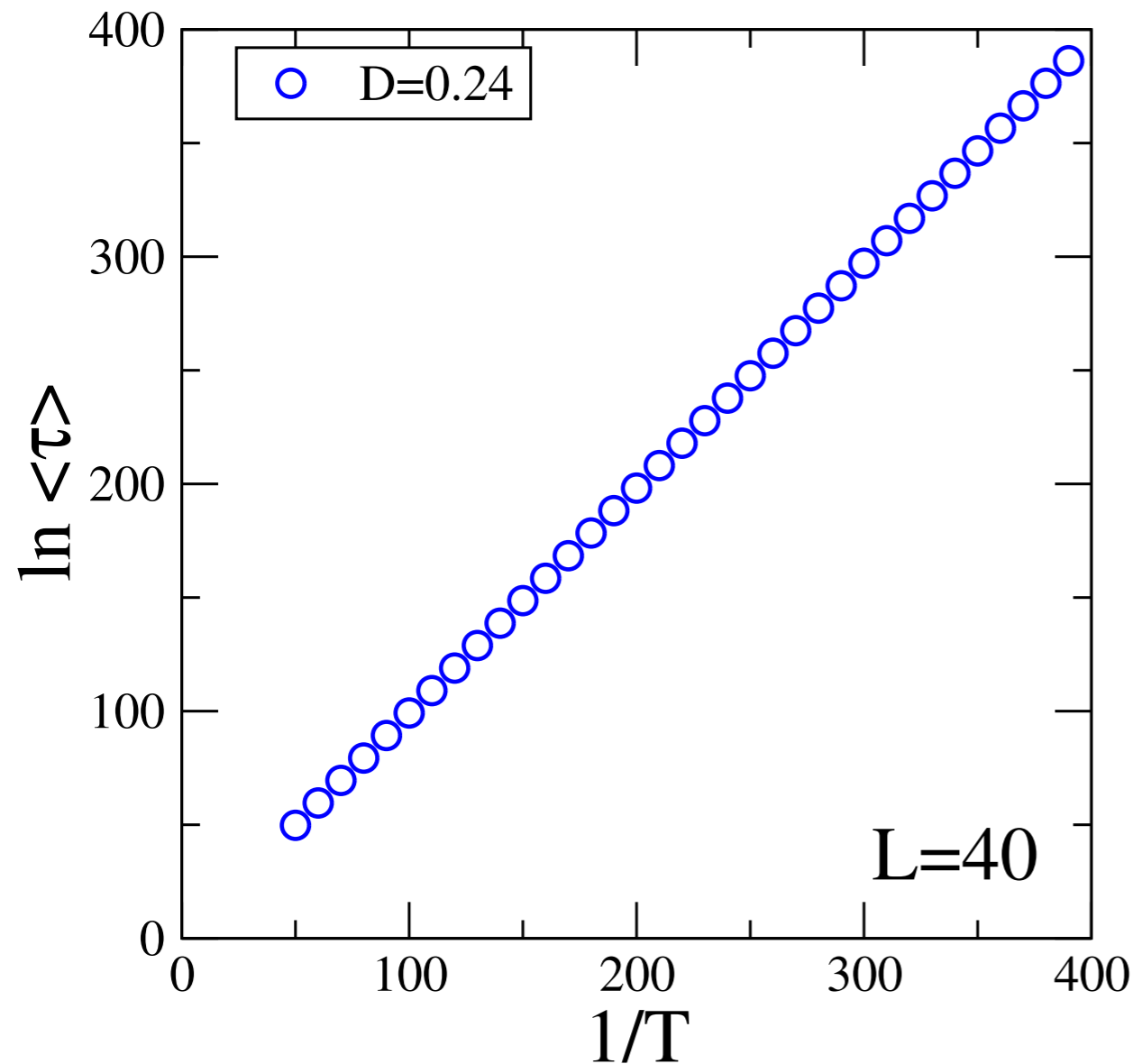
- 2D square lattice ($L \times L$) with periodic boundary condition.
- 2000 thermal escapes.
- A distribution across phase boundary $\bar{\Xi} = 3.25$ at $H = -3.25$ (fixed) and $D_0 = 0.25$
- Glauber transition rate:

$$W = \frac{1}{1 + e^{(E_{new} - E_{old})/T}}$$



Constant D

$$|H|=3.25 \quad D=0.24$$



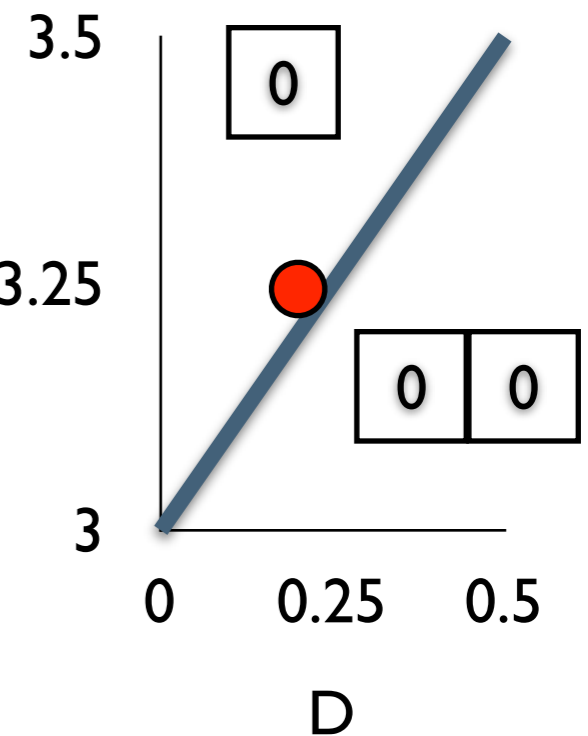
- Average lifetime follows Arrhenius Law

$$\langle \tau \rangle = A e^{\Gamma/T}$$

- Energy barrier $\Gamma = 4 - |H| + D$

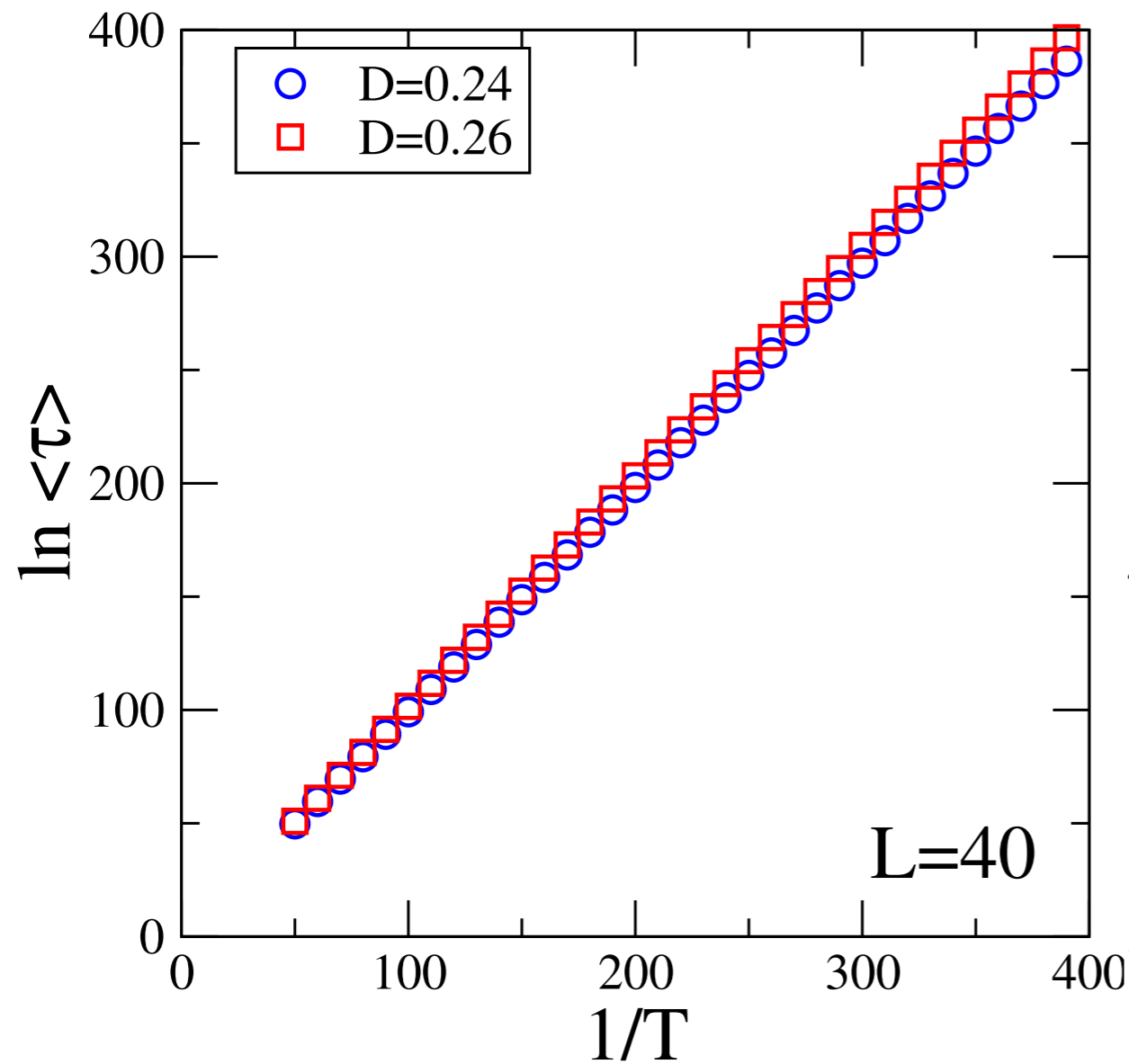
$$A = 9/8$$

$$\bar{\Gamma} = 3.25$$

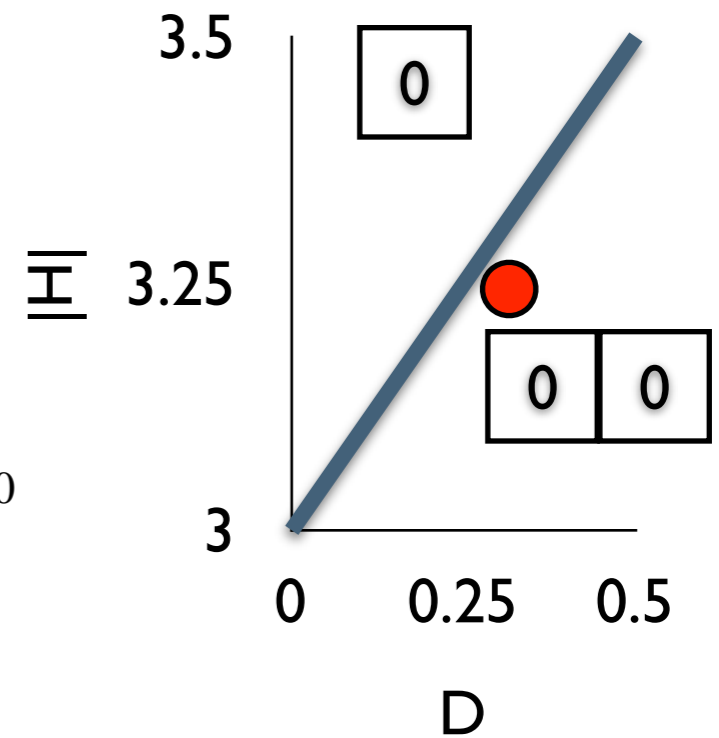
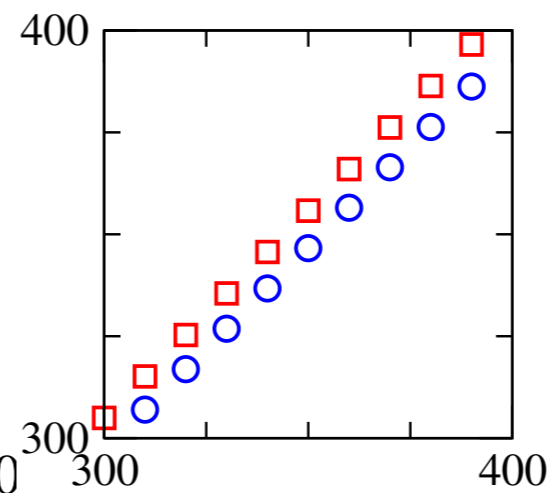


Constant D

$|H|=3.25$ $D=0.26$

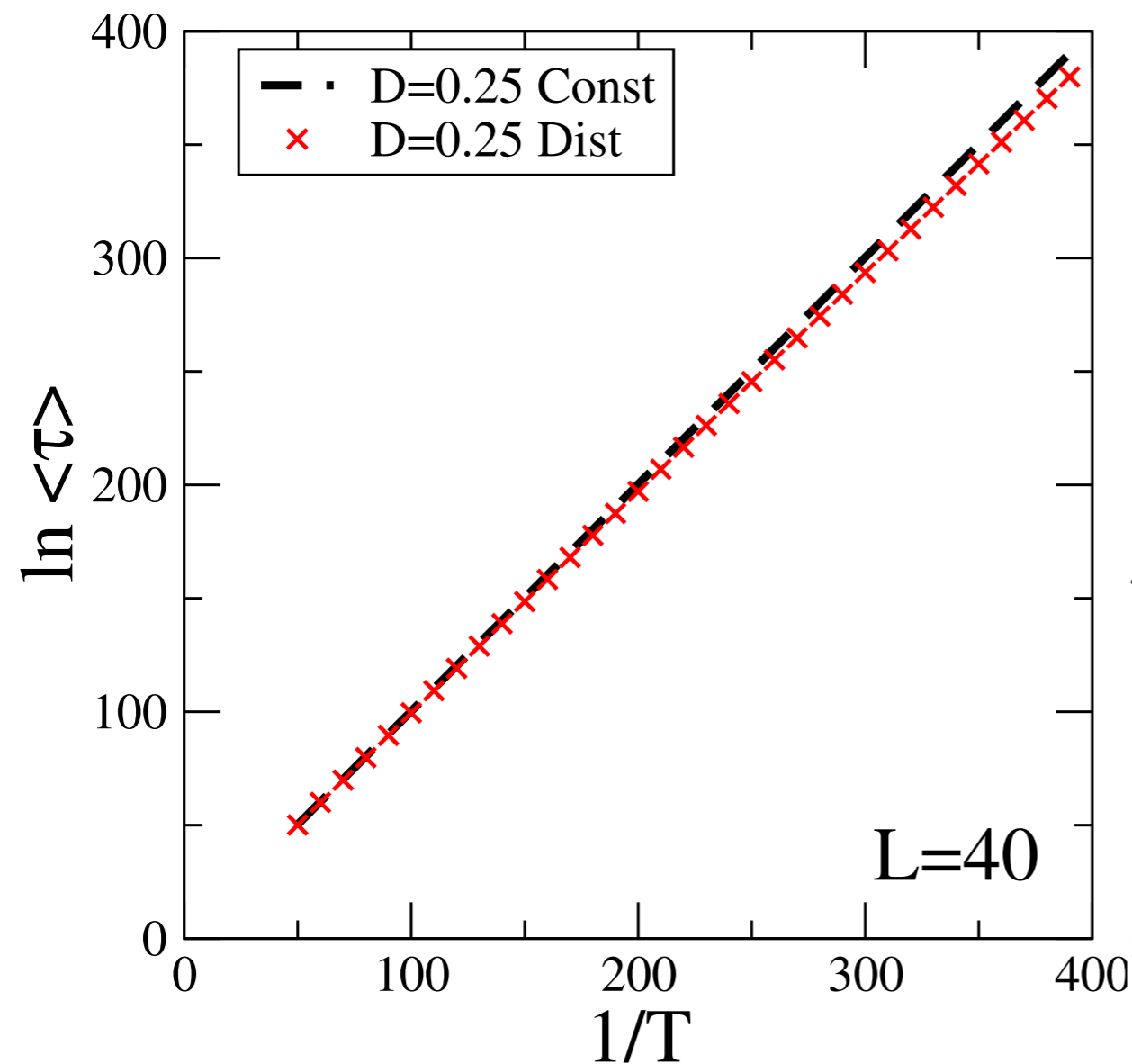


- Larger energy barrier: $\Gamma = 7 - 2|H| + 2D$

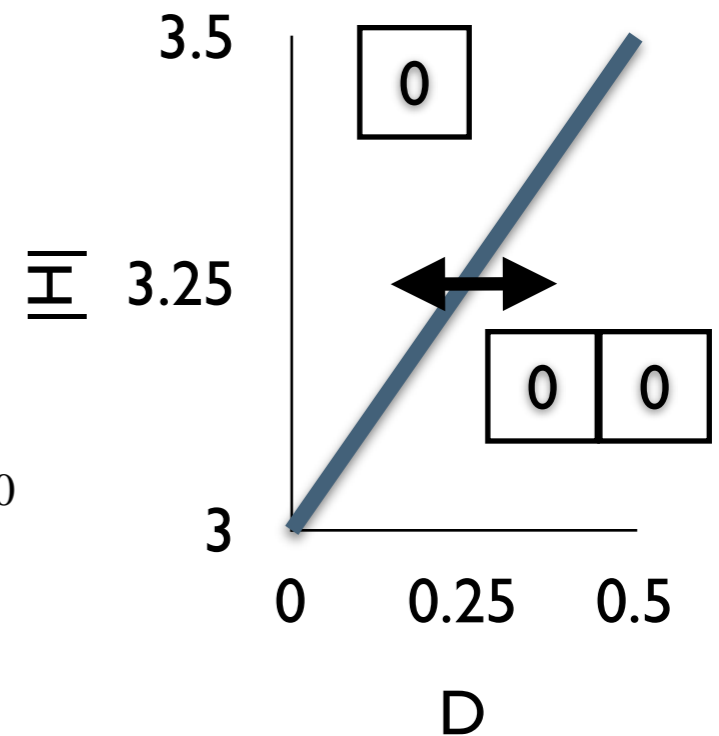
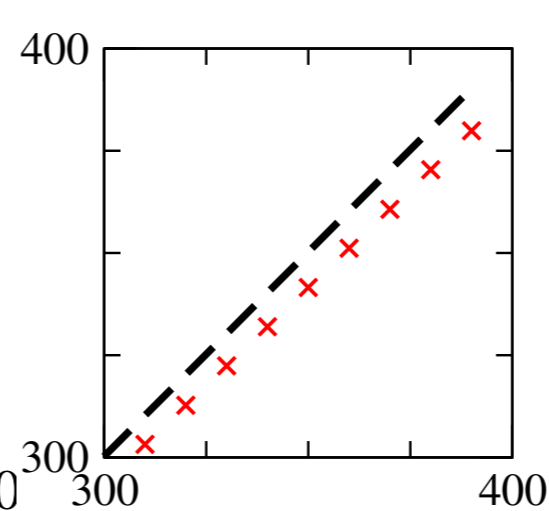


Gaussian Distribution in D

$$|H|=3.25 \quad D_0=0.25 \quad \sigma_D=0.0125$$

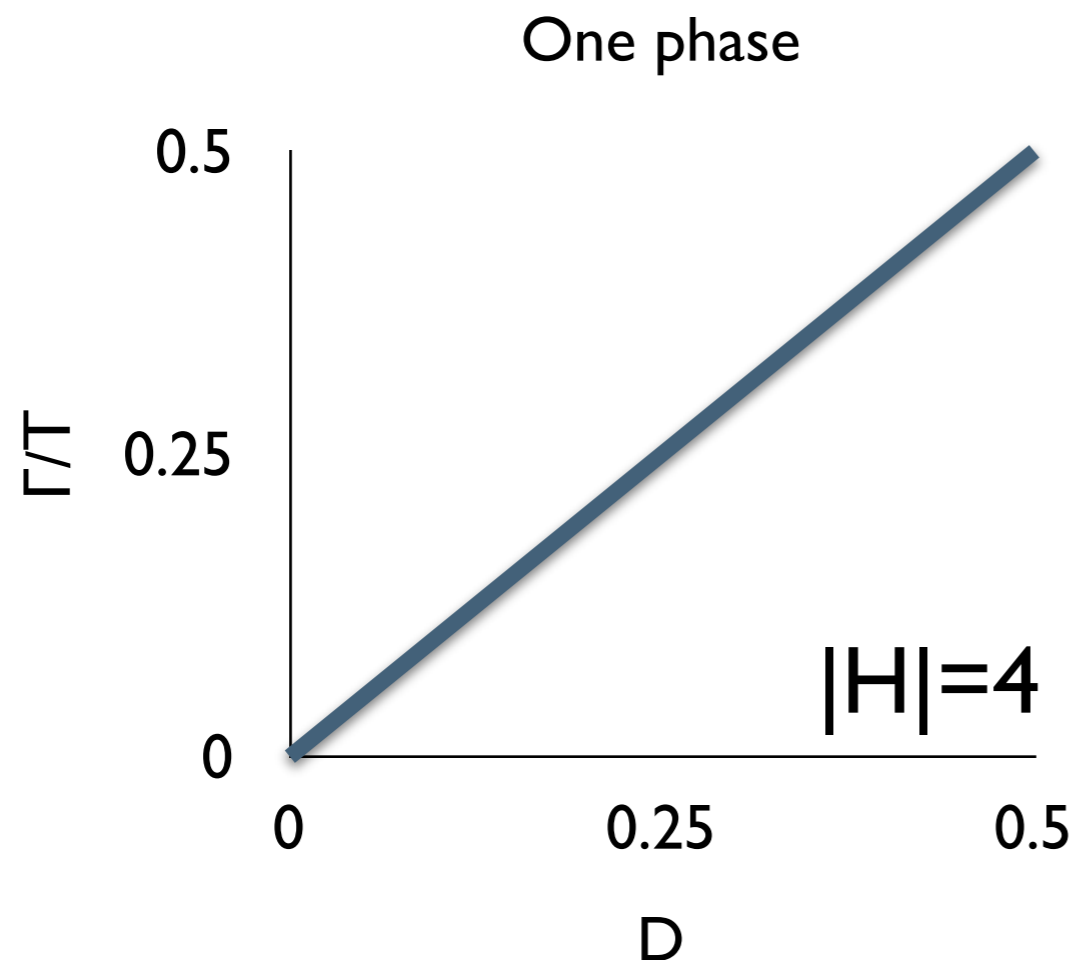


● : **Decrease** in lifetime with a distribution in D.



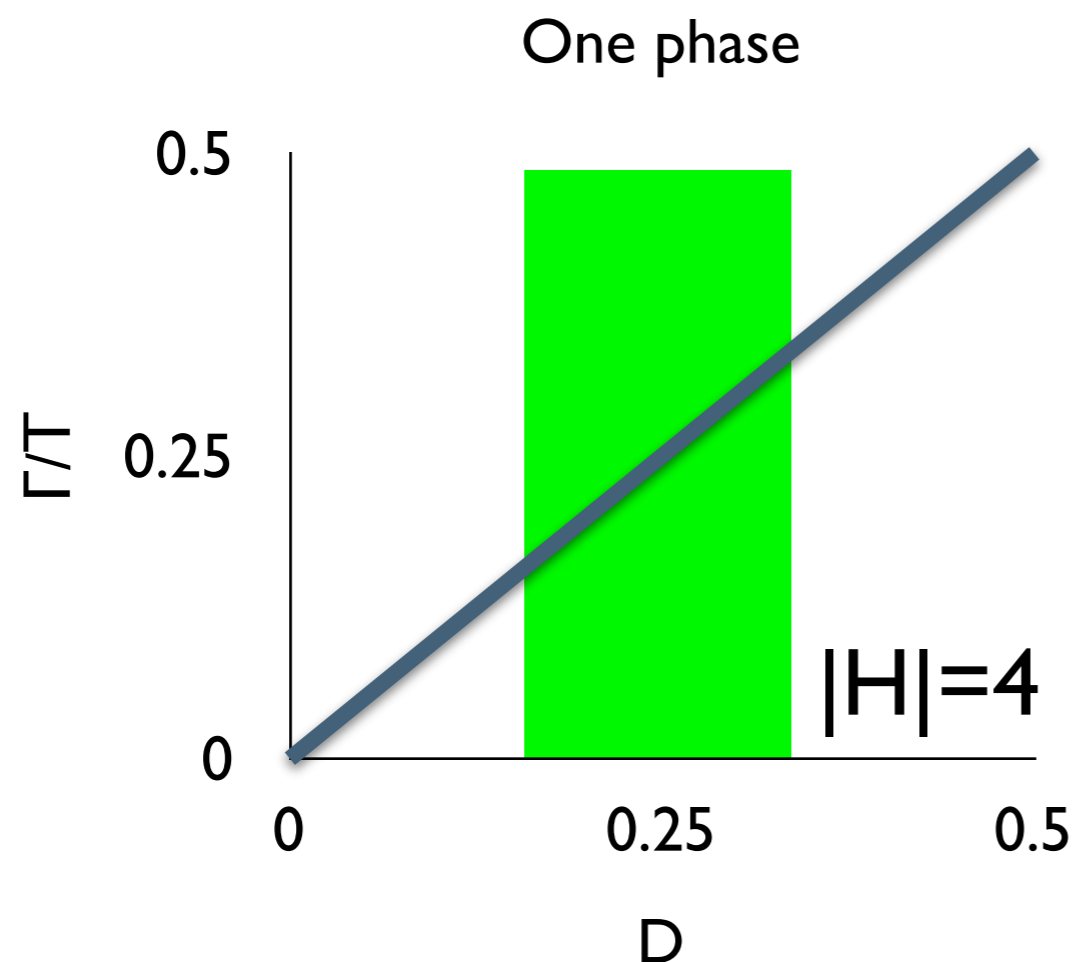
Comparison to Our Previous Study

- Previously, we studied \square phase with a distribution in D with fixed $|H|=4$. (Y.Y. and Park PRB **84**, 094415 (2011))
- Avoid high Γ and prefer low Γ especially in low temperature scenario



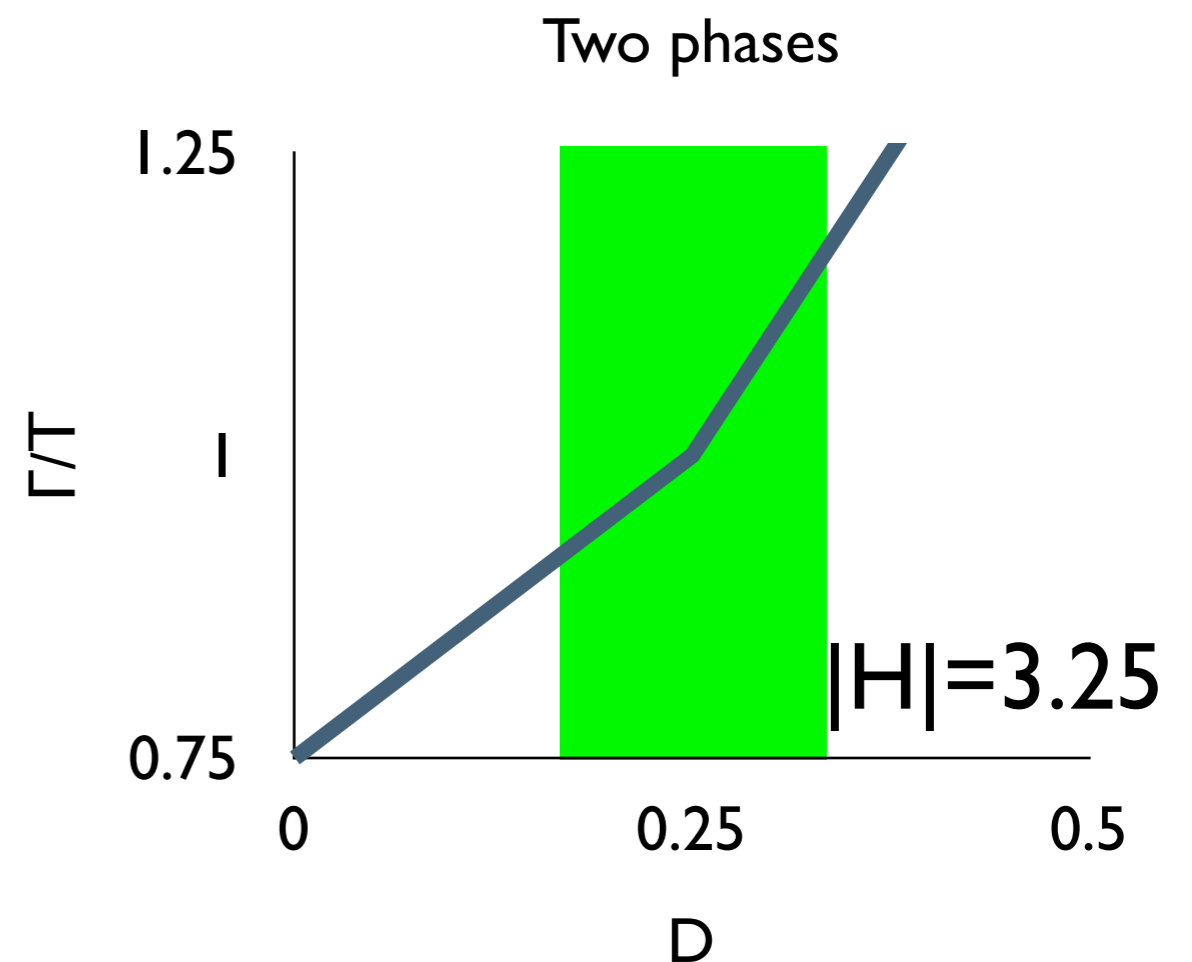
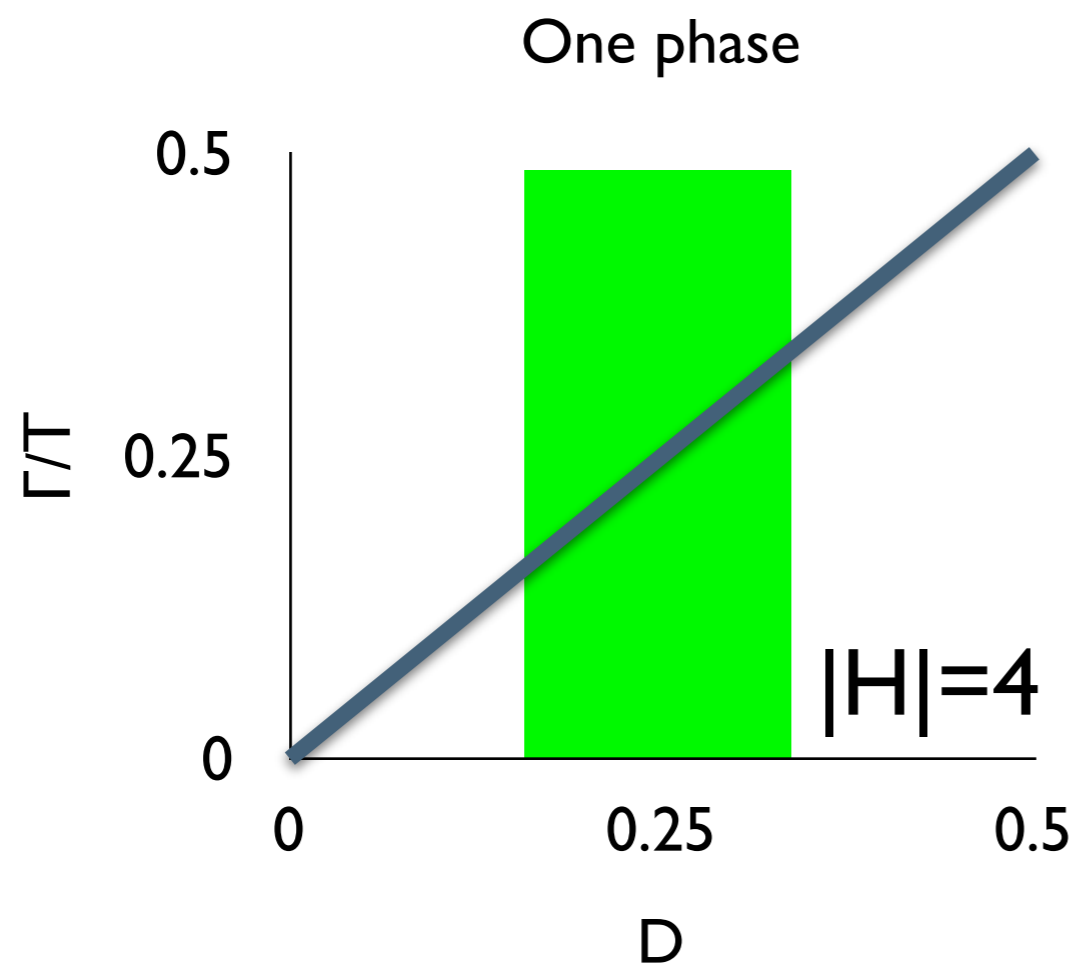
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Conclusion

- We find that the average lifetime of the metastable state decreases with distribution in D .
- The phase with smaller critical droplet size (smaller energy barrier) has the most contribution to the lifetime.
- Analytical expression - work in progress.